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The use of Ansys to calculate sandwich structures

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Abstract

In this article, we make a comparative study on a simply supported sandwich beam subjected to a uniform pressure using different modellings offered by the software Ansys 5.3 to compute displacements and stresses.

8 nodes quadrilateral elements Plane 82, multi-layered 8 nodes quadrilateral shell element Shell 91 and multi-layered 20 nodes cubic element Solid 46 are used. Influence of mesh refinement and of ratio of young's moduli of layers are studied.

Finally, a local Reissner method is presented and assessed, which permits to improve the accuracy of interface stresses for high ratio of young's moduli of layers using Plane 82 elements.

Key words: Ansys, sandwich structure, interface stresses, local Reissner method, post-processing

1 Introduction

Sandwich materials really begin to be highly appreciated in the industry, and especially in the field of transport (automotive, aeronautics, shipbuilding and railroads) or in civil engineering.

It is therefore important to determine which elements should be used to model such structures.

A sandwich structure is composed of three layers:

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- two edges made of rigid layers, working in membrane, which represent the skins;
- a thick and soft central layer, the core, with low rigidity and density and essentially submitted to transverse shear loading, is sandwiched in between the edges.

In the design process, interface stresses can be of great importance, since they play a crucial role in failure modes, as explained in [1,2].

The core being essentially subjected to transverse shear stress, this component, which is generally very much lower than the others, must not be neglected: in some cases, effects arising from shear effects overhang others phenomena (flexural effects for example), as shown for example in [3–6].

The determination of transverse shear stress at interfaces is therefore of particular importance in the design of new optimized materials.

If we assume that the three layers remain perfectly bonded, then at interfaces:

- the displacement field must be continuous;
- the normal trace of the stress must be continuous.

In this article, we shall study a very simple case using the famous finite element software Ansys 5.3. We shall not talk about special elements based on hybrid [7,8], mixed [9–12] or modified [13–15] formulation nor about pre- and postprocessing methods [16,17].

Solutions obtained with different modellings (complex or simple ones) are compared. Particular emphasis is put on their respect of continuity requirements.

By modifying the stiffness of the core, we shall see which modelling should be preferred by designers.

Finally a method, based on Reissner's formulation, is developed to improve the accuracy for new sandwiches.

2 Description of the study

One of the most simple example is the case of the simply supported sandwich beam subjected to an uniform pressure on its top face. This beam is shown in figure 1.

2.1 Characteristics

The geometry is defined as follows:

- The total length of the beam is $L = 24$ mm;
- its total height $H = 2$ mm, the core representing 80% of the total height of this symmetrical sandwich, each skin is 0.2 mm height;
- the thickness of the beam is equal to unity.

The applied pressure is $q = -1$ N/mm.

2.2 Parameters of the study

In this study, we are interested in determining the structural response at point A (at the interface between the top skin and the core and located at $x_1 = L/4$) when different parameters vary.

Skins are made of aluminum ($E_s = 70000$ MPa and $\nu_p = 0.34$). The core will be:

- Case A: of carbon/epoxy $(E_c = 3400 \text{ Mpa} \text{ and } \nu_c = 0.34);$
- Case B: of foam $(E_c = 340 \text{ Mpa}$ and $\nu_c = 0.40)$;
- Case C: of soft foam $(E_c = 70$ Mpa and $\nu_c = 0.40)$;
- Case D: other material: $\nu_c = 0.4$ is fixed and E_s/E_c varies.

2.3 The modellings

By symmetry, only one half of the beam is modelled.

Before building the different modellings, we define the following parameters for the meshing:

- *ncuts*: number of longitudinal cuts (in the beam's axis direction);
- *nskin*: number of elements in the thickness of each skin;
- *ncore*: number of elements in the thickness of the core.

