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High-frequency rheological behaviour of a multiconnected lyotropic phase

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Abstract. – High-frequency (up to $\omega = 6 \cdot 10^4$ rad/s) rheological measurements combined with light scattering investigations show that an isotropic and multiconnected phase of surfactant micelles exhibits a terminal relaxation time of a few μ s, much smaller than in solutions of entangled wormlike micelles. This result is explained in terms of the local hexagonal order of the microscopic structure and we discuss its relevance for the understanding of dynamic behaviour in related systems, such as wormlike micelles and sponge phases.

In recent years, experimental evidence was presented as to the existence of isotropic phases consisting of connected surfactant micelles [1–3]. It has been proposed that they provide an intermediate structure between entangled wormlike micelles and sponge phases [4, 5]. Indeed, experimental results [4, 6, 7] show that, in some ionic wormlike micellar systems, a dramatic decrease in both viscosity and relaxation time is induced by increasing the counterion concentration, feature that could be explained by the appearance of connections in the micellar network. On the theoretical side, models for the flow behaviour of these connected phases have been developed [5, 8], and rheology data has been interpreted according to these models in order to characterize the appearance of connections, qualitatively [9–11] or quantitatively [12]. Throughout this body of work, however, only the relaxation modes specific to polymer systems have been considered. This approach is certainly valid in dilute phases with not too many connections, but it must fail when the density of connections becomes important and in concentrated systems, where the micelles begin to interact (sterically or otherwise). How does the system behave then and which are the relevant concepts ?

In this Letter, we try to answer these questions by investigating a concentrated and highly connected isotropic phase of a nonionic surfactant/water mixture. We argue that, in the absence of reptation (suppressed by the connections), it can be short-range order (for a concentrated system) that dominates the rheological behaviour.

We employ high-frequency rheology and dynamical light scattering (DLS) to study the isotropic phase in the $C_{12}EO_6/H_2O$ lyotropic mixture, where $C_{12}EO_6$ is the non-ionic surfactant hexa-ethylene glycol mono-n-dodecyl-ether, or $CH_3(CH_2)_{11}(OCH_2CH_2)_6OH$ (for the

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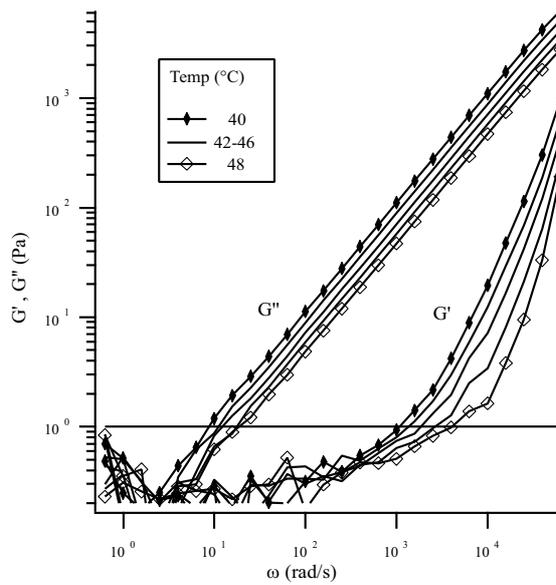


Fig. 1 – Storage (G') and loss (G'') moduli as a function of ω at different temperatures. Solid curves are guides for the eye. Only values above 1 Pa (solid horizontal line) are relevant.

phase diagram see [13]). Its dynamic behaviour has already been investigated by measuring the shear viscosity [14, 15], sound velocity and ultrasonic absorption [15] as well as NMR relaxation rates [16], all pointing to the presence of wormlike micelles (at least above 10 % surfactant concentration by weight [15]). In previous experiments [17, 18] we have shown that, for 50 % wt surfactant concentration, above the hexagonal mesophase, the isotropic phase has a structure consisting of surfactant cylinders that locally preserve the hexagonal order over a distance d that varies from about 40 nm at 40 °C to 25 nm at 60 °C. Between the cylinders there is a large number of thermally activated connections (with an estimated density $n \sim 10^6 \mu\text{m}^{-3}$) [18].

