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**EXAFS study of lead-free relaxor ferroelectric BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> at the Zr K edge**C. Laulhé,<sup>1</sup> F. Hippert,<sup>1</sup> J. Kreisel,<sup>1,\*</sup> M. Maglione,<sup>2</sup> A. Simon,<sup>2</sup> J. L. Hazemann,<sup>3</sup> and V. Nassif<sup>4</sup><sup>1</sup>*Laboratoire des Matériaux et du Génie Physique (CNRS), Bâtiment INPG-MINATEC, 3 parvis Louis Néel, B.P. 257, F-38016 Grenoble cedex 1, France*<sup>2</sup>*Institut de Chimie de la Matière Condensée de Bordeaux (CNRS), 87 Avenue A. Schweitzer, F-33608 Pessac, France*<sup>3</sup>*Laboratoire de Cristallographie (CNRS), 25 rue des Martyrs, BP 166, F-38042 Grenoble cedex 9, France*<sup>4</sup>*CEA Grenoble, DRFMC/SP2M/NRS, 17 rue des Martyrs, F-38054 Grenoble cedex 9, France*

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Extended x-ray absorption fine structure experiments at the Zr *K* edge were carried out on perovskite relaxor ferroelectrics BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> (BTZ) ( $x=0.25, 0.30, 0.35$ ), and on BaZrO<sub>3</sub> for comparison. Structural information up to 4.5 Å around the Zr atoms is obtained, revealing that the local structure differs notably from the average  $Pm\bar{3}m$  cubic structure deduced from the x-ray diffraction. In particular, our results show that the distance between Zr atoms and their first oxygen neighbors is independent of the Zr substitution rate  $x$  and equal to that measured in BaZrO<sub>3</sub>, while the x-ray cubic cell parameter increases linearly with  $x$ . Furthermore, we show that the Zr atoms tend to segregate in Zr-rich regions. We propose that the relaxor behavior in BTZ could be influenced by the random elastic fields generated by this particular chemical arrangement.

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**I. INTRODUCTION**

The perovskite-type barium zirconate titanate, BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> (BTZ), has attracted considerable attention as a possible lead-free ferroelectric material to replace the current industry standard lead-based ferroelectrics.<sup>1-6</sup> The particularity of BTZ is the continuous change of its properties from a ferroelectric behavior at low Zr substitution rates to a relaxor ferroelectric (relaxor) behavior at higher substitution rates ( $0.25 \leq x \leq 0.5$ ).<sup>7</sup> The low substitution regime has been mainly studied for its interest in lead-free ferroelectric memories.<sup>4,5</sup> However, due to the recent report of outstanding electromechanical properties in relaxor-based ferroelectric solid solutions,<sup>8,9</sup> it is rather the relaxor regime of BTZ which currently attracts a large research effort.

Relaxors are characterized by a broad and frequency-dependent dielectric anomaly as a function of temperature, instead of a sharp and frequency-independent divergence as in classical ferroelectrics.<sup>10-14</sup> In a relaxor such as PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> (PMN), the anomaly surprisingly occurs in a cubic average structure which remains centrosymmetric (nonpolar) at all temperatures. It is generally admitted that the peculiar properties of relaxors are related to the presence of nanoscaled polar regions, due to different cation shifts in different parts of the structure.

Two ingredients are often cited for a relaxor ferroelectric: (i) the presence of Pb<sup>2+</sup> or Bi<sup>3+</sup> cations (showing large displacements due to their lone pair) and/or (ii) an aliovalent cationic disorder (generating random local electric fields<sup>15</sup> that break long-range polar correlations). Both are present in the extensively studied model relaxor PMN (e.g., Refs. 16-22). On the other hand, BTZ relaxors present a homovalent Zr<sup>4+</sup>/Ti<sup>4+</sup> substitution. It has been proposed that the difference in size of Zr<sup>4+</sup> and Ti<sup>4+</sup> cations ( $r_{Zr^{4+}}/r_{Ti^{4+}}=1.18$ ) in BTZ induces random elastic fields.<sup>23</sup> Such fields could affect the displacement of the ferroelectrically active Ti<sup>4+</sup> ions in their oxygen octahedra; yet it is not known how, and on which scale such random elastic fields build up. The

BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> solid solution thus opens an interesting route towards the comprehension of the relaxor behavior, and presents a fundamental interest.<sup>7,24-27</sup> Furthermore, it is intriguing that PbZr<sub>1-x</sub>Ti<sub>x</sub>O<sub>3</sub> (PZT) shows no relaxation<sup>28</sup> while BTZ does.

The average crystal structure of the BTZ relaxors ( $0.25 \leq x \leq 0.5$ ) is cubic (space group  $Pm\bar{3}m$ ) at any temperature.<sup>26</sup> Local distortions away from the ideal cubic structure expected from the observation of the relaxation behavior are evidenced by the observation of a first-order Raman scattering,<sup>24,25</sup> which is forbidden in a perfect primitive cubic structure. However, the latter technique does not reveal the nature of these distortions. The aim of the present study is to determine the local structure and chemical order in BTZ relaxors. For this purpose, we used EXAFS (extended x-ray absorption fine structure) spectroscopy, which is a structural and chemical local probe. This technique has been proven to be a powerful tool in analyzing the local distortions in ferroelectric perovskites (e.g., Refs. 29-33). On the other hand, only a few EXAFS studies have been reported for relaxors.<sup>34-39</sup>

In the case of BTZ, the effect of the substitution of Ti by Zr in the ferroelectric BaTiO<sub>3</sub> can be easily studied by EXAFS at the Zr *K* edge. Unfortunately, due to the overlap of the Ti *K* edge with the Ba *L<sub>III</sub>* edge, it is very difficult to directly investigate the Ti environment in BTZ, as in BaTiO<sub>3</sub>.<sup>29,40</sup> In the following, we report an EXAFS study of three BTZ relaxors ( $x=0.25, 0.30, \text{ and } 0.35$ ) at the Zr *K* edge. The local structure parameters were determined up to distances of 4.5 Å from the Zr atoms, giving information on their local environment up to their fourth neighbors. Hence, the Zr/Ti repartition could be probed, as well as the distortions induced by the presence of Zr atoms. In order to have a proper reference for the understanding of the local Zr environment, we also studied BaZrO<sub>3</sub> under the same experimental conditions.

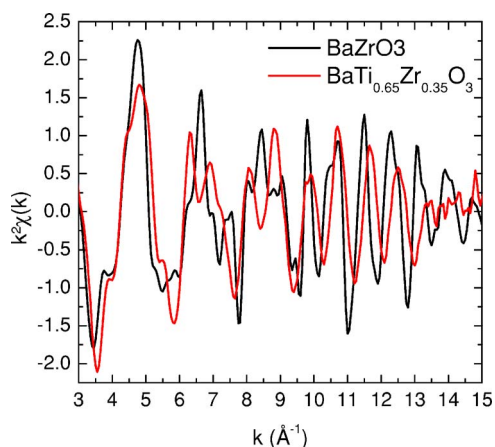


FIG. 1. (Color online)  $k^2$ -weighted normalized EXAFS signals for BaZrO<sub>3</sub> and BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub> at 300 K.

## II. EXPERIMENTAL METHODS

### A. Samples and experiments

BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> ( $x=0.25, 0.30, 0.35$ , and 1) powders were synthesized by solid state reactions, starting from the appropriate amounts of BaCO<sub>3</sub>, TiO<sub>2</sub>, and ZrO<sub>2</sub> powders and following the method described in Ref. 7. They were then characterized by x-ray diffraction at 300 K. All the powders were found to be single phases within the accuracy of the experiment. The cubic cell parameters are 4.054(1), 4.061(1), 4.072(1), and 4.192(1) Å for  $x$  values of 0.25, 0.30, 0.35, and 1, respectively.

EXAFS experiments at the Zr  $K$  edge (17.998 keV) were carried out on the FAME beamline BM30B at the European Synchrotron Radiation Facility (ESRF). The x-ray absorption coefficient  $\mu$  was measured in the transmission mode as a function of the incident photon energy  $E$  in the range [17.8–19.5 keV], using a Si(220) single crystal monochromator. The samples consisted of pellets made of BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> powders (with a grain size of about 1  $\mu$ m) mixed with very low-absorbing boron nitride. The effective thickness  $e$  of each sample was chosen in such a way that the product  $\mu e$  increases approximately by 1 through the Zr  $K$  edge. EXAFS data were collected at room temperature for all samples, as well as at 11 K for BaZrO<sub>3</sub> and at 11, 90, and 150 K for BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub>.

### B. EXAFS data treatment

The scattering of the photoelectron by the neighbors of the central absorbing atom introduces oscillations in the energy dependence of the absorption coefficient  $\mu(E)$  after the energy edge. The normalized experimental EXAFS signal is given by  $\chi(k)=[\mu(k)-\mu_0(k)]/\Delta\mu_0(k=0)$ .  $\mu_0$  is the smooth, atomiclike, absorption background,  $\Delta\mu_0(k=0)$  is the absorption edge jump, and  $k$  is the photoelectron wave number, given by  $k=\sqrt{2m_e(E-E_0)}/\hbar$  with  $m_e$  the electron mass and  $E_0$  the edge energy. In the present work,  $\chi(k)$  was extracted from the measured absorption coefficient  $\mu(E)$ , by using the AUTOBK program.<sup>41</sup>  $E_0$  was taken at the first maximum of the derivative of  $\mu(E)$  at the Zr  $K$  edge. Two representative

examples of normalized  $k^2$ -weighted  $\chi(k)$  spectra are shown in Fig. 1.