We shall use the following modellings:

- the reference modelling:
	- · 2D using the 8 nodes quadrilateral element Plane 82;
	- \cdot 4 elements through the thickness of each skin $(nskin = 4)$, 32 through the thickness of the core (*ncore* = 32), and 400 longitudinal cuts (*ncuts* = 400) in the beam's axis directions (16000 elements for the half beam); This fine meshing yields to the exact solution given by [18].
- a planar modelling using the plane element Plane 82:
	- 1 element is used to model each layers (nskin $=$ ncore $=$ 1), i.e. 3 elements through the thickness of the sandwich;
- a modelling using the multi-layered cubic element Solid 46:

1 element through the total thickness representing all the layers of the sandwich structure;

• one modelling done with the multi-layered shell element Shell 91, with sandwich option (keyopt $(9)=1$):

1 element through the total thickness representing all the layers of the sandwich structure.

2.4 Results of interest

In our studies, we shall focus on the following results of particular interest:

- the maximum displacement of the structure in z direction, denoted U_z in results;
- the discontinuous components of stresses, σ_{xx} , at point A in the skin and in the core, and the continuous component σ_{zz} ;
- interlaminar stress: this is the continuous component σ_{xz} at point A.

3 Study of the sandwich beam

We now present results obtained with Ansys 5.3 and corresponding to different materials and different meshes.

3.1 Influence of ncuts on the different modellings

In this section, we are interested in the structural responses to the different modellings for $E_c = 3400 \text{ MPa}$, $E_c = 340 \text{ MPa}$ and $E_c = 70 \text{ MPa}$.

Results concerning the case $E_c = 340$ MPa are plotted in figures 2 for displacements, 3 and 4 for the two continuous components σ_{zz} and σ_{xz} and 5 and 6 for σ_{xx} in the core and in the skin respectively.

Tables 1, 2 and 3 present numerical results and error percentages after convergence for these 3 cases.

From these figures and tables, the following conclusions can be drawn:

- Plane 82 is very much better than others modellings. Nevertheless, it is to be noticed that it seems to diverge for displacements (with the coarse mesh used: $nskin = ncore = 1);$
- Solid 46 is the worst model. It never converges towards the right values (for any component of stresses nor for displacements);
- Shell 91 is particularly interesting for continuous components of stresses σ_{zz} and σ_{xz} ;
- Plane 82 is the only modelling leading to a correct determination of the discontinuous component σ_{xx} in the skin and the core;
- It seems that errors increase with the ratio E_s/E_c . This point will be studied in the next section.

3.2 Influence of ratio E_s/E_c for ncuts=20

Since every material which can be obtained in a thin skin shape is acceptable for the skins and every material with low density is acceptable for the core, sandwich materials cover an extremely wide domain.

A parameter of interest is therefore the ratio of young's moduli E_s/E_c . This parameter can vary from 4 (old sandwiches, so to speak, very close to laminates) to 1000 (some new high-tech sandwiches developed for very particular applications go up to 1500). But we must remark that sandwiches often exhibit a ratio greater than 200.

In this section we shall study the influence of this ratio on the different modellings when the utilized mesh is fixed to $ncuts = 20$.

Results concerning displacements are plotted in figure 7. Continuous components σ_{zz} and σ_{xz} are shown in figures 8 and 9. The discontinuous component σ_{xx} is illustrated in figures 10 and 11 in the core and in the skin respectively.

From these figures, the following conclusions can be drawn:

- Plane 82 is the best modelling for displacements, σ_{zz} and σ_{xx} in the core and the skin;
- Shell 91 and Solid 46 are acceptable for displacements and σ_{xx} in the core. They are acceptable for σ_{xx} in the skin for $E_s/E_c \leq 50$;
- Shell 91 leads to an acceptable approximation of σ_{zz} , and is very interesting for σ_{xz} ;
- Plane 82, which was exceptionally good in the last section, shows some difficulty here, especially at high E_s/E_c ratio for σ_{xz} . The influence of the meshing of the beam with Plane 82 elements is studied in the next section.

3.3 Element Plane 82: influence of mesh refinement

In previous sections, the mesh corresponding to the 8 nodes quadrilateral element Plane 82 only used 1 element to model 1 layer.

We propose to see what happens when the number of elements through the thickness of the skins (nskin) and of the core (ncore) vary.