We prepared the $\text{C}_{12}\text{EO}_6/\text{H}_2\text{O}$ mixture with 50.0 % C_{12}EO_6 weight concentration. The surfactant was purchased from Nikko Chemicals Ltd. and used without further purification. We used ultrapure water from Fluka Chemie AG. The mixture was carefully homogenized by repeatedly heating, stirring and centrifuging and then allowed to equilibrate at room temperature over a few days.

Rheology measurements were performed in a piezorheometer, the principle of which has been described in reference [19]: the liquid sample of thickness $60 \mu\text{m}$ is contained between two glass plates mounted on piezoelectric ceramics. One of the plates is made to oscillate vertically with an amplitude of about 1 nm by applying a sine wave to the ceramic. This movement induces a squeezing flow in the sample and the stress transmitted to the second plate is measured by the other piezoelectric element. The shear is extremely small: $\gamma \leq 10^{-4}$, so the sample structure is not altered by the flow. The setup allows us to measure the storage (G') and loss (G'') shear moduli for frequencies ranging from 1 to $6 \cdot 10^4$ rad/s with five points per frequency decade. The entire setup is temperature regulated within $0.05 \text{ }^\circ\text{C}$ and hermetically sealed to avoid evaporation.

Ten temperature points in the isotropic phase have been investigated, from $38.85 \text{ }^\circ\text{C}$ (tran-

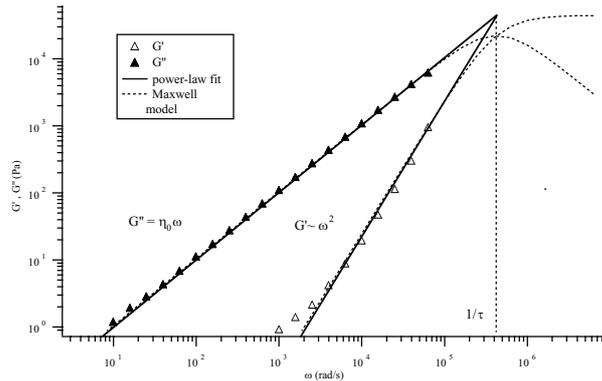


Fig. 2 – Typical data fit ($T=40^\circ\text{C}$) : thick lines, power-law fit ($G' \propto \omega^2$ and $G'' = \eta_0\omega$). The curves cross at a frequency $\omega = 1/\tau$, where τ is the terminal relaxation time. Dotted curves, Maxwell model fit (eq. 1) with the parameters η_0 and τ .

sition temperature from the hexagonal phase) up to 48°C . The results are displayed in figure 1. For clarity, only curves corresponding to $40, 42, 44, 46,$ and 48°C are plotted. Values below 1 Pa (solid horizontal line) are not reliable, as the signal/noise ratio becomes poor. At low frequencies, the response is purely viscous; it is only above $\omega = 10^3\text{ rad/s}$ that there is a noticeable increase in the value of the storage modulus G' .

On general grounds, the low-frequency behaviour of the storage and loss moduli in a fluid is [20] : $G' \propto \omega^2$ and $G'' \propto \omega$. The slope of G' vs. ω yields the "zero-shear viscosity" η_0 and the two curves cross at a frequency $\omega = 1/\tau$, where τ is the terminal relaxation time. The ratio η_0/τ defines a shear modulus. If τ is the only relevant time scale in the system, the complex modulus $G^*(\omega) = G' + iG''$ has a simple analytical expression, known as the Maxwell model [20] :

$$G^*(\omega) = \frac{i\omega\eta_0}{1 + i\omega\tau}. \quad (1)$$

The relaxation time τ separates two regimes : for $\omega\tau \ll 1$, the system can be considered as a viscous fluid with viscosity η_0 , while for $\omega\tau \gg 1$ it exhibits elasticity, with a shear modulus $G_\infty = \eta_0/\tau$.