The theoretical EXAFS signal  $\chi(k)$  is expressed as a sum of contributions from different paths, each path  $i$  corresponding to a given scattering process of the photoelectron:

$$\chi(k) = -S_0^2 \sum_i \frac{N_i A_i(k)}{k R_i^2} e^{-2k^2 \sigma_i^2} e^{-2R_i/\lambda(k)} \times \sin[2kR_i + 2\delta_c(k) + \phi_i(k)], \quad (1)$$

where  $N_i$  is the degeneracy of path  $i$ ,  $R_i$  its half-length, and  $A_i(k)$  its effective scattering amplitude. The Debye-Waller (DW) factor  $\sigma_i^2$  is the standard deviation of the  $R_i$  distance distribution, assumed to be Gaussian. The DW factor takes into account both the thermal disorder and a possible small structural disorder.  $\delta_c(k)$  and  $\phi_i(k)$  are phase shifts associated with the electron propagating into and out the potentials of the absorbing site and scattering sites, respectively. The other parameters are the photoelectron mean-free path  $\lambda(k)$  and an overall amplitude factor  $S_0^2$ , close to 1, which accounts for many-electron effects in the excited central atom. Note that Eq. (1) includes both single (back-)scattering (SS) and multiple scattering (MS) processes.<sup>42</sup> For a SS path,  $N_i$  is simply the number of chemically identical atoms situated at a given distance  $R_i$  from the central atom.

The analysis of EXAFS signals at the Zr  $K$  edge was performed in  $R$  space after a Fourier transform (FT) of the  $k^2$ -weighted  $\chi(k)$  in the  $k$  range [3.2–14.6 Å<sup>-1</sup>], using a Hanning weight function. The calculated FTs were fitted to the experimental ones using the FEFFIT program.<sup>43</sup> The electronic parameters  $A_i(k)$ ,  $\phi_i(k)$ ,  $\delta_c(k)$ , and  $\lambda(k)$  were calculated for both SS and MS paths with the FEFF8.00 code.<sup>44</sup> The structural parameters  $R_i$ ,  $\sigma_i^2$ , as well as  $N_i$  if unknown, were extracted from the fit as will be described in details in Secs. III B–III D. As customary, an additional parameter  $\Delta E_0$  was introduced to account for the small difference between the experimental edge energy  $E_0$  and its calculated value using the FEFF code. The parameter  $S_0^2$  was also refined, the experimental value usually differing from the theoretical one.

## III. RESULTS

### A. General trends

Examples of the Fourier transforms of the experimental  $k^2$ -weighted  $\chi(k)$  spectra are shown in Fig. 2. For all studied samples and at all temperatures, the FTs can be readily separated into two contributions, characteristic of the perovskite structure. The first neighbors of a Zr atom are six oxygen atoms (denoted hereafter as O1), which form a regular octahedron in the perfect  $Pm\bar{3}m$  perovskite structure. The first contribution to the FT, at  $R$  values lower than 2.5 Å, only includes a SS process by one of the O1 atoms. The second contribution, in the  $R$  range [2.5–4.5 Å], results both from SS processes where the photoelectron is backscattered by either the second (Ba), third (Zr or Ti), or fourth oxygen (O2) neighbors of the Zr atom, and from several MS processes. Note that due to the  $k$  dependence of the phase shifts  $\phi_i(k)$  and  $\delta_c(k)$ , the maxima of the FT modulus occur at distances different from the real ones.

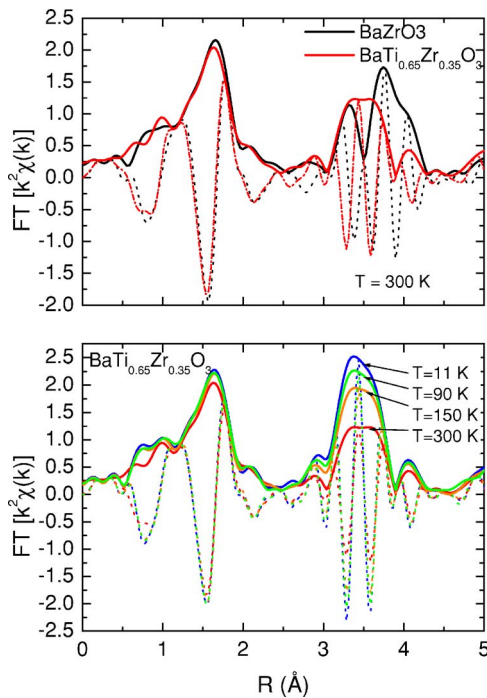


FIG. 2. (Color online) Selected FTs of the  $k^2$ -weighted EXAFS signals:  $\text{BaZrO}_3$  and  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  at 300 K (top), and thermal evolution in  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  (bottom). The imaginary part and the modulus of the FTs are plotted as dashed and solid lines, respectively.

Surprisingly, the first peaks of the FTs are nearly identical at 300 K in all relaxor samples *and* in  $\text{BaZrO}_3$  (see Figs. 2 and 3). The latter suggests very close first neighbor's environment of the Zr atoms, whatever the Zr substitution rate. On the other hand, the FTs of  $\text{BaZrO}_3$  and BTZ relaxors differ significantly for  $R$  values larger than  $2.5 \text{ \AA}$ .

The shape of the FTs suggests an analysis in two steps. Fits of the measured FTs are first performed in the  $R$  range related to the Zr first oxygen neighbors (Sec. III B). In a second step, the fitted  $R$  range is extended up to  $4.5 \text{ \AA}$ , in order to take into account the further neighbor's contributions (Sec. III C and III D). In BTZ relaxors, one has to take into account both the Zr/Ti substitution and the strong contribution of several MS paths in this  $R$  range, which makes the EXAFS analysis complicated. In order to get reference parameters for the analysis of BTZ relaxors, the FT of  $\text{BaZrO}_3$  is first fitted (Sec. III C). From previous EXAFS studies,<sup>45–47</sup> the local structure of  $\text{BaZrO}_3$  can be considered as a perfect cubic perovskite structure,<sup>48</sup> identical to the average one deduced from x-ray diffraction (space group  $Pm\bar{3}m$ ).<sup>49,50</sup>

### B. Analysis of the first neighbor contribution

We already noted that the backscattering processes between Zr atoms and their first oxygen neighbors (O1) give rise to very similar contributions to the FTs of the EXAFS signals below  $2.5 \text{ \AA}$ , for all samples and at all temperatures (Figs. 2 and 3). From the known structure of  $\text{BaZrO}_3$ , it is then reasonable to assume, as a starting point for the analysis

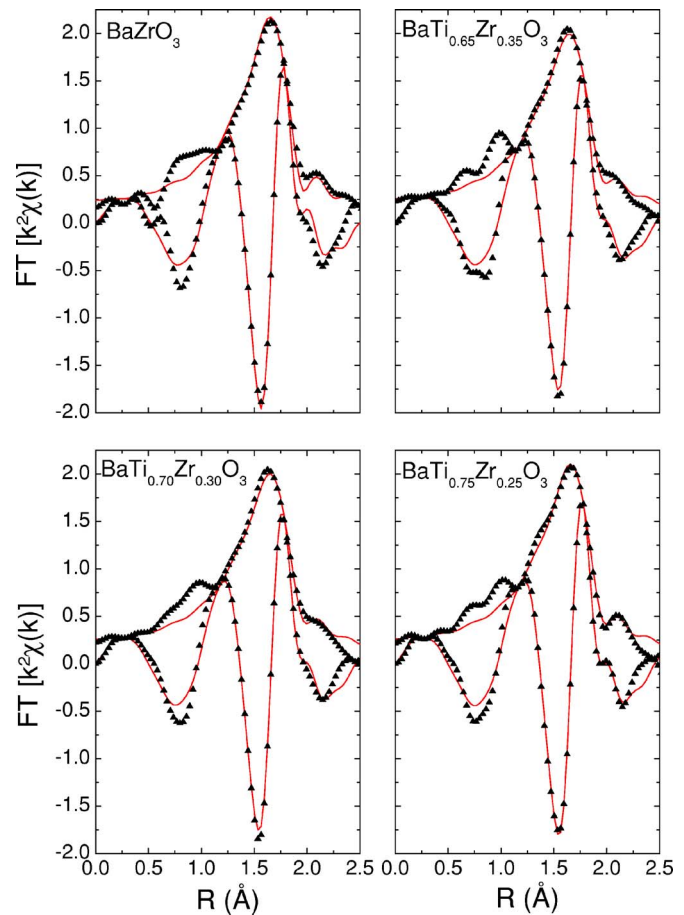


FIG. 3. (Color online) Modulus and imaginary part of the FT of  $k^2\chi(k)$  at 300 K. The dots represent measured data and the solid lines their best fit, obtained with the parameters values given in Table I. Measured data for  $R < 1 \text{ \AA}$  are affected by the background subtraction procedure and were excluded from the analysis.

of BTZ relaxors, that the six O1 atoms are located at the same distance from the absorbing Zr atom. Within this hypothesis, only one SS path (denoted hereafter as path 1) contributes in Eq. (1) for the considered  $R$  range. The fitted parameters are, for each sample, the Zr-O1 distance  $R_1$ , the associated DW factor  $\sigma_1^2$ , and  $\Delta E_0$ . The number of O1 neighbors,  $N_1$ , is fixed to 6. The analysis of the EXAFS data for  $\text{BaZrO}_3$  at 11 and 300 K allows us to determine a  $S_0^2$  value equal to  $1 \pm 0.07$ . This parameter was then fixed to 1 for all the further analysis. The EXAFS oscillations were refined in the  $R$  range  $[1.14–2.33 \text{ \AA}]$ : the data for  $R$  lower than  $1 \text{ \AA}$  are affected by the background subtraction procedure<sup>41</sup> and had to be excluded from the fit. Fits of good quality could be obtained, with reliability factors less than 1%, for all samples at all temperatures (Fig. 3 and Table I).

