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A Tensor-based Factorization Model of Semantic Compositionality

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Abstract

In this paper, we present a novel method for the computation of compositionality within a distributional framework. The key idea is that compositionality is modeled as a multi-way interaction between latent factors, which are automatically constructed from corpus data. We use our method to model the composition of subject verb object triples. The method consists of two steps. First, we compute a latent factor model for nouns from standard co-occurrence data. Next, the latent factors are used to induce a latent model of three-way subject verb object interactions. Our model has been evaluated on a similarity task for transitive phrases, in which it exceeds the state of the art.

1 Introduction

In the course of the last two decades, significant progress has been made with regard to the automatic extraction of lexical semantic knowledge from large-scale text corpora. Most work relies on the distributional hypothesis of meaning (Harris, 1954), which states that words that appear within the same contexts tend to be semantically similar. A large number of researchers have taken this dictum to heart, giving rise to a plethora of algorithms that try to capture the semantics of words by looking at their distribution in text. Up till now, however, most work on the automatic acquisition of semantics only deals with individual words. The modeling of meaning beyond the level of individual words – i.e. the combination of words into larger units – is to a large degree left unexplored.

The principle of compositionality, often attributed to Frege, is the principle that states that the meaning of a complex expression is a function of the meaning of its parts and the way those parts are (syntactically) combined (Frege, 1892). It is the fundamental principle that allows language users to understand the meaning of sentences they have never heard before, by constructing the meaning of the complex expression from the meanings of the individual words. Recently, a number of researchers have tried to reconcile the framework of distributional semantics with the principle of compositionality (Mitchell and Lapata, 2008; Baroni and Zamparelli, 2010; Coecke et al., 2010; Socher et al., 2012). However, the absolute gains of the systems remain a bit unclear, and a simple method of composition – vector multiplication – often seems to produce the best results (Blacoe and Lapata, 2012).

In this paper, we present a novel method for the joint composition of a verb with its subject and direct object. The key idea is that compositionality is modeled as a multi-way interaction between latent factors, which are automatically constructed from corpus data. In order to adequately model the multi-way interaction between a verb and its subject and objects, a significant part of our method relies on tensor algebra. Additionally, our method makes use of a factorization model appropriate for tensors.

The remainder of the paper is structured as follows. In section 2, we give an overview of previous work that is relevant to the task of computing compositionality within a distributional framework. Section 3 presents a detailed description of our method, including an overview of the necessary mathematical
machinery. Section 4 illustrates our method with a number of detailed examples. Section 5 presents a quantitative evaluation, and compares our method to other models of distributional compositionality. Section 6, then, concludes and lays out a number of directions for future work.

2 Previous Work

In recent years, a number of methods have been developed that try to capture compositional phenomena within a distributional framework. One of the first approaches to tackle compositional phenomena in a systematic way is Mitchell and Lapata’s (2008) approach. They explore a number of different models for vector composition, of which vector addition (the sum of each feature) and vector multiplication (the elementwise multiplication of each feature) are the most important. They evaluate their models on a noun-verb phrase similarity task, and find that the multiplicative model yields the best results, along with a weighted combination of the additive and multiplicative model.

Baroni and Zamparelli (2010) present a method for the composition of adjectives and nouns. In their model, an adjective is a linear function of one vector (the noun vector) to another vector (the vector for the adjective-noun pair). The linear transformation for a particular adjective is represented by a matrix, and is learned automatically from a corpus, using partial least-squares regression.

Coecke et al. (2010) present an abstract theoretical framework in which a sentence vector is a function of the Kronecker product of its word vectors, which allows for greater interaction between the different word features. A number of instantiations of the framework are tested experimentally in Grefenstette and Sadrzadeh (2011a) and Grefenstette and Sadrzadeh (2011b). The key idea is that relational words (e.g. adjectives or verbs) have a rich (multi-dimensional) structure that acts as a filter on their arguments. Our model uses an intuition similar to theirs.

