

# Evolution of geomagnetic *aa* index near sunspot minimum

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**Abstract.** The smoothed values of the minima of sunspot number  $R_z$  and the geomagnetic index  $aa$  were compared for sunspot cycles 12–23. In one cycle,  $aa(\min)$  occurred earlier than  $R_z(\min)$ , but remained at that low from a few months before  $R_z(\min)$  to a few months after  $R_z(\min)$ . In two cycles,  $R_z(\min)$  and  $aa(\min)$  coincided within a month or two. In nine cycles,  $aa(\min)$  occurred more than three months later than  $R_z(\min)$ . The  $aa(\min)$  coincided with the minima of some solar radio emission indices originating in the solar corona. For sunspot cycles 21, 22, 23, the minimum of solar wind velocity  $V$  occurred 0–9 months later than the  $aa(\min)$ . The minimum of solar wind total magnetic field  $B$  occurred near  $R_z(\min)$ . The solar wind ion density  $N$  had maxima (instead of minima) near  $R_z(\min)$ , and again near  $R_z(\max)$ , indicating a  $\sim 5$ -year periodicity, instead of an 11-year periodicity. The maxima of  $aa$ ,  $V$  and  $B$  occurred near  $R_z(\max)$  and/or later in the declining phase of  $R_z$ . The  $aa$  index was very well correlated with the functions  $BV$  and  $BV^2$ .

**Key words.** Geomagnetism and paleomagnetism (time variations, diurnal to secular – time variations, secular and long term) Interplanetary physics (interplanetary magnetic field)

## 1 Introduction

The geomagnetic index  $aa$  has proved very useful for prediction of maxima of smoothed sunspot numbers. For example, using the precursor methods (Ohl, 1966; Brown and Williams, 1969), where the precursor is the geomagnetic activity in the declining phase of the previous cycle, reasonably good predictions could be made for solar cycles 20 (1964–1975), 21 (1976–1985), and 22 (1986–1995) (Ohl, 1966, 1976; Ohl and Ohl, 1979; Sargent, 1978; Kane, 1978, 1987; Wilson, 1988, 1990). A review of the observed and predicted values of the maximum sunspot number for cycle 22 was made by Kane (1992). For solar cycle 23, many predictions were made. The cycle 23 started in 1996 and seems to have already peaked in 2000, with a maximum smoothed sunspot number of  $\sim 122$ .

In the precursor method, the smoothed value  $aa(\min)$  is used in a regression equation. This value occurs generally near the smoothed sunspot  $R_z(\min)$ . However, the exact month when  $aa(\min)$  occurs is not important. The correlation between the smoothed values (12-month moving averages) of  $aa(\min)$  and the succeeding smoothed sunspot number  $R_z(\max)$  is very high ( $\sim +0.95$ ), no matter when the  $aa(\min)$  occurred. However, it is noticed that the months of  $aa(\min)$  and  $R_z(\min)$  do not always coincide. In the present communication, it has been investigated whether the month of  $aa(\min)$  coincides with the month of minimum of any other solar index, if not with  $R_z(\min)$ .