In  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  and  $\text{BaZrO}_3$  samples, no significant temperature dependence of the Zr-O1 distance is detected, within the experimental accuracy of the EXAFS technique. More surprisingly, the Zr-O1 distance hardly varies with the Zr substitution rate  $x$ , and keeps values very close to that found in  $\text{BaZrO}_3$ .

The refined values of the  $\sigma_1^2$  DW factors in  $\text{BaZrO}_3$  at 11 and 300 K are in good agreement with those reported in Ref.



TABLE I. Structural parameters deduced from the EXAFS analysis in the  $R$  range [1.14–2.33 Å], for BaZrO<sub>3</sub> and BTZ relaxors.  $R_1$  is the length of the bond between an absorbing Zr atom and its first oxygen neighbor, and  $\sigma_1^2$  the associated Debye-Waller factor.  $\chi_v^2$  and RF are the reduced chi-squared and the reliability factor of the fit. The  $\chi_v^2$  were calculated with a root mean squared value of random fluctuations of  $0.85 \times 10^{-3}$  for all samples, except for BaZrO<sub>3</sub> at 11 K:  $1.92 \times 10^{-3}$ . Three parameters were refined on 10.02 independent data points. The uncertainties are of the order of  $\pm 0.01$  Å and  $\pm 0.0004$  Å<sup>2</sup> for  $R_1$  and  $\sigma_1^2$ , respectively. The energy shift  $\Delta E_0$  was found equal to  $1.4 \pm 0.8$  eV for all fits.

Sample	$T$ (K)	$R_1$ (Å)	$\sigma_1^2$ (Å <sup>2</sup> )	$\chi_v^2$	RF factor (%)
BaZrO <sub>3</sub>	300	2.11	0.0039	12	0.61
	11	2.11	0.0029	3	0.62
BaTi <sub>0.65</sub> Zr <sub>0.35</sub> O <sub>3</sub>	300	2.10	0.0048	8	0.58
	150	2.10	0.0038	8	0.46
	90	2.10	0.0038	16	0.96
	11	2.10	0.0035	9	0.48
BaTi <sub>0.70</sub> Zr <sub>0.30</sub> O <sub>3</sub>	300	2.10	0.0048	8	0.55
BaTi <sub>0.75</sub> Zr <sub>0.25</sub> O <sub>3</sub>	300	2.10	0.0043	7	0.47

47. In BTZ relaxors, systematically higher  $\sigma_1^2$  values are obtained. From the definition of the DW factor, this increase depicts either a stronger static disorder, or enhanced vibration amplitudes (associated with a decrease of the Zr-O1 bond stiffness). As a matter of fact, the static and dynamic contributions can be separated, by analyzing the thermal evolution of the measured DW factor. In the absence of a static disorder, the DW factor only accounts for thermal vibrations and can be written, in the Einstein model, as

$$\sigma_{i, therm}^2(T) = \frac{\hbar^2}{2k_B M_R \theta_E} \coth\left(\frac{\theta_E}{2T}\right), \quad (2)$$

where  $k_B$  is the Boltzmann constant and  $M_R$  the reduced mass of all atoms involved in the scattering path. The Einstein temperature  $\theta_E$ , characterizing the bond strength, increases with the bond stiffness. Given our hypothesis of a perfect  $Pm\bar{3}m$  perovskite local structure in BaZrO<sub>3</sub>, the two  $\sigma_1^2$  values measured at 11 and 300 K in this sample were fitted to Eq. (2). An Einstein temperature of  $606 \pm 14$  K was then obtained for the Zr-O1 bond. In BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub>, the thermal evolution of  $\sigma_1^2$  is consistent with the same  $\theta_E$  value, provided that a constant  $\Delta\sigma_1^2 = +0.0007$  Å<sup>2</sup> is added to Eq. (2) (Fig. 4). This result gives evidence for the existence of a static distribution of the Zr-O1 distances in BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub>, which is temperature-independent within the experimental accuracy. The full width at half maximum of a Gaussian distribution of distances would be equal to  $2\sqrt{2} \ln 2 \Delta\sigma_1^2 = 0.06$  Å. This small value justifies *a posteriori* the use of only one SS path in Eq. (1), the DW factor  $\sigma_1^2$  taking into account the small disorder that cannot be resolved in  $R$  space.

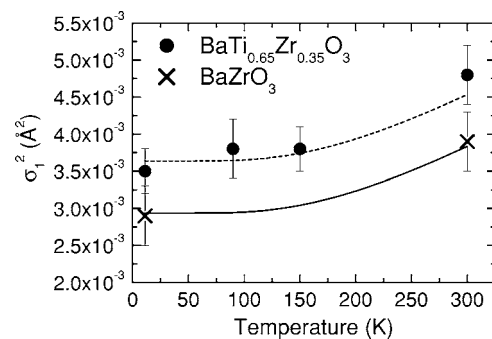


FIG. 4. Thermal evolution of the measured DW factor for the Zr-O1 bond (symbols). The solid line represents Eq. (2) with  $\theta_E = 606$  K. The dashed line corresponds to the same function shifted by  $0.0007$  Å<sup>2</sup>.

The mean square deviation of the  $R_i$  distance linked to a static disorder,  $\Delta\sigma_i^2$ , is intended to describe a Gaussian static distribution of distances in Eq. (1), with  $\sigma_i^2 = \sigma_{i, therm}^2(T) + \Delta\sigma_i^2$ . However, a measured nonzero value of  $\Delta\sigma_i^2$  can describe other distance distributions (discrete or continuous), provided their width remains small. In the present case, the distribution of the Zr-O1 distances could be due to a distortion of the ZrO<sub>6</sub> units, coming from the Zr/Ti chemical disorder, and/or to a displacement of Zr atoms in their octahedral cages. To evaluate the magnitude of such a displacement, we calculated the FT of the EXAFS signals for Zr atoms in a perfect octahedron, weakly displaced either along the [100], [110], or [111] cubic axis. We then performed fits on the calculated signals in the same conditions as described above for the measured signals. From these simulations, we conclude that the refined DW factors presented in Table I for BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub> could correspond to a Zr displacement of 0.07 Å, in any of the three directions cited above.

In conclusion, the length and strength of the bond between a Zr atom and its first oxygen neighbor are found to be independent of the Zr substitution rate in BaTi<sub>1-x</sub>Zr<sub>x</sub>O<sub>3</sub> samples. Only a small temperature-independent distribution of the Zr-O1 distances is detected in BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub>, in opposition to the single distance in the regular octahedron present in BaZrO<sub>3</sub>. These fluctuations of the Zr-O1 distance can be due to Zr displacements in their octahedra, but can also result from distortions of the ZrO<sub>6</sub> octahedra induced by the Zr/Ti chemical disorder. Note that a static distribution of Zr-O1 distances is also expected in the two other relaxor samples, BaTi<sub>0.70</sub>Zr<sub>0.30</sub>O<sub>3</sub> and BaTi<sub>0.75</sub>Zr<sub>0.25</sub>O<sub>3</sub>, from the  $\sigma_1^2$  values measured at 300 K and by analogy with the case of BaTi<sub>0.65</sub>Zr<sub>0.35</sub>O<sub>3</sub>.

### C. Analysis of the further neighbor contribution: BaZrO<sub>3</sub>

For  $R$  values up to 4.5 Å, the FT of the EXAFS signal involves scattering processes beyond the first oxygen neighbors. The amplitudes and phases of all the possible paths have been calculated by using the FEFF8.00 code, for an atomic cluster of 145 atoms representative of the BaZrO<sub>3</sub>  $Pm\bar{3}m$  perovskite structure. The scattering processes with

TABLE II. SS and MS paths used to analyze BaZrO<sub>3</sub> EXAFS data.  $N_i$  is the degeneracy of path  $i$ , and  $R_i$  its half-length, expressed as a function of  $R_1$  assuming an ideal perovskite structure. Zr<sub>c</sub> is the central absorbing Zr atom. The O1 and O1' atoms are located on opposite sides of the Zr<sub>c</sub> atom, between Zr<sub>c</sub> and one of its six Zr third neighbors.