As shown in 2, we obtain robust results for the static viscosity η_0 and for the relaxation time τ (plotted vs. temperature in figure 3).

The temperature variation of the parameters η_0 and τ can be described by Arrhenius laws; for the viscosity :

$$\eta_0(T) = \eta_0(T^*) \exp \left[\frac{E_\eta}{k_B} \left(\frac{1}{T} - \frac{1}{T^*} \right) \right], \quad (2)$$

yielding an activation energy $E_\eta = 35 \pm 1 k_B T$ (solid curve in figure 3). For comparison, continuous shear measurements in a Couette rheometer (Haake, model RS100), give an activation energy $E_\eta = 31 k_B T$ [21]. The relaxation time has an activation energy $E_\tau = 38 \pm 6 k_B T$ (solid curve in figure 3). Within experimental precision, $E_\eta = E_\tau$. The high-frequency elastic modulus is therefore constant in temperature :

$$G_\infty = \eta_0/\tau = 44 \pm 6 \cdot 10^3 \text{ Pa}. \quad (3)$$

The DLS setup uses an Ar laser ($\lambda = 514\text{ nm}$), delivering up to 1.5 W , a thermostated bath of an index matching liquid (decahydronaphthalene, $n = 1.48$), a photomultiplier and a PC-

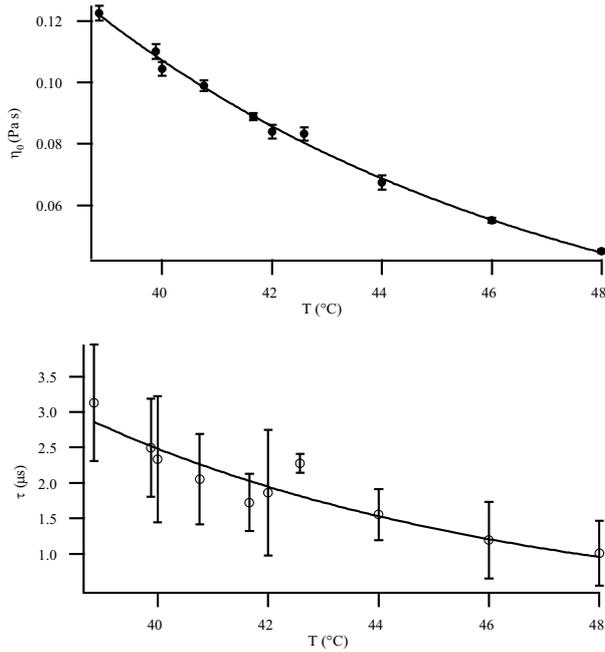


Fig. 3 – Static viscosity η_0 and relaxation time τ as a function of temperature. Solid line is an Arrhenius law fit (see text). The curves start at 38.85 °C, the transition temperature from the hexagonal phase.

controlled 256 channel Malvern correlator with sample times as fast as 0.1 μ s. The scattering vector q varies in the range $4 \cdot 10^6 - 3 \cdot 10^7 \text{ m}^{-1}$. The signal is monoexponential over the whole range. In figure 4 we show the relaxation rate $\Omega(q)$ vs. q^2 for temperatures between 40 and 49 °C. The data fit well to a diffusion law (although there is a slight indication of superdiffusive behaviour). Since the scattered intensity is related to the variations in refractive index produced by concentration fluctuations, we obtain the collective diffusion constant for the concentration field; its temperature variation can be described by an Arrhenius fit (solid curve in figure 4 – inset) with an activation energy $E_D \simeq 4 k_B T$. The average value :

$$D = 1.65 \cdot 10^{-10} \text{ m}^2/\text{s} \quad (4)$$

is in good agreement with the one previously obtained from directional-growth experiments [22] : $D = 1.2 \cdot 10^{-10} \text{ m}^2/\text{s}$ at the transition temperature (38.85 °C).

