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Micky Rakotondrabe, Yassine Haddab, Philippe Lutz. High-Stroke motion modelling and voltage/frequency proportional control of a stick-slip microsystem.. IEEE International Conference on Robotics and Automation, ICRA'2007., Apr 2007, Rome, Italy. pp.4490-4496. <hal-00163051>

HAL Id: hal-00163051

<https://hal.science/hal-00163051v1>

Submitted on 16 Jul 2007

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High-Stroke Motion Modelling and Voltage/Frequency Proportional Control of a Stick-Slip Microsystem

Micky Rakotondrabe, Yassine Haddab and Philippe Lutz

Abstract—A new control type for stick-slip microsystems is proposed in this paper: the voltage/frequency (U/f) proportional control. It gives a best resolution relatively to the classical control algorithm. It is also an englobalization of three classical controllers: the sign controller, the classical proportional controller and the frequency proportional controller. A high stroke model of a stick-slip microsystem is first given. Then, we theoretically analyze the performances of the closed loop process with the U/f controller. Finally, we give some experimental results obtained with different values of the proportional gains.

I. INTRODUCTION

Among the stepping principles for micropositioning, stick-slip [1] is the most used : examples are given in [2][3][4][5]. Stick-slip actuators, generally based on piezoelectric materials, are characterized by their simplicity, rapidity, low cost and possibility of batch fabrication. Two modes of motion can be obtained with a stick-slip micropositioner [6] : the stepping mode and the scanning mode. The stepping mode consists in applying a sawtooth voltages to the micropositioner and let it move step by step, in high range and with a high velocity on the workspace (Fig. 1-a, b and c). The resolution in this mode is limited to one step. When the difference between the target position and the current position becomes less than the value of a step, the legs (piezoelectric actuators) are bent slowly until the final position is reached (Fig. 1-d). This is the scanning mode and the obtained resolution can be very high. It is possible to have a similar resolution in the stepping mode by reducing the amplitude U of the sawtooth but the vibrations occurring in each steps [7] may influence the performances.

Two modes of control for stick-slip micropositioners are possible: control in stepping mode for high stroke positioning and control in scanning mode for fine positioning. Each of them may use an open-loop or a closed-loop structure. As the fine positioning may be controlled in closed loop with standard controllers (*PID*, optimal controllers, robust controllers, etc.), this paper deals with the high stroke positioning control.

The first section is a brief presentation of existing control methods. Then, we present the high stroke characteristics and model our stick-slip microsystem for ex-

periments. After that, we detail a new type of control : the voltage/frequency proportional control. It inferes good resolution of the motion relative to the existing methods. On the other hand, the vibrations possibilities are reduced in this approach. Finally, we present the experimental and simulation results.

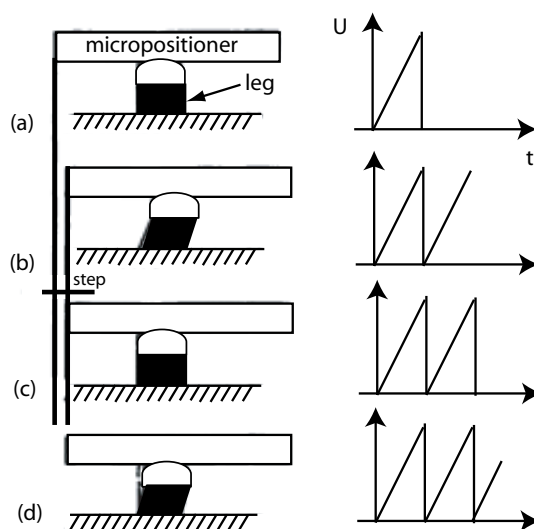


Fig. 1. Stick-slip principle [6]. a, b and c : stepping mode. d : scanning mode.