Socher et al. (2012) present a model for compositionality based on recursive neural networks. Each node in a parse tree is assigned both a vector and a matrix; the vector captures the actual meaning of the constituent, while the matrix models the way it changes the meaning of neighbouring words and phrases.

Closely related to the work on compositionality is research on the computation of word meaning in context. Erk and Padó (2008, 2009) make use of selectional preferences to express the meaning of a word in context; the meaning of a word in the presence of an argument is computed by multiplying the word’s vector with a vector that captures the inverse selectional preferences of the argument. Thater et al. (2009, 2010) extend the approach based on selectional preferences by incorporating second-order co-occurrences in their model. And Dinu and Lapata (2010) propose a probabilistic framework that models the meaning of words as a probability distribution over latent factors. This allows them to model contextualized meaning as a change in the original sense distribution. Dinu and Lapata use non-negative matrix factorization (NMF) to induce latent factors. Similar to their work, our model uses NMF – albeit in a slightly different configuration – as a first step towards our final factorization model.

In general, latent models have proven to be useful for the modeling of word meaning. One of the best known latent models of semantics is Latent Semantic Analysis (Landauer and Dumais, 1997), which uses singular value decomposition in order to automatically induce latent factors from term-document matrices. Another well known latent model of meaning, which takes a generative approach, is Latent Dirichlet Allocation (Blei et al., 2003).

Tensor factorization has been used before for the modeling of natural language. Giesbrecht (2010) describes a tensor factorization model for the construction of a distributional model that is sensitive to word order. And Van de Cruys (2010) uses a tensor factorization model in order to construct a three-way selectional preference model of verbs, subjects, and objects. Our underlying tensor factorization – Tucker decomposition – is the same as Giesbrecht’s; and similar to Van de Cruys (2010), we construct a latent model of verb, subject, and object interactions. The way our model is constructed, however, is significantly different. The former research does not use any syntactic information for the construction of the tensor, while the latter makes use of a more restricted tensor factorization model, viz. parallel factor analysis (Harshman and Lundy, 1994).
The idea of modeling compositionality by means of tensor (Kronecker) product has been proposed in the literature before (Clark and Pulman, 2007; Coecke et al., 2010). However, the method presented here is the first that tries to capture compositional phenomena by exploiting the multi-way interactions between latent factors, induced by a suitable tensor factorization model.

3 Methodology

3.1 Mathematical preliminaries

The methodology presented in this paper requires a number of concepts and mathematical operations from tensor algebra, which are briefly reviewed in this section. The interested reader is referred to Kolda and Bader (2009) for a more thorough introduction to tensor algebra (including an overview of various factorization methods).

A tensor is a multidimensional array; it is the generalization of a matrix to more than two dimensions, or modes. Whereas matrices are only able to capture two-way co-occurrences, tensors are able to capture multi-way co-occurrences.\(^1\) Following prevailing convention, tensors are represented by boldface Euler script notation (\(\mathfrak{X}\)), matrices by boldface capital letters (\(X\)), vectors by boldface lower case letters (\(x\)), and scalars by italic letters (\(x\)).

The \(n\)-mode product of a tensor \(\mathfrak{X} \in \mathbb{R}^{I_1 \times I_2 \times \cdots \times I_N}\) with a matrix \(U \in \mathbb{R}^{I_i \times B}\) is denoted by \(\mathfrak{X} \times_n U\), and is defined elementwise as

\[
(\mathfrak{X} \times_n U)_{i_1 \ldots i_{n-1} j_{n+1} \ldots i_N} = \sum_{i_n=1}^{I_n} x_{i_1 i_2 \ldots i_{n-1} j_{n+1} i_n} u_{j_{n+1} i_n} \tag{1}
\]