In unconnected wormlike micellar systems [5,24,25], the relevant relaxation process is reptation, the micelle gradually disengaging from its initial deformed environment and adopting a stress-free configuration. The typical reptation time is given by : $\tau_{\text{rep}} \simeq L_m^2/D_c$, with L_m the average length of a micelle and D_c the curvilinear diffusion constant. However, if the micelles can break up (with a lifetime τ_{br}) this provides an additional pathway for disengagement, the two resulting ends being free to recombine in a different environment. For $\tau_{\text{br}} \ll \tau_{\text{rep}}$, the terminal relaxation time is given by : $\tau = (\tau_{\text{br}}\tau_{\text{rep}})^{1/2}$ [24]. As an illustration, in the CTAB/H₂O/KBr system the typical micelle length is $L_m \simeq 1 \mu\text{m}$, while τ varies between 0.1 and 1 s depending on the surfactant concentration [26].

Let us now consider the effect of connections; following Drye and Cates [5], we will in-

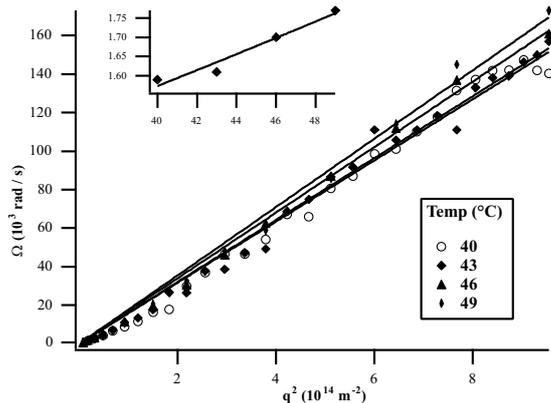


Fig. 4 – Relaxation frequency Ω versus q^2 for different temperature values. Lines are linear fits through the origin. The inset shows the values of D (in units of $10^{-10} \text{ m}^2/\text{s}$) as a function of temperature. Solid curve is an Arrhenius fit.

introduce a typical micelle length between cross-links L_c . The effect of the connections is that reptation occurs on distances of the order of L_c , instead of the much larger L_m [25]. This explains the fact (counterintuitive at first sight) that connecting the network does in fact reduce the viscosity. If L_c is small enough, the network is saturated, and the concept of entanglement is no longer applicable; neither is the reptation mechanism. The system we investigate is well in the saturated case, since the typical distance between connections on a micelle is only four times the mean distance between micelles [18].

What is then the origin of viscoelasticity? We begin the discussion of our results with the very general observation that, when a system is dynamically correlated over a typical distance L , one can only observe elastic behaviour by probing the system on scales smaller than the correlation distance [27]. The time τ needed to relax the stress can then be estimated as :

$$\tau \sim L^2 / (2\delta D), \quad (5)$$

where δ is the space dimension and D is the diffusion constant associated to the relaxation process (a classical example is provided by the Nabarro–Herring creep in solids [23]). The system under investigation is very concentrated so, in contrast with the semi-dilute wormlike micellar solutions usually studied, the micelle-micelle interaction plays an important role in the dynamics of the phase. This interaction locally induces hexagonal order as mentioned above; the relevant correlation length is the distance d over which the micelles preserve local order. A pictorial representation is given in figure 5 : consider a material with short-range order confined between two plates. The system can be seen as consisting of elasticity-endowed units of typical size d , the correlation distance. After applying an instantaneous shear γ by moving the upper plate to the left, one such unit (represented in thick line) has been advected from point 1 to point 2. At time $t = 0^+$ after the deformation, the stress on the upper plate is $\sigma = G_\infty \gamma$. Since there is no long-range restoring force, once the particles equilibrate their internal configuration (over a distance d), the elastic stress is completely relaxed; thus, after a time τ given by eq. 5, $\sigma = 0$.