Index	Scattering process	$N_i$	$R_i$	$\sigma_i^2$
1	Zr <sub>c</sub> →O1→Zr <sub>c</sub>	6	$R_1$	$\sigma_1^2$
2	Zr <sub>c</sub> →Ba→Zr <sub>c</sub>	8	$\sqrt{3}R_1$	$\sigma_2^2$
3	Zr <sub>c</sub> →Zr→Zr <sub>c</sub>	6	$2R_1$	$\sigma_3^2$
4	Zr <sub>c</sub> →O1'→O1→Zr <sub>c</sub>	6	$2R_1$	$\sigma_4^2$
5	Zr <sub>c</sub> →Zr→O1→Zr <sub>c</sub>	12	$2R_1$	$\sigma_3^2$
6	Zr <sub>c</sub> →O1'→Zr <sub>c</sub> →O1→Zr <sub>c</sub>	6	$2R_1$	$\sigma_4^2$
7	Zr <sub>c</sub> →O1→Zr <sub>c</sub> →O1→Zr <sub>c</sub>	6	$2R_1$	$2\sigma_1^2$
8	Zr <sub>c</sub> →O1→Zr→O1→Zr <sub>c</sub>	6	$2R_1$	$\sigma_3^2$
9	Zr <sub>c</sub> →O1→Ba→Zr <sub>c</sub>	48	$\frac{1+\sqrt{2}+\sqrt{3}}{2}R_1$	$\sigma_9^2$
10	Zr <sub>c</sub> →O2→Zr <sub>c</sub>	24	$\sqrt{5}R_1$	$\sigma_{10}^2$

relative weight lower than 2.5% have been neglected. The single backscattering processes on the second (Ba), third (Zr), and fourth (O2) neighbors of the Zr central atom must be considered, as well as several collinear MS paths and only two nonlinear MS paths. One of the two latter paths involves Ba atoms. The other one is a triple scattering path within the ZrO<sub>6</sub> octahedron, which corresponds to a  $R$  range between the two main peaks of the FTs. We verified that it does not affect the fit, and did not consider it further. The retained paths for the EXAFS analysis are listed in Table II. Note that the half-lengths of all the collinear MS paths are equal to the Zr-Zr distance. As a consequence, these MS paths contribute to the FT in the same  $R$  range as the single backscattering path by a Zr atom, which makes the analysis complex.

Assuming a perfect  $Pm\bar{3}m$  cubic structure, all  $N_i$  are known and the  $R_i$  parameters for the ten paths can be expressed as a function of  $R_1$ , the distance between the central absorbing Zr atom and O1 (see Table II). The number of  $\sigma_i^2$  parameters needed could be decreased using the expression of the DW factor:<sup>42</sup>

$$\sigma_i^2 = \frac{1}{4} \left\langle \left[ \sum_j (\vec{u}_{j+1} - \vec{u}_j) \cdot \vec{R}_{jj+1} \right]^2 \right\rangle, \quad (3)$$

where  $t$  is the time,  $j$  represents an atomic site of the scattering path  $i$ ,  $\vec{u}_j$  is the displacement vector of the  $j$  atom, and

TABLE III. Structural parameters deduced from the EXAFS analysis in the  $R$  range [1.14–4.52 Å], for BaZrO<sub>3</sub>. The parameters have already been defined in Tables I and II. Seven parameters were refined on 24.16 independent data points. The uncertainties are of the order of  $\pm 0.01$  Å for  $R_1$ ,  $\pm 0.0003$  Å<sup>2</sup> for  $\sigma_2^2$  and  $\sigma_3^2$ , and  $\pm 0.003$  Å<sup>2</sup> for  $\sigma_{10}^2$ .  $\Delta E_0$  was found equal to  $0.0 \pm 0.5$  eV for both fits.

	$R_1$ (Å)	$\sigma_2^2$ (Å <sup>2</sup> )	$\sigma_3^2$ (Å <sup>2</sup> )	$\sigma_{10}^2$ (Å <sup>2</sup> )	$\chi_v^2$	RF factor (%)
300 K	2.10	0.0072	0.0048	0.013	9	1.04
11 K	2.10	0.0026	0.0025	0.006	4	1.01

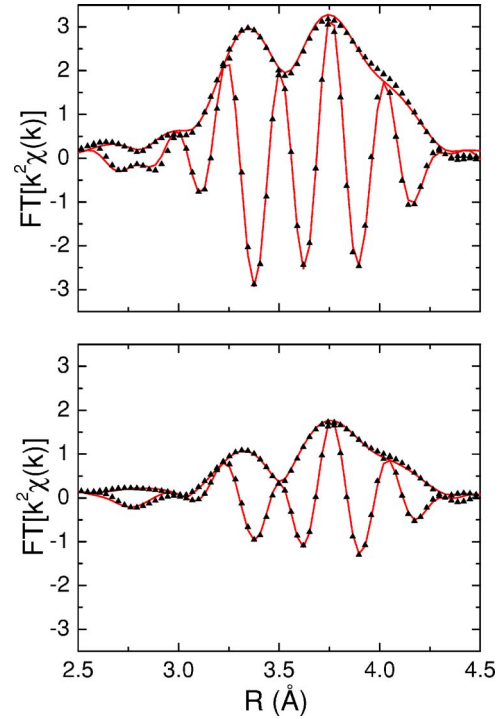


FIG. 5. (Color online) Modulus and imaginary part of the FT of  $k^2\chi(k)$  for BaZrO<sub>3</sub>, at 11 K (top) and 300 K (bottom). The dots represent measured data and the solid lines their best fit. The fit parameters are given in Table III.

$\vec{R}_{jj+1}$  is the directing unit vector between  $j$  and  $j+1$  atoms at equilibrium. The resulting relations between the  $\sigma_i^2$  parameters in BaZrO<sub>3</sub> are given in Table II. For the fit of the measured FT, in the  $R$  range [1.14–4.52 Å], seven parameters were then refined:  $\Delta E_0$ ,  $R_1$ ,  $\sigma_2^2$ ,  $\sigma_3^2$ ,  $\sigma_4^2$ ,  $\sigma_9^2$ , and  $\sigma_{10}^2$ . Although they have already been determined in Sec. III B,  $R_1$  and the strongly correlated parameter  $\Delta E_0$  were refined,<sup>51</sup> all distances up to 4.5 Å being functions of  $R_1$ . On the other hand, the  $S_0^2$  and  $\sigma_1^2$  parameters were fixed to the previously refined values. The obtained parameters at 11 and 300 K are presented in Table III. During the refinement process, the  $\sigma_4^2$  and  $\sigma_9^2$  values were found to have no influence on the RF factor. These two DW factors are related to paths 4, 6, and 9, which give rise to very large, and relatively weak contributions in  $R$  space. Consequently,  $\sigma_4^2$  and  $\sigma_9^2$  values do not affect significantly the amplitude and shape of these contributions and cannot be precisely determined, so that they are not given in Table III.

The calculated FTs are in very good agreement with the measured ones (Fig. 5). The DW factors for the Zr-Ba ( $\sigma_2^2$ ), Zr-Zr ( $\sigma_3^2$ ), and Zr-O<sub>2</sub> ( $\sigma_{10}^2$ ) bonds are consistent with those reported in Ref. 47. Their thermal evolution was fitted to Eq. (2), resulting in Einstein temperatures equal to  $194 \pm 8$  K,  $263 \pm 10$  K, and  $296 \pm 50$  K for the Zr-Ba, Zr-Zr, and Zr-O<sub>2</sub> bonds, respectively.

The analysis of the EXAFS oscillations in BaZrO<sub>3</sub> gives information on the relative contributions of the different paths to the FTs in the  $R$  range [2.5–4.5 Å], which will help us to analyze BTZ samples (see Fig. 6). Only the backscattering path on Ba atoms (path 2 in Table II) contributes in the  $R$  range [3.0–3.6 Å], which allows us a precise determination of the Zr-Ba distance and the associated DW factor. The contributions in the  $R$  range [3.6–4.2 Å] mainly arise from the MS linear paths that involve the third neighbor Zr atoms (paths 5 and 8 in Table II). The backscattering path on Zr atoms (path 3) also contributes in the same  $R$  range, but it is much less important. The remaining MS paths (paths 4, 6, 7, and 9 in Table II) correspond to weak contributions to the FTs, but it is necessary to take them into account in order to obtain good quality fits. The DW factors of paths 4, 6, and 9 were shown to have no influence on the fit. Finally, the backscattering path on O<sub>2</sub> atom (path 10) contributes over a very large  $R$  range [3–4.6 Å]. It is then compulsory to keep this path in the analysis, as it cannot be separated from the other contributions to the FTs.

#### D. Analysis of the further neighbor contribution: BTZ relaxors

In the following analysis, we shall introduce two different models of the local structure in BTZ relaxors. In a first step, we show that a model with aligned Zr, O1, and (Zr/Ti) atoms in the perovskite structure cannot account for the measured EXAFS signals. In a second step, we introduce a buckling angle for the Zr-O1-(Zr/Ti) bonds.