Displacements are plotted in figure 12, σ_{zz} and σ_{xz} in figures 13 and 14, and σ_{xx} in figures 15 and 16 in the core and in the skin respectively. These computations are done for a ratio $E_s/E_c = 500$.

From these figures, the following conclusions can be drawn:

- results are always accurate when $ncore = 8$ nskin, i.e. when the meshing is regular through the thickness;
- *nskin* and *ncore* do not have any influence on the convergence of displacements, essentially due to flexion: the number of longitudinal cuts, ncuts, is therefore the most preponderant parameter.
- a very refined mesh $(nskin = 4$ and $ncore = 8$ nskin) must be used in order to converge towards the right value of σ_{zz} ;
- a coarse mesh $(nskin = 1)$ does not permit to obtain an acceptable value of σ_{xz} ;
- convergence towards σ_{xx} reference value in the core is controlled by ncuts. Results are not improved by increasing nskin nor ncore;
- the last point is also true for the convergence towards σ_{xx} value in the skin.

4 Local Reissner: improving results for Plane 82

As it can be see from figure 9 and from table 4 (which summaries results and gives the good "working zone" of the different modellings), Plane 82 is not able to give accurately the interlaminar stress σ_{xz} with a coarse mesh. Since this component is very important in the design process, results must be improved.

A way of improving results is to refine the meshing. In figure 9, the curve 'Plane $82/2$ ' gives results obtained with $nskin = 1$ and $ncore = 2$ (instead of 1). This slightest modification of the mesh (4 elements through the thickness of the sandwich instead of 3) is sufficient to lead to very good results for $E_s/E_c \leq 200$.

But, as mentioned before, sandwiches nowadays exhibit ratios generally higher than 200. In this range, the convergence is only reached with a very refined meshing: $nskin \geq 3$ and $ncore = 8$ nskin. Such a mesh yields an unacceptable computation time.

In order to improve the accuracy of stresses, we must answer to the following question: how are nodal stresses computed?

Nodal stresses τ are generally computed using a minimization process. They are obtained from nodal displacements q using a least squares method and by minimizing:

$$
\int_{\Omega} \left(\boldsymbol{\sigma_m} - \boldsymbol{\sigma_u} \right)^2 \, \mathrm{d}\Omega \tag{1}
$$

where σ_m denotes the mixed way to calculate stresses:

$$
\sigma_m = N_{\sigma} \tau \tag{2}
$$

and σ_u the displacements way:

$$
\sigma_u = D\mathcal{L}N_u q \tag{3}
$$

or using the stress projection method presented in [19] by minimizing:

$$
\int_{\Omega} \left(\boldsymbol{\sigma}_{m} - \boldsymbol{\sigma}_{u} \right) \, \mathrm{d}\Omega \tag{4}
$$

In these equations, \boldsymbol{D} is the generalized Hooke's matrix relating stresses to strains, $\mathcal L$ the differential operator relating strains to displacements, N_{σ} and N_u the matrices of shapes functions for stresses and displacements, and Ω the volume or surface of interest.

It is to be noticed that these methods lead to convergence towards Reissner's (reference) solution.

As expressed in [20], the minimization process can be global (done over the whole structure: Ω being the entire structure) or local (done over one element: Ω being the considered element). Since the local process converges towards the same limit as the global process, the minimization process chosen is generally the local one.

Nevertheless, instead of minimizing the difference between two solutions, it may be more convenient (simpler and faster) to directly find the stress field using Reissner's formulation.

In Reissner's solution, nodal stresses are related to nodal displacements by [21–24]:

$$
\boldsymbol{\tau} = \boldsymbol{A}^{-1} \boldsymbol{B} \boldsymbol{q} \tag{5}
$$

with:

$$
\mathbf{A} = +\int_{\Omega} {}^{t} \mathbf{N}_{\sigma} \mathbf{S} \mathbf{N}_{\sigma} \, d\Omega \tag{6}
$$

and

$$
\boldsymbol{B} = +\int_{\Omega} {}^{t} \boldsymbol{N}_{\sigma} \mathcal{L} \boldsymbol{N}_{u} \ d\Omega \tag{7}
$$

 $S = D^{-1}$ being the compliance matrix.