II. EXISTING METHODS

Open-loop control based on step counting as in stepper motors are not applicable for stick-slip microsystems because:

- the steps are never identical along a displacement due to the nonlinearities phenomena coming from the friction and the piezoelectric materials,
- the step is very low relative to the distance, then the number of steps of the displacement is very high. Thus, small counting error may generate high static error,
- the step errors ($step_{errors} = step_{estimated} - step_{real}$) accumulate along the motion unlike those of in stepper motors,
- the external disturbances (adhesion forces, thermal effect, vibrations of the workspace etc.) influence

the accuracy.

Thus, the classical employed closed-loop controller is the following algorithm [8] except for a sign:

$$\begin{aligned} & \text{While } |x_c - x| \geq \text{step} \text{ Do} \\ & \quad \text{apply one step} \\ & \text{EndWhile} \end{aligned} \quad (1)$$

where x_c is the target position and x is the current position. When the accuracy of the sensor is worse than the value of a step, the term *step* in the precedent algorithm is replaced by $n \times \text{step}$ which gives the limit of the sensor accuracy.

Another method based on the hybrid modeling of the stick-slip systems has been proposed in [9]. The hybrid model is approximated into a continuous one (called dehybridization) and a continuous controller is applied (*PD*). This method gives the possibility to reach the target position without using two separate control modes (stepping and scanning). However, the dehybridization requires a hybrid controller in series with the stick-slip microsystem which makes the whole algorithm more complex than the precedent algorithms.

Finally, *Breguet and Clavel* proposed a numerical frequency proportional controller in [10]. In this method, the frequency is proportional to the error while the amplitude U of the voltage still stays constant. Thereby, as the step is constant along the motion, the resolution is also constant.

III. CHARACTERISTICS AND MODELLING OF THE MICROSYSTEM

Fig. 2-a shows the stick-slip microsystem [11] used for experiments in this paper. Fig. 2-b shows how the microactuators are spread out inside the microsystem. It has two degrees of freedom (2DoF: linear and angular) but our test will only be performed in the linear motion. The maximal step value of the microsystem is about 200nm and the speed can reach 2mm/s . These performances are obtained using a sawtooth input voltage with an amplitude of $\pm 150\text{V}$ and a frequency of 10kHz .

When applying a continuous input voltage U , the microsystem works in scanning mode. Hypothesizing that the scanning displacement x_{sc} is dynamically linear relative to the voltage, we can write the following function:

$$X_{sc}(s) = G_{sc}(s).U(s) \quad (2)$$

Where s is the Laplace variable and G_{sc} is the transfer function connecting the amplitude U and the scanning position x_{sc} . When the voltage is abruptly removed, the resulting step x_{step} is smaller than the corresponding amplitude x_{sc}^U so that [12](Fig. 3-a):

$$x_{step} = x_{sc}^U - \Delta_{back} \quad (3)$$

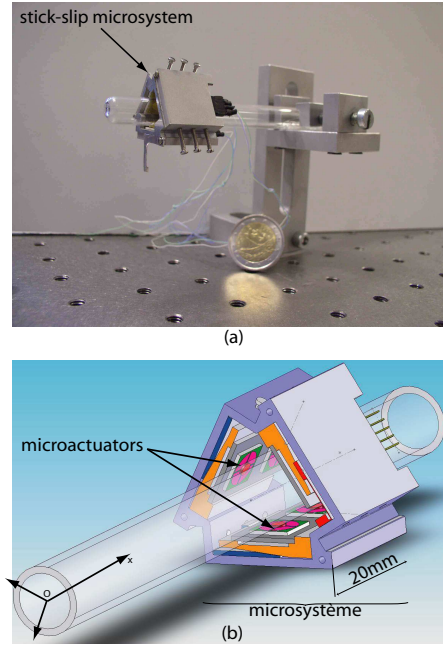


Fig. 2. The stick-slip microsystem.