The Kronecker product of matrices \(A \in \mathbb{R}^{I \times J}\) and \(B \in \mathbb{R}^{K \times L}\) is denoted by \(A \otimes B\). The result is a matrix of size \((IK) \times (JL)\), and is defined by

\[
A \otimes B = \begin{bmatrix}
a_{11}B & a_{12}B & \cdots & a_{1J}B \\
a_{21}B & a_{22}B & \cdots & a_{2J}B \\
\vdots & \vdots & \ddots & \vdots \\
a_{11}B & a_{12}B & \cdots & a_{1J}B
\end{bmatrix} \tag{2}
\]

\(^1\)In this research, we limit ourselves to three-way co-occurrences of verbs, subject, and objects, modelled using a three-mode tensor.

A special case of the Kronecker product is the outer product of two vectors \(a \in \mathbb{R}^I\) and \(b \in \mathbb{R}^J\), denoted \(a \circ b\). The result is a matrix \(A \in \mathbb{R}^{I \times J}\) obtained by multiplying each element of \(a\) with each element of \(b\).

Finally, the Hadamard product, denoted \(A \ast B\), is the elementwise multiplication of two matrices \(A \in \mathbb{R}^{I \times J}\) and \(B \in \mathbb{R}^{I \times J}\), which produces a matrix that is equally of size \(I \times J\).

3.2 The construction of latent noun factors

The first step of our method consists in the construction of a latent factor model for nouns, based on their context words. For this purpose, we make use of non-negative matrix factorization (Lee and Seung, 2000). Non-negative matrix factorization (NMF) minimizes an objective function – in our case the Kullback-Leibler (KL) divergence – between an original matrix \(V_{I \times J}\) and \(W_{I \times K}H_{K \times J}\) (the matrix multiplication of matrices \(W\) and \(H\)) subject to the constraint that all values in the three matrices be non-negative. Parameter \(K\) is set \(\ll I, J\) so that a reduction is obtained over the original data. The factorization model is represented graphically in figure 1.

\[
V = WH
\]

Figure 1: Graphical representation of NMF

NMF can be computed fairly straightforwardly, alternating between the two iterative update rules represented in equations 3 and 4. The update rules are guaranteed to converge to a local minimum in the KL divergence.

\[
H_{ij} \leftarrow H_{ij} \frac{\sum_k W_{ik} V_{kj}}{\sum_k W_{ik} H_{kj}} \tag{3}
\]

\[
W_{ia} \leftarrow W_{ia} \frac{\sum_j H_{ij} V_{ij}}{\sum_j H_{ij} W_{ij}} \tag{4}
\]

3.3 Modeling multi-way interactions

In our second step, we construct a multi-way interaction model for subject verb object (svo) triples, based
Tucker decomposition

Tucker decomposition is a multilinear generalization of the well-known singular value decomposition, used in Latent Semantic Analysis. It is also known as higher order singular value decomposition (HOSVD, De Lathauwer et al. (2000)). In Tucker decomposition, a tensor is decomposed into a core tensor, multiplied by a matrix along each mode. For a three-mode tensor $X \in \mathbb{R}^{I \times J \times L}$, the model is defined as

$$X = \mathcal{G} \times_1 A \times_2 B \times_3 C$$  \hspace{1cm} (5)

$$= \sum_{p=1}^{P} \sum_{q=1}^{Q} \sum_{r=1}^{R} g_{pq} a_p \circ b_q \circ c_r$$  \hspace{1cm} (6)

Setting $P, Q, R \ll I, J, L$, the core tensor $\mathcal{G}$ represents a compressed, latent version of the original tensor $X$; matrices $A \in \mathbb{R}^{I \times P}$, $B \in \mathbb{R}^{J \times Q}$, and $C \in \mathbb{R}^{L \times R}$ represent the latent factors for each mode, while $\mathcal{G} \in \mathbb{R}^{P \times Q \times R}$ indicates the level of interaction between the different latent factors. Figure 2 shows a graphical representation of Tucker decomposition.\(^2\)