In order to improve the stress computation at interfaces, we propose to use the last formulation on two adjacent elements, located on each side of an interface. Doing so, we ensure the equilibrium state at interface on a better way. We shall refer to this method as "local Reissner" method.

This kind of method is not more time consuming than least squares methods generally used (in Ansys for example) to derive nodal stresses from nodal displacements.

Now looking at figure 17, which is a close-up view of figure 9 for sandwiches with $E_s/E_c \geq 200$, we can see that:

- the use of local Reissner's method (denoted Local Reissner/2 because we used ncore = 2) permits to really improve the accuracy of σ_{xz} , which is of great importance.
- It is to be noticed that the same mesh with Plane 82 (Plane 82/2) does not permit to improve results with this high E_s/E_c ratio.
- The solution given by Shell 91 is not so good as for lower E_s/E_c ratio.

5 Conclusions

The reference solution has been obtained using a very fine meshing and the 8 node quadrilateral element Plane 82 in order to reach the analytical solution of Pagano [18].

The first study, influence of *ncuts* on the different modelling in section 3.1, seems to lead to the conclusion that Plane 82 is the best model, specially when looking at figures 2-6 (obtained with a coarse mesh and in the case $E_s/E_c \approx 200$). Nevertheless, the study of the influence of the E_s/E_c ratio in section 3.2 permits to see some weakness of this model.

In terms for design quantities:

- all models leads to a correct value of displacements, but Plane 82 is the most accurate;
- σ_{zz} can be correctly given by Shell 91 and Plane 82, the latest being the most accurate;
- σ_{xz} is only very accurately computed with Shell 91, but for $E_s/E_c \leq 200$;
- σ_{xx} in the core can be calculated using any model, Plane 82 being the most accurate;
- σ_{xx} in the skin is very accurately computed with Plane 82 and with Shell 91 (but only for $E_s/E_c \leq 20$), and acceptable with Solid 46 (and only for $E_s/E_c \leq 20$.

A summary of results, and the "working zone" in which the different elements can be used is given in table 4.

Hence, from the previous results, we can say that:

- for planar problems, Plane 82 is very well adapted. Nevertheless, it is to be noticed that this method is not very stable for very coarse meshes (small values of nskin, ncore and ncuts), and that interlaminar stress σ_{xz} can only be reached with a fine meshing;
- Shell 91 (with sandwich option) is a good way of computing sandwich structures. Nevertheless if the designer must know σ_{xx} at interfaces, then this element can only be used for $E_s/E_c \leq 50$.
- Solid 46 is not very accurate in the determination of the design quantities. A model using this kind of element should be avoided. Nevertheless, it is to be noticed that this element has not been developed to perform such computations (high differentce of stiffness between layers).

The presented local Reissner's method permits to reach excellent results, especially for the interlaminar stress σ_{xz} and for $E_s/E_c \geq 200$ with a coarse mesh through the thickness of the sandwih. We can notice that such a meshing, with 4 elements through the thickness of the sandwich yields results very closed to the exact solution obtained with 40 elements through the thickness!

This method is particularly interesting for the design of new sandwich materials.

Finally, we want to put emphasis on the fact that this method is particularly easy to implement, as a stand-alone program, but also in existing finite element softwares.