Hypothesizing that the flashback Δ_{back} is dynamically linear relative to the amplitude U , the step can be written as follow:

$$X_{step}(s) = G_{step}(s).U(s) \quad (4)$$

When the sequence is repeated (stepping mode) with a frequency $f = 1/T$, the dynamic of the continuous part G_{step} is not visible and the microsystem works with a quasi-static manner. Thus, the step can be approximated by:

$$x_{step} = \alpha.U \quad (5)$$

where $\alpha > 0$ is the static gain of G_{step} .

From the Fig. 3-b and the (Eq. 5), we infer the bilinearity of the speed:

$$v = \dot{x} = \alpha.U.f \quad (6)$$

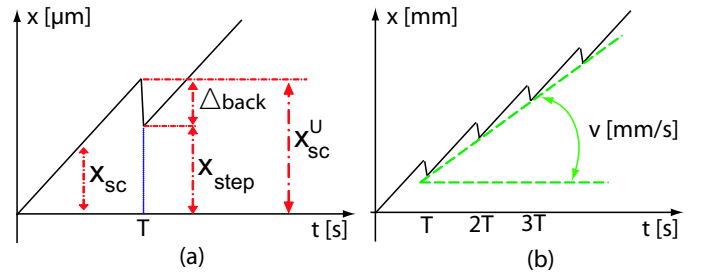


Fig. 3. a: motion of a stick-slip system. b: speed approximation.

When the amplitude U is below a value U_0 , the torque is not sufficient and the microsystem can't move. Thus,

an offset is introduced to the (Eq. 5) and the final model becomes:

$$\begin{cases} v = 0 & \text{if } |U| \leq U_0 \\ v = \alpha.f.(U - \text{sgn}(U).U_0) & \text{if } |U| > U_0 \end{cases} \quad (7)$$

Fig. 4 summarize the speed performances of the microsystem. Until $f = 10\text{kHz}$, the speed is approximately linear versus f (Fig. 4-a). Above this frequency value, a saturation and a fluctuation appear. The identified parameters are: $\alpha = 15.652173 \times 10^{-7}$ and $U_0 = 35\text{V}$ (Fig. 4-b).

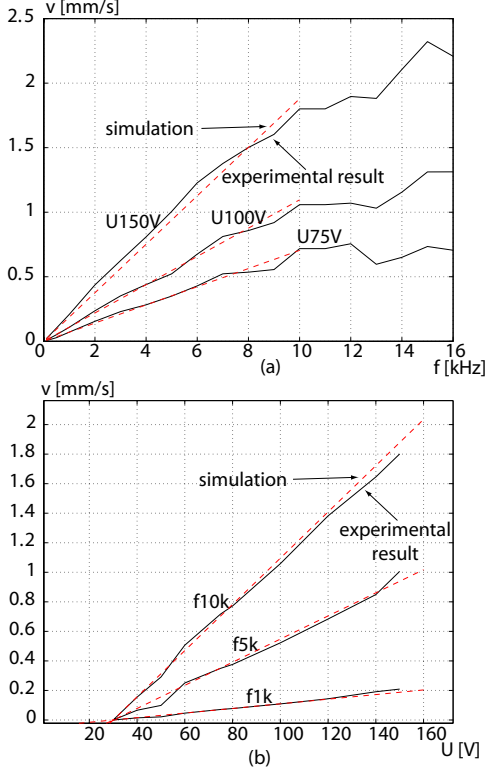


Fig. 4. Speed performances of the microsystem. a: speed versus the frequency f . b: speed versus the amplitude U .

IV. U/F PROPORTIONAL CONTROL

A. Principle scheme

The principle scheme of U/f proportional control is shown in Fig. 5. The saturations avoid the overvoltages and limit the microsystem work inside the linear zone of the frequency. The proportional gains $K_U > 0$ and $K_f > 0$ are to be adjusted like in a classical proportional controller.