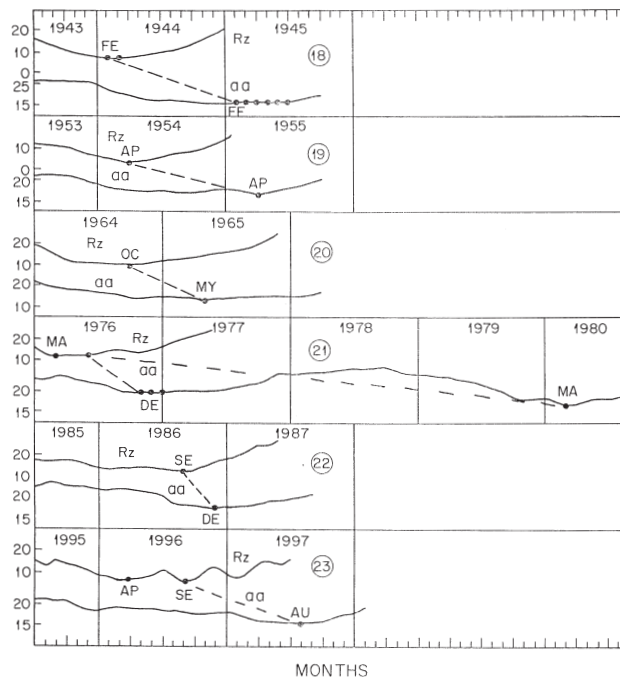
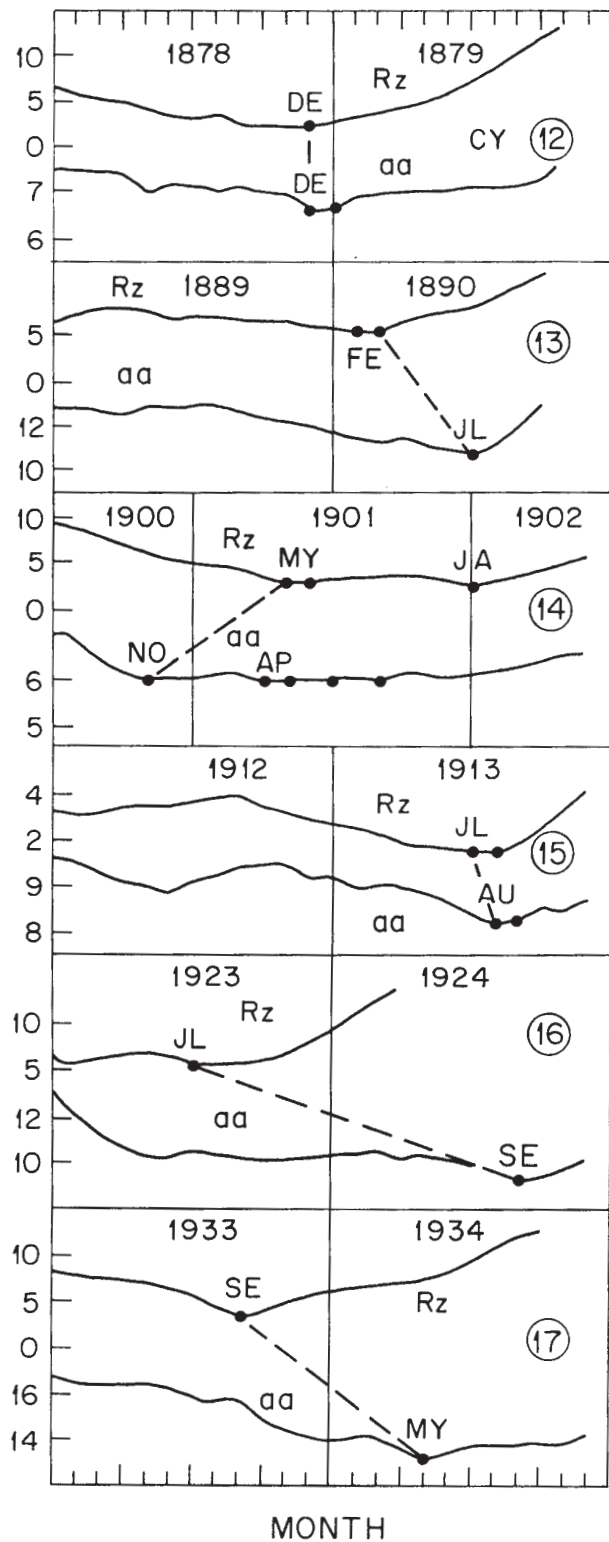
## 2 Data