Does this mechanism account for the observed behaviour? In light of the previous discussion, let us estimate the relaxation time for our system. With the value of d obtained from

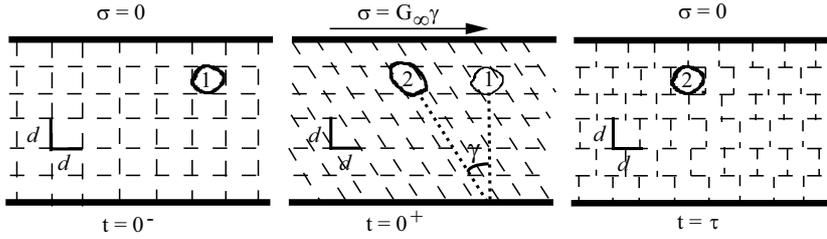


Fig. 5 – Schematic representation of shear in a material consisting of units of typical size d . One such unit (thick line contour) has been displaced between points 1 and 2. The instantaneous elastic stress is $\sigma = G_\infty\gamma$; it relaxes over a typical time τ given by equation 5.

X-ray scattering and the DLS collective diffusion coefficient (eq. 4), one has :

$$\tau \simeq d^2/(6D) \sim 10^{-6} \text{ s}, \quad (6)$$

in good agreement with the experimental results (figure 3).

A rough estimate of G_∞ can be obtained by noticing that at short range (less than d), the structure of the phase resembles that of the hexagonal one, so it should exhibit a similar shear modulus when probed on very short scales. The shear modulus of the hexagonal phase can be estimated as $G_{\text{hex}} = k_B T/a^3 \simeq 2 \cdot 10^4 \text{ Pa}$ (with $a = 6 \text{ nm}$ the lattice parameter), in agreement with our result (eq. 3). This value can also be compared with preliminary measurements of the shear modulus in the hexagonal phase of C_{12}EO_6 [28] yielding :

$$G_{\text{hex}} \simeq 2 \cdot 10^5 \text{ Pa} \quad (7)$$

at room temperature, of the same order of magnitude as our result. The shear modulus of the hexagonal phase should vary very little with temperature, in agreement with our experimental findings.

However, our very simple model does not accurately describe the temperature variation of the physical parameters in equation 6. An Arrhenius fit of $d(T)$ (from the X-ray data of reference [18]) yields an activation energy $E_d = 7 \pm 1 k_B T$. From equation (7) we would expect that :

$$E_\tau = 38 \pm 6 k_B T \sim 2E_d + E_D = 18 \pm 2 k_B T \quad (8)$$

which is clearly off by a factor of two.

A tentative explanation involves the possible anisotropy of the correlated domains; in this case, the value obtained from the X-ray diffractogram is an average between a transverse correlation length $d = d_\perp$ (which is the one relevant for the relaxation) and a d_\parallel (which need not exhibit the same temperature variation). The same observation applies for D : we measure an average value, but at small scale the structure is anisotropic.

A more detailed comparison with theory requires additional data on unsaturated structures. We are currently investigating the same isotropic phase at lower surfactant concentration, where preliminary experiments show rather complicated rheological behaviour.

Finally, we suggest that this approach can also be applied to sponge phases, the characteristic distance being ξ , the correlation length. These phases are equally very fluid and, at low frequency (up to at least 10^2 s^{-1}), display pure Newtonian behaviour [29, 30]. Within the framework of the same highly simplified model (equation 5), we predict a relaxation time of order $\tau \sim \xi^2/(6D)$. For instance, in the C_{12}EO_5 /hexanol/water system at 5.3 % volume fraction of membrane, where $\xi \simeq 0.1 \mu\text{m}$ and $D \simeq 2 \cdot 10^{-12} \text{ m}^2/\text{s}$ [31], we expect $\tau \sim 10^{-3} \text{ s}$.

In conclusion, we study the dynamics of the isotropic (micellar) phase in the $C_{12}EO_6/H_2O$ mixture at high concentration, where it is highly connected. We show that the observed viscoelastic behaviour can be related to the local hexagonal order of the system.

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