B. Equations and analysis

In this section, we express the speed according to the values of K_U and K_f . Let U_s and f_s indicate the saturations respectively used for the voltage and for the frequency. a)

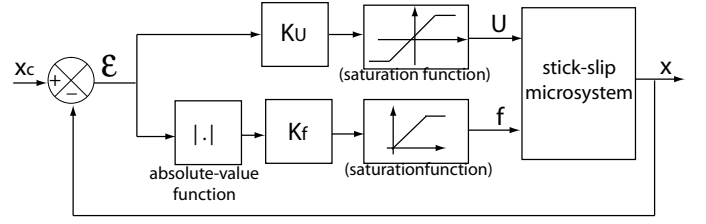


Fig. 5. Principle scheme of the U/f proportional control.

$$\text{if } K_U \cdot |x_c - x| > U_s \text{ and } K_f \cdot |x_c - x| > f_s$$

From the Fig. 5 and the bi-affine expression in (Eq. 7), we obtain:

$$\dot{x} = \alpha.f_s.(U_s - U_0).\text{sgn}(x_c - x) \quad (8)$$

This case is equivalent to a sign control (Fig. 6-a). When the microsystem is at the neighborhood of the final position, there are oscillations in sign control. The frequency and the amplitude of these oscillations depend on the response time T_r of the process, on the refreshing time T_s (Fig. 6-b) of the controller and on the frequency saturation f_s . It is the way that realtime feedback systems give the best performances.

b) $\text{if } U_0 > K_U \cdot |x_c - x| \quad \forall \quad f = K_f \cdot |x_c - x|$ we have:

$$\dot{x} = 0 \quad (9)$$

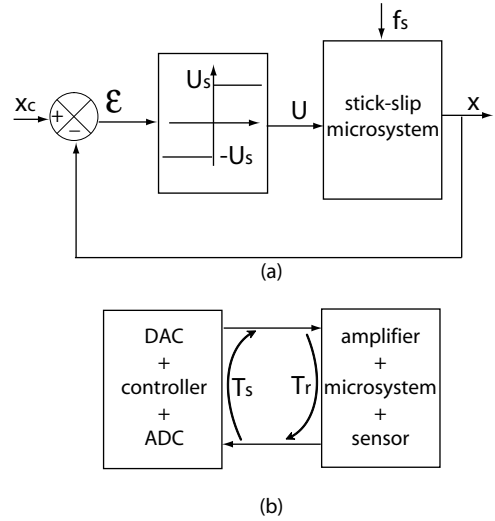


Fig. 6. a: sign control. b: oscillations in sign control.

c) $\text{if } U_s \geq K_U \cdot |x_c - x| \geq U_0 \text{ and } K_f \cdot |x_c - x| > f_s$ Here, the closed loop process is equivalent to a voltage proportional control (Fig. 7), also known as proportional control in the control theory.

The equation of the closed loop is:

$$\dot{x} = \alpha.f_s.(K_U \cdot (x_c - x) - \text{sgn}(x_c - x).U_0) \quad (10)$$

For simplification but without loss of generality, let us take a positive target position x_c and an initial value

$x(t = 0)$ equal to zero, we obtain the following Laplace transformation:

$$X = \frac{1}{1 + \frac{1}{\alpha \cdot f_s \cdot K_U} \cdot s} \cdot X_c - \frac{\frac{1}{K_U}}{1 + \frac{1}{\alpha \cdot f_s \cdot K_U} \cdot s} \cdot U_0 \quad (11)$$

where s is the Laplace variable. The (Eq. 11) means that the closed loop process is a first order dynamic system with a static gain equal to unity and a disturbance U_0 . We can infer that, the more K_U is great, the more a voltage proportional control of a stick-slip system is accurate. The voltage proportional control always gives stability because it is a first order.

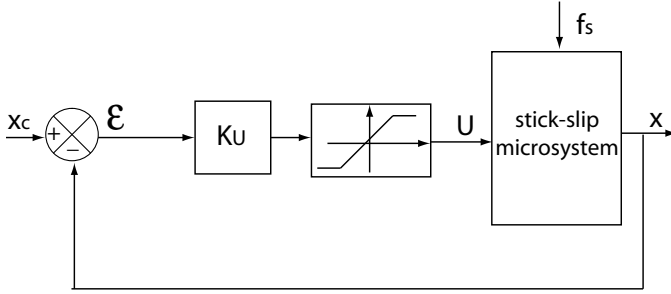


Fig. 7. Voltage proportional control.

d) *if* $K_U \cdot |x_c - x| > U_s$ *and* $f_s \geq K_f \cdot |x_c - x|$
This case is equivalent to a frequency proportional control (Fig. 8).