3.3.2 Reconstructing a Tucker model from two-way factors

Computing the Tucker decomposition of a tensor is rather costly in terms of time and memory requirements. Moreover, the decomposition is not unique: the core tensor $\mathcal{G}$ can be modified without affecting the model’s fit by applying the inverse modification to the factor matrices. These two drawbacks led us to consider an alternative method for the construction of the Tucker model. Specifically, we consider the factor matrices as given (as the output from our first step), and proceed to compute the core tensor $\mathcal{G}$. Additionally, we do not use a latent representation for the first mode, which means that the first mode is represented by its original instances.

Our model can be straightforwardly applied to language data. The core tensor $\mathcal{G}$ models the latent interactions between verbs, subject, and objects. $\mathcal{G}$ is computed by applying the n-mode product to the appropriate mode of the original tensor (equation 7),

$$\mathcal{G} = X \times_2 W^T \times_3 W^T$$  \hspace{1cm} (7)

where $X^{V \times N \times N}$ is our original data tensor, consisting of the weighted co-occurrence frequencies of svo triples (extracted from corpus data), and $W^{N \times K}$ is our latent factor matrix for nouns. Note that we do not use a latent representation for the verb mode. To be able to efficiently compute the similarity of verbs (both within and outside of compositional phrases), only the subject and object mode are represented by latent factors, while the verb mode is represented by its original instances. This means that our core tensor $\mathcal{G}$ will be of size $V \times K \times K$.\(^3\) A graphical representation is given in figure 3.

Note that both tensor $X$ and factor matrices $W$ are non-negative, which means our core tensor $\mathcal{G}$ will also be non-negative.

3.4 The composition of svo triples

In order to compute the composition of a particular subject verb object triple $(s, v, o)$, we first extract the appropriate subject vector $w_s$ and object vector $w_o$ (both of length $K$) from our factor matrix $W$, and

\(^2\)where $P = Q = R = K$, i.e. the same number of latent factors $K$ is used for each mode

\(^3\)It is straightforward to also construct a latent factor model for verbs using NMF, and include it in the construction of our core tensor; we believe such a model might have interesting applications, but we save this as an exploration for future work.
Figure 3: A graphical representation of our model instantiation without the latent verb mode

compute the outer product of both vectors, resulting in a matrix $Y$ of size $K \times K$.

$$Y = w_s \circ w_o$$  \hfill (8)

Our second and final step is then to weight the original verb matrix $G_v$ of latent interactions (the appropriate verb slice of tensor $G$) with matrix $Y$, containing the latent interactions of the specific subject and object. This is carried out by taking the Hadamard product of $G_v$ and $Y$.

$$Z = G_v \cdot Y$$  \hfill (9)

4 Example

In this section, we present a number of example computations that clarify how our model is able to capture compositionality. All examples come from actual corpus data, and are computed in a fully automatic and unsupervised way.

Consider the following two sentences:

(1) The athlete runs a race.
(2) The user runs a command.

Both sentences contain the verb $run$, but they represent clearly different actions. When we compute the composition of both instances of $run$ with their respective subject and object, we want our model to show this difference.

To compute the compositional representation of sentences (1) and (2), we proceed as follows. First, we extract the latent vectors for subject and object ($w_{\text{athlete}}$ and $w_{\text{race}}$ for the first sentence, $w_{\text{user}}$ and $w_{\text{command}}$ for the second sentence) from matrix $W$. Next, we compute the outer product of subject and object – $w_{\text{athlete}} \circ w_{\text{race}}$ and $w_{\text{user}} \circ w_{\text{command}}$ – which yields matrices $Y_{(\text{athlete},\text{race})}$ and $Y_{(\text{user},\text{command})}$. By virtue of the outer product, the matrices $Y$ – of size $K \times K$ – represent the level of interaction between the latent factors of the subject and the latent factors of the object. We can inspect these interactions by looking up the factor pairs (i.e. matrix cells) with the highest values in the matrices $Y$. Table 1 presents the factor pairs with highest value for matrix $Y_{(\text{athlete},\text{race})}$; table 2 represents the factor pairs with highest value for matrix $Y_{(\text{user},\text{command})}$. In order to render the factors interpretable, we include the three most salient words for the various factors (i.e. the words with the highest value for a particular factor).