##### 1. Basic model for the BTZ analysis

The BaZrO<sub>3</sub> model (see Sec. III C) is used as a starting point to analyze BTZ samples. To take into account the Ti

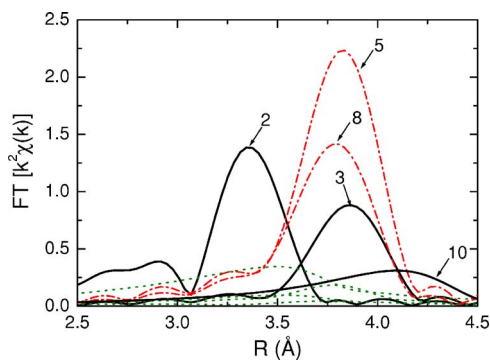


FIG. 6. (Color online) Modulus of the FT of the individual contributions to  $k^2\chi(k)$ , in BaZrO<sub>3</sub> at 300 K. SS paths, MS paths within Zr<sub>c</sub> octahedra, and MS paths outside Zr<sub>c</sub> octahedra are represented as solid, dash-dotted, and dotted lines, respectively. Numbers correspond to the path indexes of Table III.

third neighbors, we also calculated the amplitudes and phases of the scattering paths within a hypothetical cluster of BaTiO<sub>3</sub> in the  $Pm\bar{3}m$  cubic perovskite structure, with a single Zr impurity as the absorbing atom. For the paths that do not involve Ti atoms, the calculated amplitude and phase remain strictly identical to those calculated for the BaZrO<sub>3</sub> structure. Thus, we only consider three extra paths 3' (Zr<sub>c</sub> → Ti → Zr<sub>c</sub>), 5' (Zr<sub>c</sub> → Ti → O1 → Zr<sub>c</sub>), and 8' (Zr<sub>c</sub> → O1 → Ti → O1 → Zr<sub>c</sub>), in addition to those presented in Table II. The  $k$  dependence of these path amplitudes differs significantly from that of the corresponding paths 3, 5, and 8 of the BaZrO<sub>3</sub> model. Thus, the EXAFS technique allows the refinement of structural parameters for Zr and Ti atoms with limited correlations effects, despite similar Zr-Zr and Zr-Ti distances. A new parameter  $N_{Zr}$  has to be introduced, which is the average number of Zr third neighbors of the central atom Zr<sub>c</sub>. The degeneracy of paths 3, 5, and 8 is then multiplied by  $N_{Zr}/6$ , and that of paths 3', 5', and 8' by  $(6 - N_{Zr})/6$ . A unique  $\sigma_{3'}^2$  parameter is attached to the paths 3', 5' and 8', according to Eq. (3).

Zr atoms are larger than Ti ones, so that they likely cause local distortions in the BaTiO<sub>3</sub> matrix. This difference in size is taken into account by introducing independent Zr-O1, Zr-Ba, Zr-Ti, and Zr-O<sub>2</sub> distances. The O1 atoms lying between Zr<sub>c</sub> and (Zr/Ti) atoms in this first model, the Zr-Zr and Ti-O1 distances are defined using the expressions  $d_{Zr-Zr} = 2d_{Zr-O1}$  and  $d_{Ti-O1} = d_{Zr-Ti} - d_{Zr-O1}$ . The DW factors  $\sigma_4^2$  and  $\sigma_9^2$  were fixed to the same values as in BaZrO<sub>3</sub>, since they are not expected to affect the fit (see Sec. III C). Furthermore, the relations between the DW factors presented in Table II remain correct, so that only  $\sigma_2^2$ ,  $\sigma_3^2$ ,  $\sigma_{3'}^2$ , and  $\sigma_{10}^2$  DW factors were refined. The Zr-O1 distance ( $R_1$ ) and  $\sigma_1^2$ , as well as  $\Delta E_0$  and  $S_0^2$ , were fixed to the values refined in the  $R$  range [1.14–2.33 Å] (see Table I).

Within this model, the fitting procedure over the  $R$  range [1.14–4.52 Å] yields nonphysical values of the  $\sigma_3^2$  and  $\sigma_{3'}^2$  parameters (0.033 and  $-0.0008$ , respectively, at 11 K). In fact, the calculated contribution of paths linked to Zr atoms (paths 3, 5, and 8 in Table II) are completely damped (see top of Fig. 7). Only paths involving Ti atoms then contribute to the calculated signal, in the  $R$  range [3.4–3.9 Å]. Fixing  $\sigma_3^2$  to its value in BaZrO<sub>3</sub> made impossible a good agreement between calculated and experimental signals. In particular, the shift of the FT's imaginary part in the  $R$  range [3.6–3.9 Å] indicates an overestimated Zr-Zr distance (see bottom of Fig. 7). Hence, we deduce that  $d_{Zr-Zr}$  must be smaller than  $2d_{Zr-O1}$ .

##### 2. Determination of the buckled local structure in BTZ relaxors

With the hypothesis of aligned Zr<sub>c</sub>, O1, and Zr atoms being not valid in BTZ samples, a new model has to be built, where the O1 atoms are no longer aligned with Zr ones. In order to get all different possible configurations, one can introduce two mean buckling angles  $\Theta_{Zr}$  and  $\Theta_{Ti}$  defined as  $180^\circ - \widehat{ZrO1Zr}$  and  $180^\circ - \widehat{ZrO1Ti}$ , respectively. All the possible paths and their parameters were calculated in the preceding BaZrO<sub>3</sub> and BaTiO<sub>3</sub> clusters, moving the O1 atoms



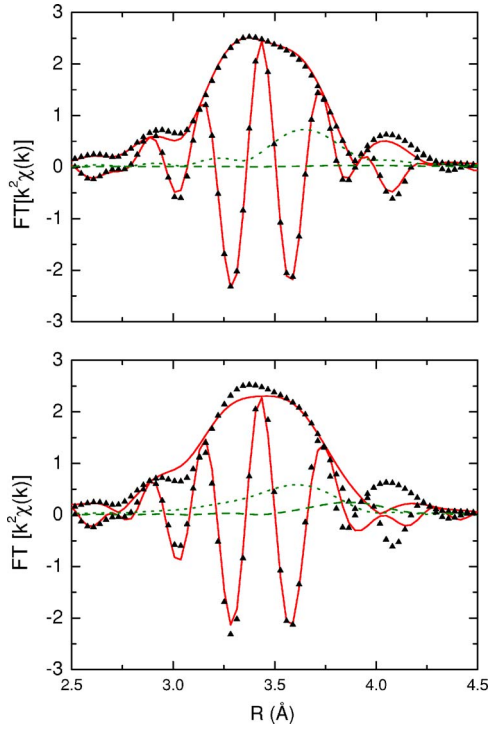


FIG. 7. (Color online) Modulus and imaginary part of the FTs of the observed (dots) and refined (solid line)  $k^2\chi(k)$  for  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  at 11 K. The modulus of the FT for paths 3 (dashed line) and 3' (dotted line), which describe the backscattering on Zr and Ti atoms, respectively, are also represented. The fits were obtained in the hypothesis of aligned Zr, O1, and (Zr/Ti) atoms. Top: the path 3 is completely damped by a nonphysical, huge  $\sigma_3^2$  DW factor. Bottom:  $\sigma_3^2$  is fixed to its value in  $\text{BaZrO}_3$ , i.e.,  $0.0020 \text{ \AA}^2$ . The calculated imaginary part is then shifted towards high  $R$  values in the  $R$  range [3.7–3.9  $\text{\AA}$ ], where the path 3 now contributes. The latter clearly indicates an overestimated  $d_{\text{Zr-Zr}}$  distance.

out of their collinear sites with varying values of the buckling angle  $\Theta$ . The only effect of the O1 atom displacements is the damping of the amplitudes of the MS paths in which these atoms play a focusing role, i.e., paths 5, 5', 8, and 8' (Table II). As an example, we show the evolution of the amplitude of path 5 as a function of  $\Theta$  on Fig. 8. This evolution can be expressed by expanding the scattering amplitude of the focusing paths about  $\Theta=0$ :

$$A(k, \Theta) \approx A(k, 0)[1 - b(k)\Theta^2]^n, \quad (4)$$

where  $n$  is the number of scattering processes by the off-centered focusing atom (O1).<sup>52</sup> For each of the paths 5, 5', 8, and 8', the coefficients  $b(k)$  were determined for various buckling angles and averaged. Equation (4) is found to be correct for the buckling angles' values below  $20^\circ$ .