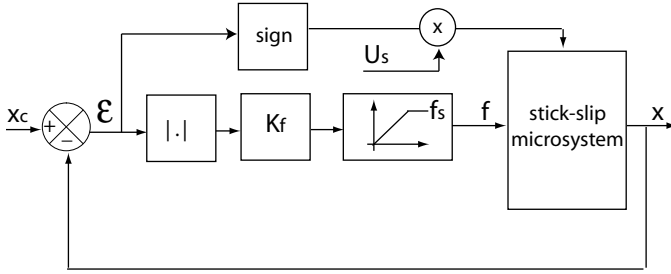


Fig. 8. Frequency proportional control.

The following equation is easily obtained:

$$\dot{x} = \alpha \cdot K_f \cdot |x_c - x| \cdot (U_s - U_0) \cdot \text{sgn}(x_c - x) \quad (12)$$

The expression (Eq. 12) is equivalent to the following transfer function:

$$\frac{X}{X_c} = \frac{1}{1 + \frac{1}{\alpha \cdot K_f \cdot (U_s - U_0)} \cdot s} \quad (13)$$

The (Eq. 13) differently means that in this case, the closed loop process is a first order system with a static gain equal to unity. The stability is always ensured.

e) *if* $U_s \geq K_U \cdot |x_c - x| \geq U_0$ *and* $f_s \geq K_f \cdot |x_c - x|$
The frequency and the voltage are both proportional to

the error ε . From the Fig. 5 and the formula (Eq. 7), we have the following expression:

$$\dot{x} = \alpha \cdot K_f \cdot |x_c - x| \cdot (K_U \cdot (x_c - x) - \text{sgn}(x_c - x) \cdot U_0) \quad (14)$$

The expression (Eq. 14) is equivalent to:

$$\frac{dx}{dt} = (\alpha \cdot K_f \cdot U_0 - \alpha \cdot K_f \cdot K_U \cdot |x_c - x|) \cdot x + (-\alpha \cdot K_f \cdot U_0 + \alpha \cdot K_f \cdot K_U \cdot |x_c - x|) \cdot x_c \quad (15)$$

which is in the form of:

$$\frac{dx}{dt} = A(x_c, x) \cdot x + B(x_c, x) \cdot x_c \quad (16)$$

Where A and B are the state and the input coefficients. Here, the closed loop system has a 1st order pseudo-linear behavior.

C. Stability

According to the values of K_U , K_f and the error $(x_c - x)$, all the above cases may appear during a displacement. Without loss of generality, let us suppose that $x_c = 0$ and $x(t = 0) > 0$ for the stability analysis. Let us divide the displacement into two phases (Fig. 9):

- **phase-1**; the error $(x_c - x)$ is initially high so that the voltage U and the frequency f are both in their saturations (case a)). The speed is constant.
- **phase-2**; the error becomes smaller and the speed is not yet constant (equivalent to the other cases).

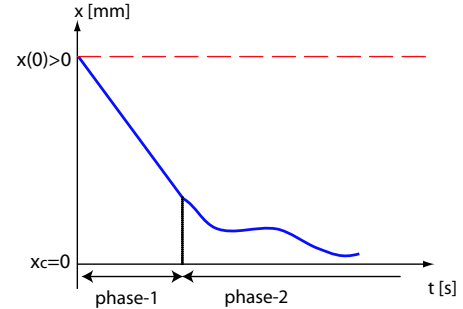


Fig. 9. The displacement may be divided into two phases.