The examples in tables 1 and 2 give an impression of the effect of the outer product: semantic features of the subject combine with semantic features of the object, indicating the extent to which these features interact within the expression. In table 1, we notice that animacy features (28, 195) and a sport feature (25) combine with a ‘sport event’ feature (119). In table 2, we see that similar animacy features (40, 195) and technological features (7, 45) combine with another technological feature (89).

Similarly, we can inspect the latent interactions of the verb $run$, which are represented in the tensor slice $G_{\text{run}}$. Note that this matrix contains the verb semantics computed over the complete corpus. The most salient factor interactions for $G_{\text{run}}$ are represented in table 3.

Table 3 illustrates that different senses of the verb $run$ are represented within the matrix $G_{\text{run}}$. The first two factor pairs hint at the ‘organize’ sense of the verb ($run$ a seminar). The third factor pair represents the ‘transport’ sense of the verb (the bus runs every hour). And the fourth factor pair represents the ‘execute’ or ‘deploy’ sense of $run$ ($run$ Linux, run a computer program). Note that we only show the factor pairs with the highest value; matrix $G$ contains a value for each pairwise combination of the latent factors, effectively representing a rich latent semantics for the verb in question.

The last step is to take the Hadamard product of matrices $Y$ with verb matrix $G$, which yields our final

\footnote{Obviously, hour is not an object of the verb, but due to parsing errors it is thus represented.}
matrices, $Z_{\text{run},(\text{athlete, race})}$ and $Z_{\text{run},(\text{user, command})}$. The Hadamard product will act as a bidirectional filter on the semantics of both the verb and its subject and object: interactions of semantic features that are present in both matrix $Y$ and $G$ will be highlighted, while the other interactions are played down. The result is a representation of the verb’s semantics tuned to its particular subject-object combination. Note that this final step can be viewed as an instance of function application (Baroni and Zamparelli, 2010). Also note the similarity to Grefenstette and Sadrzadeh’s (2011a, 2011b) approach, who equally make use of the elementwise matrix product in order to weight the semantics of the verb.

We can now go back to our original tensor $G$, and compute the most similar verbs (i.e. the most similar tensor slices) for our newly computed matrices $Z$.\(^5\)

If we do this for matrix $Z_{\text{run},(\text{athlete, race})}$, our model comes up with verbs `finish` (.29), `attend` (.27), and `win` (.25). If, instead, we compute the most similar verbs for $Z_{\text{run},(\text{user, command})}$, our model yields `execute` (.42), `modify` (.40), `invoke` (.39).

Finally, note that the design of our model naturally takes into account word order. Consider the following two sentences:

(3) man damages car
(4) car damages man

Both sentences contain the exact same words, but the process of damaging described in sentences (3) and (4) is of a rather different nature. Our model is able to take this difference into account: if we compute $Z_{\text{damage, (man, car)}}$ following sentence (3), our model yields `crash` (.43), `drive` (.35), `ride` (.35) as most similar verbs. If we do the same for $Z_{\text{damage, (car, man)}}$ following sentence (4), our model instead yields `scare` (.26), `kill` (.23), `hurt` (.23).