The expressions for Zr-Zr and Ti-O1 distances are now given by  $d_{\text{Zr-Zr}} = 2d_{\text{Zr-O1}} \cos(\Theta_{\text{Zr}}/2)$ , and  $d_{\text{Ti-O1}} = \sqrt{d_{\text{Zr-Ti}}^2 - d_{\text{Zr-O1}}^2 \sin^2 \Theta_{\text{Ti}} - d_{\text{Zr-O1}} \cos \Theta_{\text{Ti}}}$ , from which the lengths of paths 1–8 can be easily derived. The path length  $R_0$  splits into several different values, due to the misalignment of the O1 oxygen atoms. This effect can be modeled by

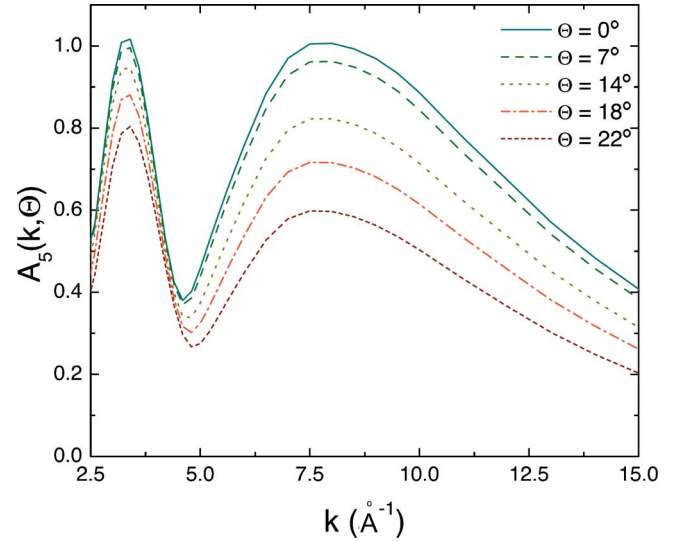


FIG. 8. (Color online) Evolution of the focusing path amplitudes with increasing values of the buckling angle  $\Theta$ : example of path 5.

an increase of the corresponding DW factor  $\sigma_9^2$ , but we already showed that this parameter does not affect the fit quality. Thus, we determined the mean distance  $R_9$  with the expression given in Table II, using the  $\sigma_9^2$  value of  $\text{BaZrO}_3$ . The length of path 10 splits as well, depending on the size and shape of the octahedra next to the central one  $\text{Zr}_c\text{O}_6$ . With this information being out of the scope of this study, we assigned to this path an average value of the Zr-O2 distances,  $R_{10}$ . In that case  $\sigma_{10}^2$  is expected to take into account both thermal and static disorders. In the absence of an adequate model for the O2 repartition, the values obtained for  $R_{10}$  and  $\sigma_{10}^2$  will not be interpreted. Concerning the DW factors, the linearity of paths 5, 5', 8, and 8' is broken by the off-centering of O1 atoms with respect to Zr-(Zr/Ti) bonds, so that the relations  $\sigma_5^2 = \sigma_8^2 = \sigma_3^2$  and  $\sigma_{5'}^2 = \sigma_{8'}^2 = \sigma_{3'}^2$  are no longer exact. However, we postulated their validity for the buckled paths, in order to limit the number of free parameters. The buckling angles  $\Theta_{\text{Zr}}$  and  $\Theta_{\text{Ti}}$  were determined separately, as preliminary fits using the same buckling angle for both  $\text{Zr}_c\text{-O1-Zr}$  and  $\text{Zr}_c\text{-O1-Ti}$  bonds did not yield a good agreement between experimental and calculated signals (see Fig. 9). Ten parameters were then refined:  $R_2, R_{3'}, R_{10}, N_{\text{Zr}}, \Theta_{\text{Zr}}, \Theta_{\text{Ti}}, \sigma_2^2, \sigma_3^2, \sigma_{3'}^2$ , and  $\sigma_{10}^2$ . The  $\sigma_3^2$  and  $\sigma_{3'}^2$  parameters were found to reach very low (nonphysical) values when not fixed. Like  $N_{\text{Zr}}, \Theta_{\text{Ti}}$ , and  $\Theta_{\text{Zr}}$ , these two DW factors determine the signal amplitude in the  $R$  range [3.4–3.9  $\text{\AA}$ ]. Strong correlation effects exist between these five parameters and various sets of their values give rise to similar, very good fits. To go further in the analysis, we assume that  $\sigma_3^2$  and  $\sigma_{3'}^2$  in BTZ relaxors are equal to  $\sigma_3^2$  in  $\text{BaZrO}_3$ , which is determined for all temperatures using Eq. (2) with the Einstein temperature of 263 K reported in Sec. III C. Values of refined parameters in this hypothesis are presented in Table IV and fits are shown in Fig. 10 for the three BTZ relaxors. The fits are not very sensitive to the variations of  $\Theta_{\text{Ti}}$  in the range  $[0^\circ\text{--}10^\circ]$ .  $\Theta_{\text{Ti}}$  values larger than  $10^\circ$  are excluded since they do not yield satisfactory agreements.



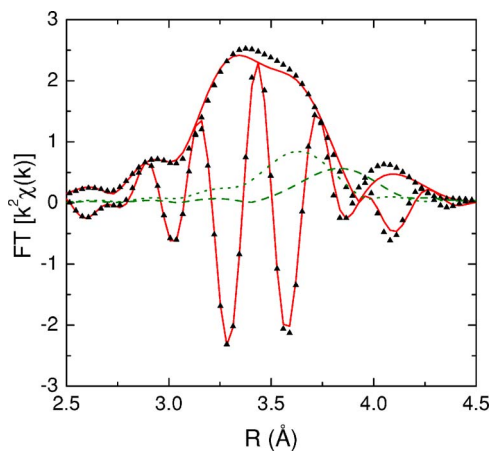


FIG. 9. (Color online) Modulus and imaginary part of the FTs of the observed (dots) and refined (solid line)  $k^2\chi(k)$  for  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  at 11 K. The modulus of the FT for paths 3 (dashed line) and 3' (dotted line), which describe the backscattering on Zr and Ti atoms, respectively, are also represented. We show the best fit obtained in the hypothesis of a single buckling angle for  $\text{Zr}_c\text{-O1-Zr}$  and  $\text{Zr}_c\text{-O1-Ti}$  bonds, for reasonable values of  $\sigma_3^2$  and  $\sigma_{3'}^2$  parameters. The missing amplitude in the  $R$ -range [3.3–3.7 Å], characteristic of the path 3', indicates an overestimated buckling angle for the Ti bonds.

Note that the Zr-Ba distance and the associated DW factor  $\sigma_2^2$  are accurately defined, the contribution of path 2 to the FTs being well separated from the others.

One needs to estimate the consequences of fixing  $\sigma_3^2$  and  $\sigma_{3'}^2$  for the analysis of BTZ relaxors. For this purpose, we performed several fits for various, not necessarily equal, values of  $\sigma_3^2$  and  $\sigma_{3'}^2$ , in a range of  $\pm 0.0010 \text{ \AA}^2$  around the  $\sigma_3^2$  value in  $\text{BaZrO}_3$ . The  $\Theta_{\text{Zr}}$ ,  $N_{\text{Zr}}$ , and  $R_{3'}$  values were found to vary by  $\pm 1.5^\circ$ ,  $\pm 0.2$ , and  $\pm 0.01 \text{ \AA}$ , respectively. Furthermore, the refined values of  $\Theta_{\text{Zr}}$  being at the limit of the validity range of Eq. (4), one expects an error of  $\pm 1^\circ$  on its determination. The uncertainties given in Table IV are those determined by the FEFFIT code, augmented by the preceding

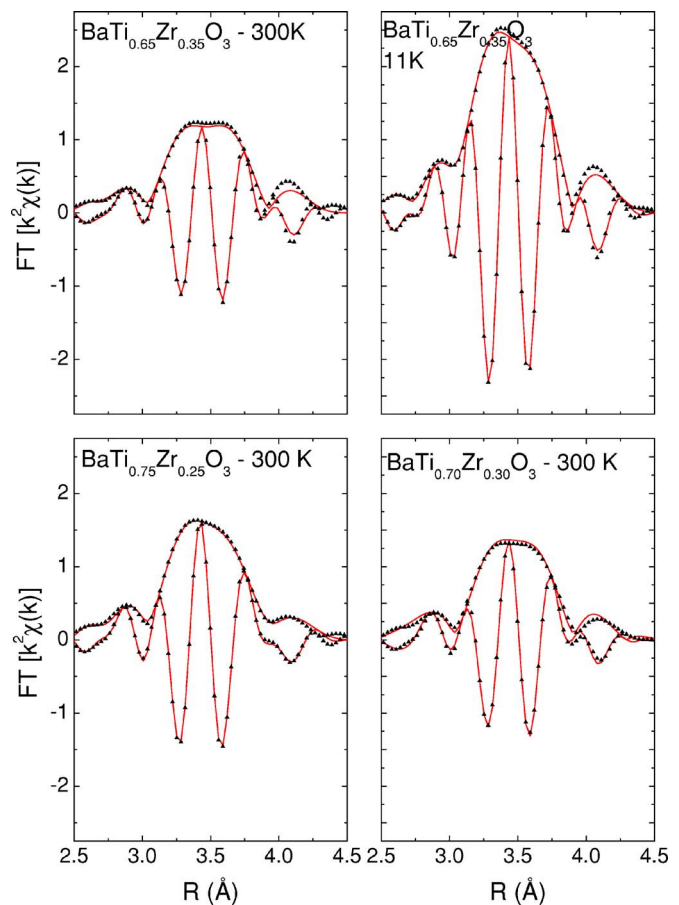


FIG. 10. (Color online) Modulus and imaginary part of the FT of  $k^2\chi(k)$  at either 11 or 300 K, for BTZ samples. The dots represent measured data and the solid lines their best fit, obtained with the parameters values given in Table IV.

amounts. Note that in the case of  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$ , the refined value of  $N_{\text{Zr}}$  is found to be independent of the temperature, as it should be. This confirms *a posteriori* that the hypothesis of an identical thermal evolution of  $\sigma_3^2$  and  $\sigma_{3'}^2$  in BTZ samples and  $\sigma_3^2$  in  $\text{BaZrO}_3$  is reasonable.