As the equations are quasi-static, ie. there is no acceleration, one case does not influence the succeeding case. So, the phase-2 may be studied independently from the phase-1. In the phase-2, two sub-phases happen:

- **phase-2.1**: either the frequency is in saturation but not the voltage (case c)) or the voltage is in saturation but not the frequency (case d)),
- **phase-2.2**: both the frequency and the voltage are not in saturation (case e)).

Once again, the phase-2.1 does not influence the phase-2.2. As the possible two cases inside the phase-2.1 have a 1st order linear behaviors, the displacement from the initial position to current position has not yet an overshoot. On the other hand, when the voltage becomes

smaller than U_0 (case b)), the stick-slip microsystem stops independently to the precedent phases. Thus, the stability analysis of the microsystem may be done only with the phase-2.2 (case e)). For that, we use the direct method of Lyapunov.

A dynamic system $\frac{dx}{dt} = f(x, e, t)$, where e is the input vector, is Lyapunov stable if a Lyapunov function $V(x)$ exists such as:

$$V(x = 0) = 0 \quad (17)$$

$$V(x) > 0 \quad \forall \quad x \neq 0 \quad (18)$$

$$\frac{dV(x)}{dt} \leq 0 \quad \forall \quad x \neq 0 \quad (19)$$

From the (Eq. 15) and the conditions $x(t = 0) > 0$ and $x_c = 0$, we obtain:

$$\frac{dx}{dt} = -\alpha.K_f.x.(K_U.x - U_0) \quad (20)$$

We use the following quadratical functional $V(x)$:

$$V(x) = \gamma.x^2 \quad (21)$$

where γ is a positive constant. The conditions (Eq. 17) and (Eq. 18) are filled.

From (Eq. 20) and (Eq. 21), we have:

$$\frac{dV(x)}{dt} = -2.\gamma.\alpha.K_f.x^2.(K_U.x - U_0) \quad (22)$$

As $(K_U.x - U_0) > 0$, the condition (Eq. 19) is filled and all the trajectory is asymptotically (Lyapunov) stable. When $(K_U.x - U_0) < 0$, the microsystem stops, the stability is obvious and the static error is given.

V. EXPERIMENTS

The experimental setup is composed of a computer, an amplifier, the microsystem and a laser sensor (0.5nm resolution, 10m accuracy). The computer has no real-time operating system (Windows-XP) and we use LabView software for the implementation of the U/f controller.

The choice of K_U is a compromise. If K_U is very low, the static error is high. If K_U is very high, oscillations may occur (case a) when the refreshing time T_s and the response time T_r are not negligible. For all the experiments, the target point $x_c = 10mm$ and the initial point $x(0) = 0mm$.

The first experiment are done with high values of K_u and K_f . They have been chosen so that the phase-2 never happen. It is equivalent to the (case a). The Fig. 10-a gives the experimental and the simulation curves. Due to the fact that the computer has a non real-time operating system, the experimental results have oscillations (Fig. 10- in solid plot).

Then, we use a low K_U and a high K_f . The frequency stays in saturation while the voltage becomes non saturated when $x_c - x$ is inferior to a given value x_{US} (Fig. 10-b) such as $x_{US} = U_s/K_U$. In that case, the behavior is equivalent to (Eq. 11) of the case c), ie. a voltage proportional control. As shown in the figure, there is a static error. Its value is equal to $\varepsilon_{stat} = U_0/K_U$.