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Fig. 3. Influence of $\mathit{ncuts}\colon\sigma_{zz}$ (case B)

Fig. 4. Influence of *ncuts*: σ_{xz} (case B)

Fig. 5. Influence of *ncuts*: σ_{xx} in the core (case B)

Fig. 6. Influence of *ncuts*: σ_{xx} in the top skin (case B)

Fig. 7. Influence of E_s/E_c : U_z (ncuts = 20)

Fig. 8. Influence of E_s/E_c : σ_{zz} (ncuts = 20)

Fig. 9. Influence of E_s/E_c : σ_{xz} (ncuts = 20)

Fig. 10. Influence of E_s/E_c : σ_{xx} in the core (ncuts = 20)

Fig. 11. Influence of E_s/E_c : σ_{xx} in the top skin (ncuts = 20)

Fig. 12. Influence of *nskin* and *ncore*: U_z (*ncuts* = 20 and $E_s/E_c = 500$)

Fig. 13. Influence of *nskin* and *ncore*: σ_{zz} (*ncuts* = 20 and $E_s/E_c = 500$)

Fig. 14. Influence of *nskin* and *ncore*: σ_{xz} (*ncuts* = 20 and $E_s/E_c = 500$)

Fig. 15. Influence of *nskin* and *ncore*: σ_{xx} in the core (*ncuts* = 20 and $E_s/E_c = 500$)

Fig. 16. Influence of *nskin* and *ncore*: σ_{xx} in the top skin (*ncuts* = 20 and $E_s/E_c = 500)$

Fig. 17. Influence of high E_s/E_c ratio: σ_{xz} (ncuts = 20)

Table 1 Case A: $E_c = 3400$ Mpa

		$ U_z $ $ \sigma_{zz} $ $ \sigma_{xz} $ $ \sigma_{xx} $		skin	$ \sigma_{xx} $ core	ncuts
Ref		0.21596 0.94624	3.1635	123.13	6.2844	
P82	0.21527	0.95033 3.2616		123.08	6.2843	400
		0.319% 0.432% 3.10% 0.04% 0.001%				
S91	0.21388	0.90000		3.1587 126.35	6.1369	1000
		0.963% 4.887\%	0.15% 2.61%		2.35%	
S46	0.20355	0.50000	3.0000	123.28	8.4202	1000
		5.746% 47.16% 5.17% 0.12%			34.0\%	

Table 2

Case B: $E_c = 340$ Mpa

$ \sigma_{zz} $ $ \sigma_{xz} $ $ U_z $ $ \sigma_{xx} $ $ \sigma_{xx} $ skin core 0.51353 0.95461 103.71 Ref 3.2956 0.8262 0.52618 0.96321 102.38 0.8701 P82 3.3091 0.901% 1.28\% 5.31% 2.463\% 0.41% 0.90000 3.3024 132.09 S91 0.55712 0.6599 0.22% 27.4% 5.721% 20.1% 8.488\%				
				ncuts
				400
				1000
S46 0.45994 3.0000 0.50000 130.68 1.2042				1000
10.44% 47.62% 8.97% -26.0% 45.7%				

Table 3 Case C: $E_c = 70$ Mpa

		$ U_z $ $ \sigma_{zz} $ $ \sigma_{xz} $ $ \sigma_{xx} $ $ \sigma_{xx} $ neuts		skin core	
		Ref 1.740 0.96121 3.2926 20.43 0.3614			
		P82 1.741 0.96847 3.1561 20.77 0.3301 400			
		0.06% 0.755% 4.15% 1.66% 8.66%			
S91		1.987 0.90000 3.3161 132.64 0.1364			1000
		14.2% 6.368\% 0.71\% 549\% 62.2\%			
S46	1.506	0.50000 3.0000 131.43 0.4802			1000
		13.4% 47.98% 8.89% 543% 32.9%			

Table 4 Accuracy of results (ncuts ≥ 20 understood)

	U_z	σ_{zz}	σ_{xz}	σ_{xx} core	σ_{xx} skin		
P82	always good	always good	acceptable for $E_s/E_c \in$ [100, 400]	always good	always good		
	improvement of results						
	– use a fine meshing: $nskin \geq 3$ and $ncore = 8$ $nskin$						
	– use local Reissner's method						
S91	always $ac-$ ceptable	always $ac-$ ceptable	always good	for good $E_s/E_c \leq 100$	good for $E_s/E_c \leq 20$		
S ₄₆	always $ac-$ ceptable	never accept- able	acceptable for $E_s/E_c \in$ [8, 15]	always weak	acceptable for $E_s/E_c \leq 20$		