TABLE IV. Structural parameters deduced from the EXAFS analysis in the  $R$  range [1.14–4.52 Å], for BTZ relaxors. The path half-lengths are denoted  $R_i$ , and the associated DW factors  $\sigma_i^2$ .  $\Theta_{\text{Zr}}$  is the buckling angle of the Zr-O1-Zr bonds, defined as  $180^\circ - \widehat{\text{ZrO1Zr}}$ , and  $N_{\text{Zr}}$  the mean number of Zr third neighbors of the  $\text{Zr}_c$  atom.  $R_3$  is deduced from  $R_1$  (Table I) and  $\Theta_{\text{Zr}}$ . Ten parameters were refined on 24.16 independent data points. The uncertainties are of the order of  $\pm 0.006 \text{ \AA}$ ,  $\pm 0.0004 \text{ \AA}^2$ ,  $\pm 5^\circ$ ,  $\pm 0.04 \text{ \AA}$ ,  $\pm 0.02 \text{ \AA}$ ,  $\pm 0.04 \text{ \AA}$ ,  $\pm 0.005 \text{ \AA}^2$ , and  $\pm 1.0$  for  $R_2$ ,  $\sigma_2^2$ ,  $\Theta_{\text{Zr}}$ ,  $R_3$ ,  $R_{3'}$ ,  $R_{10}$ ,  $\sigma_{10}^2$ , and  $N_{\text{Zr}}$ , respectively.

Sample	$T$ (K)	$R_2$ (Å)	$\sigma_2^2$ (Å <sup>2</sup> )	$\Theta_{\text{Zr}}$ (°)	$R_3$ (Å)	$R_{3'}$ (Å)	$R_{10}$ (Å)	$\sigma_{10}^2$ (Å <sup>2</sup> )	$N_{\text{Zr}}$	$\chi_v^2$	RF factor (%)
$\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$	300	3.557	0.0070	18	4.15	4.07	4.61	0.018	3.4	8	1.09
	150	3.554	0.0048	17	4.15	4.06	4.60	0.014	3.4	10	0.81
	90	3.556	0.0041	19	4.15	4.07	4.60	0.012	3.4	11	0.80
	11	3.554	0.0037	18	4.14	4.06	4.60	0.012	3.3	8	0.51
$\text{BaTi}_{0.70}\text{Zr}_{0.30}\text{O}_3$	300	3.553	0.0068	19	4.16	4.07	4.60	0.019	3.1	7	0.84
$\text{BaTi}_{0.75}\text{Zr}_{0.25}\text{O}_3$	300	3.544	0.0060	20	4.16	4.07	4.60	0.015	2.7	76	0.49

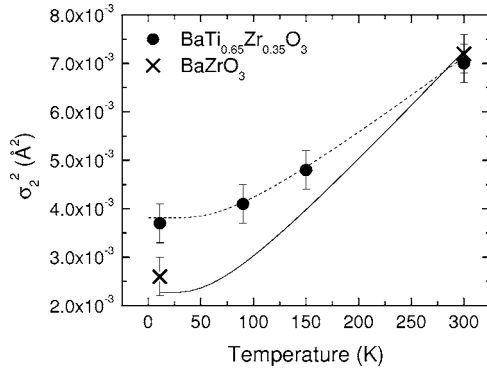


FIG. 11. Thermal evolution of the measured DW factor for the Zr-Ba bond (symbols). The solid line represents Eq. (2) with  $\theta_E = 194$  K. The dashed line corresponds to the same equation with  $\theta_E = 231$  K, and shifted by  $0.0019 \text{ \AA}^2$ .

### 3. Fit results

For all the relaxor samples investigated, the refined values of the buckling angle  $\Theta_{\text{Zr}}$  range from  $18^\circ$  to  $20^\circ$ . With  $\Theta_{\text{Ti}}$  being smaller (less than  $10^\circ$ ), the  $\text{ZrO}_6$  octahedra are, therefore, distorted differently depending on the type of the third neighbors (Zr or Ti) of the Zr central atom.

In BTZ relaxors, the existence of a nearly constant buckling angle as a function of the Zr substitution rate  $x$ , together with the invariant Zr-O1 distance (Sec. III B) result in a Zr-Zr distance of the order of  $4.15 \text{ \AA}$ , which hardly varies with  $x$ . Of course, the Zr-Zr distance is smaller in BTZ samples than in  $\text{BaZrO}_3$ , since the oxygen atoms are aligned with the Zr-Zr bonds in the latter compound. The Zr-Ti distance ( $4.07 \text{ \AA}$ ) does not change with  $x$ , and is found to be significantly smaller than the Zr-Zr distance. The Zr-Ba distance, on its turn, increases with  $x$ . From the Zr-Ti distance and the buckling angle of the Zr-O1-Ti bond, we can derive the Ti-O1 distance value at 300 K in BTZ relaxors, which is of the order of  $1.98 \text{ \AA}$ . This corresponds to the shortest Ti-O distance in the quadratic  $\text{BaTiO}_3$  at 300 K.<sup>53</sup>

We now consider the temperature dependence of  $\sigma_2^2$  in the  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  sample. As shown in Fig. 11, it can be described following Eq. (2) with an Einstein temperature equal to  $231 \pm 4$  K, instead of  $194 \pm 8$  K in  $\text{BaZrO}_3$ . This result indicates an increase of Zr-Ba bond strength with increasing Ti content. In addition, a constant  $\Delta\sigma_2^2 = 0.0019 \text{ \AA}^2$  must be added to Eq. (2), revealing the presence of a static disorder. The full width at half maximum of the corresponding Gaussian distance distribution would be equal to  $2\sqrt{2 \ln 2} \Delta\sigma_2^2 = 0.10 \text{ \AA}$ . However, let us remind the reader that other distance distributions can be expected (see Sec. III B). The possible distribution of the Zr-Zr and Zr-Ti bond lengths is out of the scope of this study, since  $\sigma_3^2$  and  $\sigma_3^2$  parameters had to be fixed during the refinement process.

The mean number of Zr third neighbors around a Zr atom  $N_{\text{Zr}}$  brings information on the distribution of the Zr and Ti atoms in BTZ relaxor samples.  $N_{\text{Zr}}$  is found to be equal to 2.7, 3.1, and 3.4 in  $\text{BaTi}_{0.75}\text{Zr}_{0.25}\text{O}_3$ ,  $\text{BaTi}_{0.70}\text{Zr}_{0.30}\text{O}_3$ , and  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$  samples, respectively. Despite the large uncertainty attached to  $N_{\text{Zr}}$  ( $\pm 1.0$ ), the measured values are higher than those expected for a random distribution of Zr

and Ti atoms: 1.5, 1.8, and 2.1. This observation indicates a tendency of Zr atoms to segregate in Zr-rich regions. However, with the EXAFS technique giving only an average of the local structure, we cannot conclude on the Zr concentration in the Zr-rich regions, and hence on the sizes of these regions.

In summary, in all the BTZ relaxors investigated the shape of a  $\text{ZrO}_6$  octahedra depends on the nature of its neighboring octahedra ( $\text{ZrO}_6$  or  $\text{TiO}_6$ ), the oxygen atoms being differently off-centered with respect to the Zr-Zr and Zr-Ti bonds. The Zr-Zr and Zr-Ti distances do not depend on  $x$ , Zr-Ti distances being significantly shorter than Zr-Zr ones. The Zr-Ba bond length increases with the Zr content, and is affected by a strong static disorder. Finally, the EXAFS analysis reveals a tendency of Zr atoms to segregate. Note that in the case of  $\text{BaTi}_{0.65}\text{Zr}_{0.35}\text{O}_3$ , the Zr environment is found to be remarkably stable with temperature. Therefore, no important changes of the local structure are observed around Zr atoms in the temperature range of the maximum of the dielectric permittivity.

## IV. CONCLUDING DISCUSSION

### A. Microstructural picture of BTZ relaxors

In the preceding sections we have described quantitatively the local structural features of the Zr environment in BTZ relaxors. It is now interesting to discuss how this local structure contrasts with the average, long-range cubic structure evidenced by x-ray diffraction (XRD). The interatomic distances deduced from EXAFS are compared to those determined from XRD in Fig. 12. The two techniques yield quite different values of distances. On the one hand, the XRD measurements show that the unit cell dimensions of BTZ samples follow the Vegard's law, i.e., the cell volume cubic root linearly increases from its value in  $\text{BaTiO}_3$  to that in  $\text{BaZrO}_3$ . In the cubic relaxor samples, all the average distances then linearly increase with the Zr substitution rate  $x$ . On the other hand, the distances deduced from the EXAFS analysis systematically exceed those expected in the average structure and, with the exception of the Zr-Ba distance, are found to be independent of  $x$ . Considering that EXAFS probes the structure on a very local scale, the latter observation is a direct evidence that the local structure is different from the average structure.