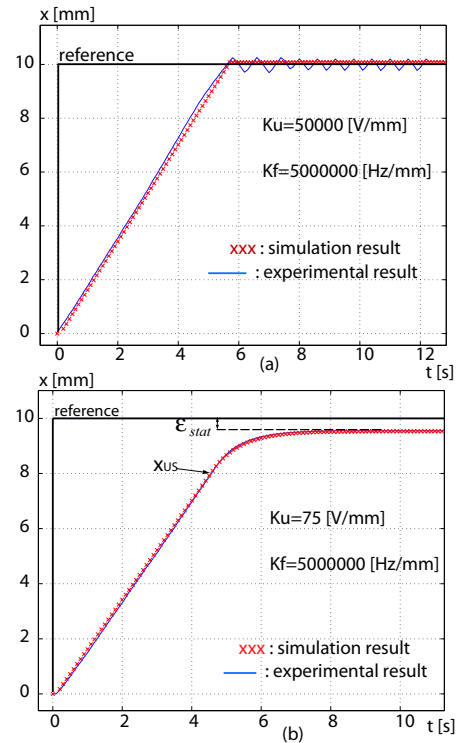


Fig. 10. a: high values of K_U and K_f : (case a). b: low K_U and high K_f .

After that, we apply a high K_U but a low K_f (Fig. 11-a). The leaving saturation speed is obtained at $(x_c - x) = x_{fs} = f_s/K_f$. From this point, the closed loop system has the frequently proportional controller behavior and there is no static error (case d)).

Finally, we test moderated values of K_U and K_f (Fig. 11-b). First, the frequency leaves the saturation at $x_{fs} = f_s/K_f$ while the voltage stays saturated. When $x_{US} = U_s/K_U$ is reached, the voltage leaves the saturation. According to the values of K_U and K_f , the inverse circumstance can happen. The static error is given by $\varepsilon_{stat} = U_0/K_U$.

VI. DISCUSSION

The U/f proportional controller encompasses some classical controllers: the sign controller (see case a), the classical proportional controller (see case c) and the frequency proportional controller (see case d). On the other hand, in comparison with the classical algorithm of (Eq. 1) and with the frequential proportional controller, the U/f proportional controller seems to have a high resolution. The resolution obtained with the two formers is one step (respectively $n \times step$) while the one obtained with the U/f controller is better than one step, within the limits of the sensor accuracy. In fact, the diminution of the applied voltage $U = K_U.\varepsilon$ reduces the value of a step. In addition, the diminution of the frequency $f = K_f.\varepsilon$ reduces the number of the steps and then the vibrations.

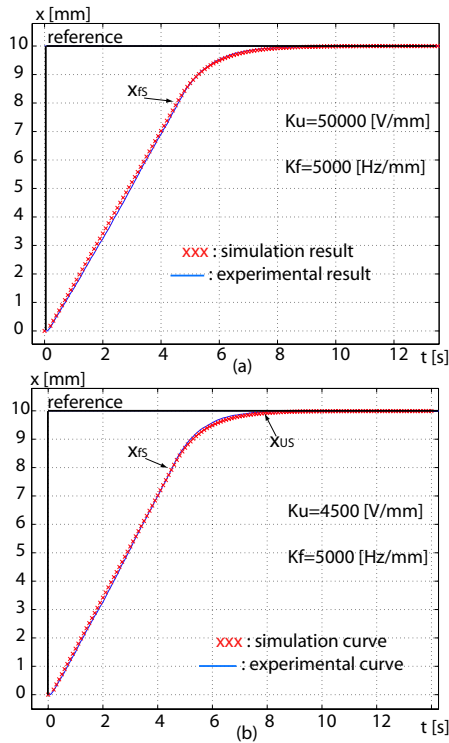


Fig. 11. a: high K_U and low K_f . b: decent values of K_U and K_f .

A test has been performed with an interferometer sensor (resolution = $1.24nm$) to compare the static precision obtained with the algorithm in (Eq. 1) and the U/f proportional controller. The setup used is composed of materials with high values of T_s and T_r : the interferometer datagate and a LabView software under Windows-XP. Thus, we use a low frequency ($1Hz$) for the classical controller in order to avoid oscillations.

Fig. 12 shows the results with a setpoint (reference) of $10m$. The zoom (Fig. 12-b) indicates that the static error (accuracy) is about $130nm$. As we can see, the resolution before the stop is the half value of a step instead of a step because the applied voltage is a peak-to-peak signal ($\pm 150V$), then when stopping it, the half only is cut out ($+150V \rightarrow 0V$).