5 Evaluation

5.1 Methodology

In order to evaluate the performance of our tensor-based factorization model of compositionality, we make use of the sentence similarity task for transitive sentences, defined in Grefenstette and Sadrzadeh (2011a). This is an extension of the similarity task for compositional models developed by Mitchell and Lapata (2008), and constructed according to the same guidelines. The dataset contains 2500 similarity judgements, provided by 25 participants, and is publicly available.\(^6\)

The data consists of transitive verbs, each paired with both a subject and an object noun – thus forming a small transitive sentence. Additionally, a ‘landmark’ verb is provided. The idea is to compose both the target verb and the landmark verb with subject and noun, in order to form two small compositional

\(^5\)Similarity is calculated by measuring the cosine of the vectorized and normalized representation of the verb matrices.

\(^6\)http://www.cs.ox.ac.uk/activities/CompDistMeaning/GD2011data.txt
Table 3: Factor combinations for \( G_{rn} \)

<table>
<thead>
<tr>
<th>factors</th>
<th>subject</th>
<th>object</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(128, 181)</td>
<td>( \text{Mathematics (.004), Science (.004), Economics (.004)} )</td>
<td>( \text{course (.005), tutorial (.005), seminar (.005)} )</td>
<td>.058</td>
</tr>
<tr>
<td>(293, 181)</td>
<td>( \text{organization (.007), association (.007), federation (.006)} )</td>
<td>( \text{course (.005), tutorial (.005), seminar (.005)} )</td>
<td>.053</td>
</tr>
<tr>
<td>(60, 140)</td>
<td>( \text{rail (.111), bus (.009), ferry (.008)} )</td>
<td>( \text{third (.004), decade (.004), hour (.004)} )</td>
<td>.038</td>
</tr>
<tr>
<td>(268, 268)</td>
<td>( \text{API (.008), Apache (.007), Unix (.007)} )</td>
<td>( \text{API (.008), Apache (.007), Unix (.007)} )</td>
<td>.038</td>
</tr>
</tbody>
</table>

Table 4: Two example judgements from the phrase similarity task defined by Grefenstette and Sadrzadeh (2011a)

<table>
<thead>
<tr>
<th>p</th>
<th>target</th>
<th>subject</th>
<th>object</th>
<th>landmark</th>
<th>sim</th>
</tr>
</thead>
<tbody>
<tr>
<td>19</td>
<td>meet</td>
<td>system</td>
<td>criterion</td>
<td>visit</td>
<td>1</td>
</tr>
<tr>
<td>21</td>
<td>write</td>
<td>student</td>
<td>name</td>
<td>spell</td>
<td>6</td>
</tr>
</tbody>
</table>

Grefenstette and Sadrzadeh (2011a) seem to calculate the similarity score contextualizing both the target verb and the landmark verb. Another possibility is to contextualize only the target verb, and compute the similarity score with the non-contextualized landmark verb. In our view, the latter option provides a better assessment of the model’s similarity judgements, since contextualizing low-similarity landmarks often yields non-sensical phrases (e.g. system visits criterion). We provide scores for both contextualized and non-contextualized landmarks.

We compare our results to a number of different models. The first is Mitchell and Lapata’s (2008) model, which computes the elementwise vector multiplication of verb, subject and object. The second is Grefenstette and Sadrzadeh’s (2011b) best scoring model instantiation of the categorical distributional compositional model (Coecke et al., 2010). This model computes the outer product of the subject and object vector, the outer product of the verb vector with itself, and finally the elementwise product of both results. It yields the best score on the transitive sentence similarity task reported to date.

As a baseline, we compute the non-contextualized
similarity score for target verb and landmark. The upper bound is provided by Grefenstette and Sadrzadeh (2011a), based on interannotator agreement.

5.2 Implementational details

All models have been constructed using the UKWAC corpus (Baroni et al., 2009), a 2 billion word corpus automatically harvested from the web. From this data, we accumulate the input matrix \( V \) for our first NMF step. We use the 10K most frequent nouns, cross-classified by the 2K most frequent context words. In our view, the latter option provides a better assessment of the model’s similarity judgements, since contextualizing low-similarity landmarks often yields non-sensical phrases (e.g. system visits criterion). We provide scores for both contextualized and non-contextualized landmarks.