We have shown in Sec. III D 3 that Zr atoms tend to segregate in BTZ relaxors. The latter result is in agreement with previous speculations based on Raman scattering.<sup>25</sup> If we assume that the Zr-rich regions consist of  $\text{BaZrO}_3$  spherical inclusions in a  $\text{BaTiO}_3$  matrix, it is possible to roughly estimate the mean number of segregated atoms, as well as the size of the inclusions. Pure  $\text{BaZrO}_3$  regions with radii of  $a'$ ,  $a'\sqrt{2}$ ,  $a'\sqrt{3}$ , and  $2a'$  were considered ( $a' = R_3$  is the Zr-Zr distance given in Table IV). These inclusions contain 7, 19, 27, and 33 Zr atoms, respectively. The number of Zr neighbors was determined for each of these Zr atoms, and averaged on the inclusions. The average number of Zr neighbors of one Zr atom is found to be equal to 1.7, 3.2, 3.4, and 3.6 in the spherical inclusions with radii of  $a'$ ,  $a'\sqrt{2}$ ,  $a'\sqrt{3}$ , and  $2a'$ , respectively. The latter values can directly be compared

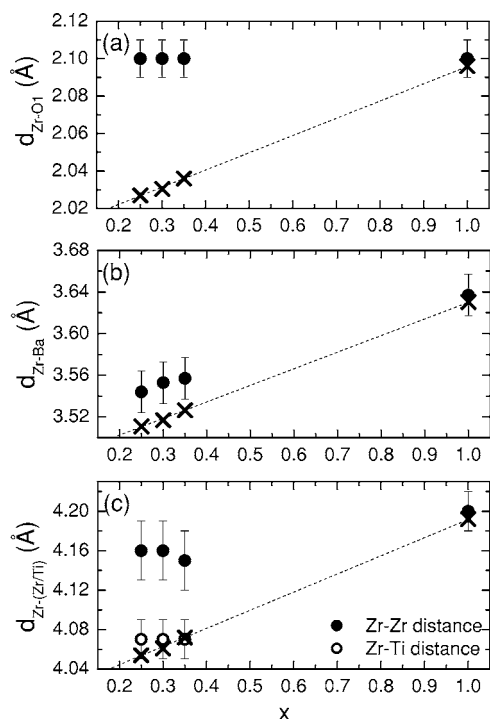


FIG. 12. Evolution of the Zr-O1 (a), Zr-Ba (b), and Zr-(Zr/Ti) (c) distances with the Zr substitution rate  $x$ . EXAFS results are reported as round dots. They are compared to the corresponding average distances deduced from the x-ray diffraction experiments (crosses); i.e.,  $a/2$ ,  $a\sqrt{3}/2$ , and  $a$ , respectively, where  $a$  is the cubic cell parameter.

to  $N_{\text{Zr}}$ , the mean number of Zr atoms around one Zr atom deduced from the EXAFS analysis. From Table IV, we conclude that the mean number of Zr atoms segregated in hypothetical spherical  $\text{BaZrO}_3$  regions would be 27 in BTZ with  $x=0.35$ , corresponding to a radius of  $a'\sqrt{3}=7.2$  Å. Concerning BTZ samples with  $x=0.30$  and  $0.25$ , linear interpolations on the values enumerated above result in regions of mean radii 5.8 Å (19 Zr atoms) and 5.3 Å (15 Zr atoms), respectively.

The EXAFS study of BTZ relaxors at the Zr  $K$  edge thus allowed us to evidence local structural deviations from the average cubic structure, as well as chemical inhomogeneities. In the following, we shall propose a microstructural picture of BTZ relaxors and discuss its origin and implications on the relaxor behavior. In order to expose the possible basic physical mechanisms in a clear and simple manner, we will assume that the segregation of Zr atoms consists of small inclusions of  $\text{BaZrO}_3$  (non-necessarily spherical) in a  $\text{BaTiO}_3$  matrix. However, let us recall that the real repartition of the Zr atoms could be much more complex (see Sec. III D 3).

Such  $\text{BaZrO}_3$  inclusions in BTZ relaxors must be submitted to a chemical pressure from the  $\text{BaTiO}_3$  environment, which has a smaller unit cell volume than  $\text{BaZrO}_3$ . It is first interesting to note that the Zr-O distance in BTZ relaxors is almost insensitive to this chemical pressure, since it is the same as in  $\text{BaZrO}_3$  [Fig. 12(a)]. On the other hand, the Zr-Ba distance decreases with increasing Ti content [Fig. 12(b)] and hence, is more sensitive to the chemical pressure. This

latter difference in  $\text{ABO}_3$  perovskites is well understood within the polyhedral approach: the A-O distance in perovskites is generally more compressible than the shorter B-O distance in the closed-packed  $\text{BO}_6$  octahedra.<sup>54</sup> Insight into the  $\text{BO}_6$  linkage can be also gained from the  $\widehat{\text{ZrO1Zr}}$  angle value, which deviates considerably from  $180^\circ$  (Table IV). In a perovskite structure, the presence of buckled Zr-O-Zr bonds suggests the presence of octahedron tilts. This distortion could be a direct consequence of the chemical pressure exerted by the surrounding  $\text{BaTiO}_3$  matrix. Within this context, let us be reminded that the hydrostatic pressure reveals and/or enhances structural lattice instabilities related to tilts in the perovskite compounds with  $\text{BO}_6$  polyhedra more rigid than  $\text{AO}_{12}$  ones.<sup>55</sup> Furthermore, it has been proposed in the literature that  $\text{BaZrO}_3$  undergoes a pressure-induced phase transition to the tilted  $a^-a^-a^-$  perovskite structure<sup>56</sup> (Glazer's notations<sup>57</sup>). Assuming that the  $\text{BaZrO}_3$  inclusions adopt the latter structure in BTZ relaxors, the tilt angle calculated from the buckling angle of the Zr-O-Zr bonds is about  $11^\circ$ , which is a reasonable value for a tilted perovskite.<sup>58–60</sup> In summary, within our simplified picture,  $\text{BaZrO}_3$  inclusions do not adopt the cubic bulk structure of  $\text{BaZrO}_3$  but present considerable distortions away from it. The Zr environment in BTZ relaxors appears to be determined by both the high stiffness of the  $\text{ZrO}_6$  octahedra and chemical pressure effects.

Let us now discuss the structure around the inclusions. Given that the Zr-Zr distance is approximately 2% larger than the average B-B cation distance deduced from XRD [Fig. 12(c)], we expect a significant strain at the interface of the  $\text{BaZrO}_3$  inclusions and the  $\text{BaTiO}_3$  matrix. The  $\text{TiO}_6$  octahedra adjacent to the inclusions likely accommodate the structural misfit between  $\text{BaZrO}_3$  inclusions and the  $\text{BaTiO}_3$  matrix. Considering that the cell volume of  $\text{BaZrO}_3$  is larger than that of  $\text{BaTiO}_3$ , we expect that these adjacent  $\text{TiO}_6$  octahedra are then submitted to a tensile strain. Although their deformation shape remains an open question, different  $\text{Ti}^{4+}$  displacements (and thus polarity) are expected in the adjacent regions when compared to the  $\text{BaTiO}_3$  matrix. These displacements, which depend on local strain, would naturally lead to random electric fields. Note that the important impact of the local chemical environment has already been evoked for the solid solution  $\text{Pb}(\text{Sc}, \text{Ta})\text{O}_3\text{-PbTiO}_3$  (PST-PT).<sup>39</sup>

## B. Comparison to PZT

We have already mentioned in the Introduction that the ferroelectric  $\text{PbZr}_{1-x}\text{Ti}_x\text{O}_3$  (PZT), similar to BTZ, does surprisingly present no relaxation, making the comparison of BTZ to PZT insightful. First, we note that in both BTZ and PZT, the mean Zr-O distance is almost unaffected by the Ti content, and equal to 2.07–2.08 Å within the data accuracy, which is very close to the Zr-O distance in BTZ and  $\text{BaZrO}_3$  (2.10 Å).<sup>33</sup> As a consequence, the relaxor properties of BTZ cannot only be linked to the stiffness of  $\text{ZrO}_6$  octahedra.

It is obvious that the presence of either  $\text{Ba}^{2+}$  or  $\text{Pb}^{2+}$  cations, which show very dissimilar electronic configurations, can drive the different properties of BTZ and PZT. However, an explanation for the different behaviors of BTZ and PZT could lie in the local chemical order, which is known to play

a determinant role for relaxor properties (e.g., the so-called 1:1 Mg/Nb order on the nanometer scale in PMN).<sup>10,11</sup> In that context, it is interesting to note that BTZ cannot be synthesized in the region  $0.5 < x < 1$  (Ref. 7), which suggests an important internal chemical strain which inhibits the formation of BTZ across the whole composition range. We speculate that the local phase segregation observed for BTZ relaxors is a precursor for the macroscopic phase separation observed for higher Zr substitution rates. Such an internal chemical strain does not seem to exist for PZT since it forms a solid solution whatever the Zr/Ti ratio. The distribution of elastic fields is thus expected to differ significantly from BTZ to PZT. In particular, the strain around the local phase

separation in BTZ can be regarded as the source of random elastic fields. Such random elastic fields are then considered to lead to a particular local pattern of polar regions and thus random electric fields, that cause the relaxor behavior.

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