Fig. 13 gives the results obtained with the U/f controller when applying a setpoint of $1mm$. The zoom (Fig. 13-b) indicates that the frequency and the step amplitude become increasingly small. The medium static error also becomes increasingly small. However, the flashback Δ_{back} becomes increasingly important. That is due to the diminution of the amplitude U so that there will not be enough torque to move the microsystem during the slip phase. The proposed method appears to converge to the reference position much faster than the classical controller. That is due to the low frequency used for this latter. Increasing the frequency increases the speed of the classical controller but oscillations may appear.

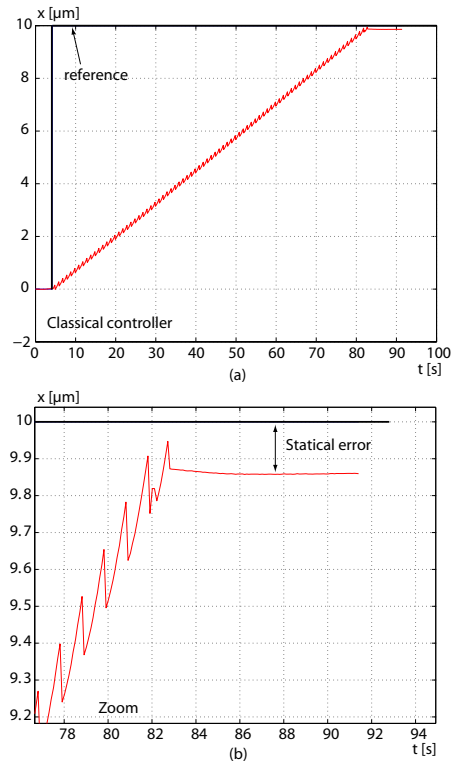


Fig. 12. Classical controller using an interferometer sensor. a: high stroke motion. b: zoom of the final position.

VII. CONCLUSION

A new controller type for high stroke displacement of stick-slip microsystems was proposed: voltage/frequency proportional controller. Here, the frequency f and an amplitude U of a sawtooth signal are proportional to the error. To analyze the performances given by such controller, we have first modeled the high stroke displacement of the microsystem. Then, we have analysed the stability according to the value of the proportional gains K_U and K_f . Finally, we have presented experiments and simulations of different cases. The U/f proportional control is a globalization of existing some existing controllers, the sign controller, the classical proportional controller and the frequency proportional controller, and it gives a better resolution relative to existing controllers for stick-slip microsystems.

ACKNOWLEDGMENT

Particular thanks to Dr Jean-Marc Breguet and his team from the LSRO - EPFL (Lausanne Switzerland) for accepting us to use their interferometer sensor. This work is partially supported by the European Project EUPASS (<http://www.eupass.org/>)

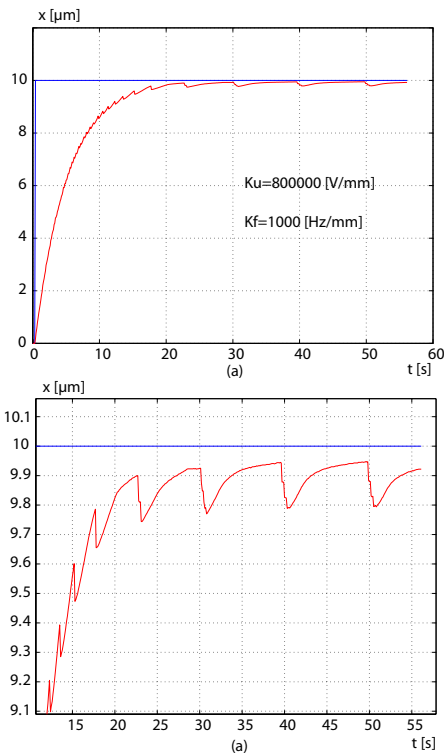


Fig. 13. U/f controller using an interferometer sensor. a: high stroke motion. b: zoom of the final position.

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