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A parsed version of the corpus is available, which has been parsed with MaltParser (Nivre et al., 2006). We use this version in order to extract our \( svo \) triples. From these triples, we construct our tensor \( \mathbf{X} \), using 1K verbs \( \times 10K \) subjects \( \times 10K \) objects. Note once again that the subject and object instances in the second step are exactly the same as the noun instances in the first step. Tensor \( \mathbf{X} \) has been weighted using a three-way extension of PMI, following equation 10 (Van de Cruys, 2011).

\[
\text{pmi}^3(x,y,z) = \log \frac{p(x,y,z)}{p(x)p(y)p(z)}
\]

We set \( K = 300 \) as our number of latent factors. The value was chosen as a trade-off between a model that is both rich enough, and does not require an excessive amount of memory (for the modeling of the core tensor). The algorithm runs fairly efficiently. Each NMF step is computed in a matter of seconds, with convergence after 50-100 iterations. The construction of the core tensor is somewhat more

7: We use a context window of 5 words, both before and after the target word; a stop list was used to filter out grammatical function words.
evolved, but does not exceed a wall time of 30 minutes. Results have been computed on a machine with Intel Xeon 2.93Ghz CPU and 32GB of RAM.

5.3 Results

The results of the various models are presented in table 5; multiplicative represents Mitchell and Lapata’s (2008) multiplicative model, categorical represents Grefenstette and Sadrzadeh’s (2011b) model, and latent represents the model presented in this paper.

<table>
<thead>
<tr>
<th>Model</th>
<th>Contextualized</th>
<th>Non-Contextualized</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>.23</td>
<td></td>
</tr>
<tr>
<td>Multiplicative</td>
<td>.32</td>
<td>.34</td>
</tr>
<tr>
<td>Categorical</td>
<td>.32</td>
<td>.35</td>
</tr>
<tr>
<td>Latent</td>
<td>.32</td>
<td>.37</td>
</tr>
<tr>
<td>Upper Bound</td>
<td>.62</td>
<td></td>
</tr>
</tbody>
</table>

Table 5: Results of the different compositionality models on the phrase similarity task

In our experience, PMI performs better than weighting with conditional probabilities.9

6 Conclusion

In this paper, we presented a novel method for the computation of compositionality within a distributional framework. The key idea is that compositionality is modeled as a multi-way interaction between latent factors, which are automatically constructed from corpus data. We used our method to model the composition of subject verb object combinations. The method consists of two steps. First, we compute a latent factor model for nouns from standard co-occurrence data. Next, the latent factors are used to induce a latent model of three-way subject verb object interactions, represented by a core tensor. Our model has been evaluated on a similarity task for transitive phrases, in which it matches and even exceeds the state of the art.

We conclude with a number of future work issues. First of all, we would like to extend our framework in order to incorporate more compositional phenomena. Our current model is designed to deal with the latent modeling of subject verb object combinations. We would like to investigate how other compositional phenomena might fit within our latent interaction framework, and how our model is able to tackle the computation of compositionality across a differing number of modes.

Secondly, we would like to further explore the possibilities of our model in which all three modes are represented by latent factors. The instantiation of our model presented in this paper has two latent modes, using the original instances of the verb mode in order to efficiently compute verb similarity. We think a full-blown latent interaction model might prove to have interesting applications in a number of NLP tasks, such as the paraphrasing of compositional expressions.

Finally, we would like to test our method using a number of different evaluation frameworks. We think tasks of similarity judgement have their merits, but in a way are also somewhat limited. In our opinion, research on the modeling of compositional phenomena within a distributional framework would substantially

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9 Contrary to the findings of Mitchell and Lapata (2008), who report a high correlation with human similarity judgements.
benefit from new evaluation frameworks. In particular, we think of a lexical substitution or paraphrasing task along the lines of McCarthy andNavigli (2009), but specifically aimed at the assessment of compositional phenomena.

References