All the data were obtained from the NOAA websites [ftp://ftp.ngdc.noaa.gov/STP/SOLAR/\\_DATA/](ftp://ftp.ngdc.noaa.gov/STP/SOLAR/_DATA/) and <http://www.ngdc.noaa.gov/stp/>, but some were obtained from other websites given by the various authors. The sunspot numbers used are the Wolf (Zürich) sunspot number  $R_z$ , available since 1700 and published by Wolf in the various issues of *Astron. Mitt.* (1858–1893) (also in Waldmeir, 1961; McKinnon, 1987), presently generated by the Solar Index Data Center, Brussels. The  $aa$  index data are originally from Mayaud (1973). Many data appear in the Solar Geophysical Data (SGD) Reports of NOAA. The data were available as monthly means, or daily values, from which monthly values were calculated. Furthermore, smoothed values (12-month moving averages) were calculated and used. Thus, short-term variations, such as a 27-day variation, are obliterated and only intermediate-term variations are studied.

## 3 Plots

### 3.1 Plots of $R_z$ and $aa$ indices in cycles 12–23

The  $aa$  index data are available from 1868 (cycle 12) onward (the cycles are numbered since 1750, cycle 1 = 1755 minimum to 1766 minimum). Figure 1a shows the plots of smoothed sunspot numbers  $R_z$  and smoothed  $aa$  for sunspot cycles 12–17 and Fig. 1b for cycles 18–23. The months of minima (JA, FE, MA, AP, MY, JN, JL, AU, SE, OC, NO,



**Fig. 1.** Plots of the 12-month moving averages of sunspot number  $Rz$  and geomagnetic index  $aa$  during years of minima of sunspot cycles, (a) cycles 12–17, (b) cycles 18–23. The dashed line connects  $Rz(\min)$  to  $aa(\min)$ .

DE) are indicated and the minima of  $Rz$  and  $aa$  are connected by a dashed line. In cycle 14,  $aa(\min)$  occurred in November 1900, several months before  $Rz(\min)$ , which oc-

curred in May 1901. However, the  $aa$  values were almost flat for several months, so that the  $aa(\min)$  could be considered as during November 1900 – September 1901. In cycles 12

and 15, the minima of *aa* and *Rz* were almost coincident. In the other nine cycles, *aa*(min) occurred three or more months later than *Rz*(min). A very unusual thing occurred in cycle 21 when *aa* had two minima, one in November 1976 (five months after the *Rz*(min) of June 1976), and another several years later, in March 1980.

Regarding sunspot minimum for cycles 22–23, Harvey and White (1999) made an interesting investigation. They concluded that cycle minimum is not defined solely on the basis of the occurrence of the minimum in the smoothed sunspot number, but rather by several additional parameters, including the monthly (or rotationally) averaged sunspot number, the number of regions (total, new- and old-cycle), and the number of spotless days, and they recommended that minimum between cycles 22 and 23 should be considered as having occurred in September 1996 and not in May 1996. In Fig. 1b, we have considered the sunspot minimum to be in April 1996, as well as in September 1996. (The discrepancy of whether or not sunspot minimum should be in April or May 1996 is appearing due to the consideration of centering. We have considered 12-month moving averages as centered on the sixth month, e.g. January to December mean centered at June. Others may consider it as at July. The double-smoothed means, as given in McKinnon, 1987, will be centered at July). The smoothed sunspot numbers had a minimum value of 7.6 in April 1996, but then followed a flat minimum until September 1996, when the value was only 8.4, almost the same as for April 1996.

### 3.2 Plots of months of minima for several indices in cycles 18–23

Among solar indices, sunspot number data are available for more than three centuries, but other indices are of recent origin. The Calcium plage areas are available since 1915 (cycle 15), the coronal green line emission index since 1939 (cycle 17), and the 10.7 cm 2800 MHz flux (called F10) since 1947. Figure 2 shows the months when the minima of the smoothed values of various indices occurred during cycles (A) 18, (B) 19, (C) 20, (D) 21, (E) 22, (F) 23. In each frame, the bottom plot is of smoothed *Rz* values and the next plot above it is of smoothed *aa* values. The minima are indicated by full dots. If values adjacent to the minima are within 5%, these are also shown by dots. Only the months of minima of the smoothed values are indicated by dots. The month of *aa*(min) is shown by a bigger dot, for easy comparison with months of minima of other indices.

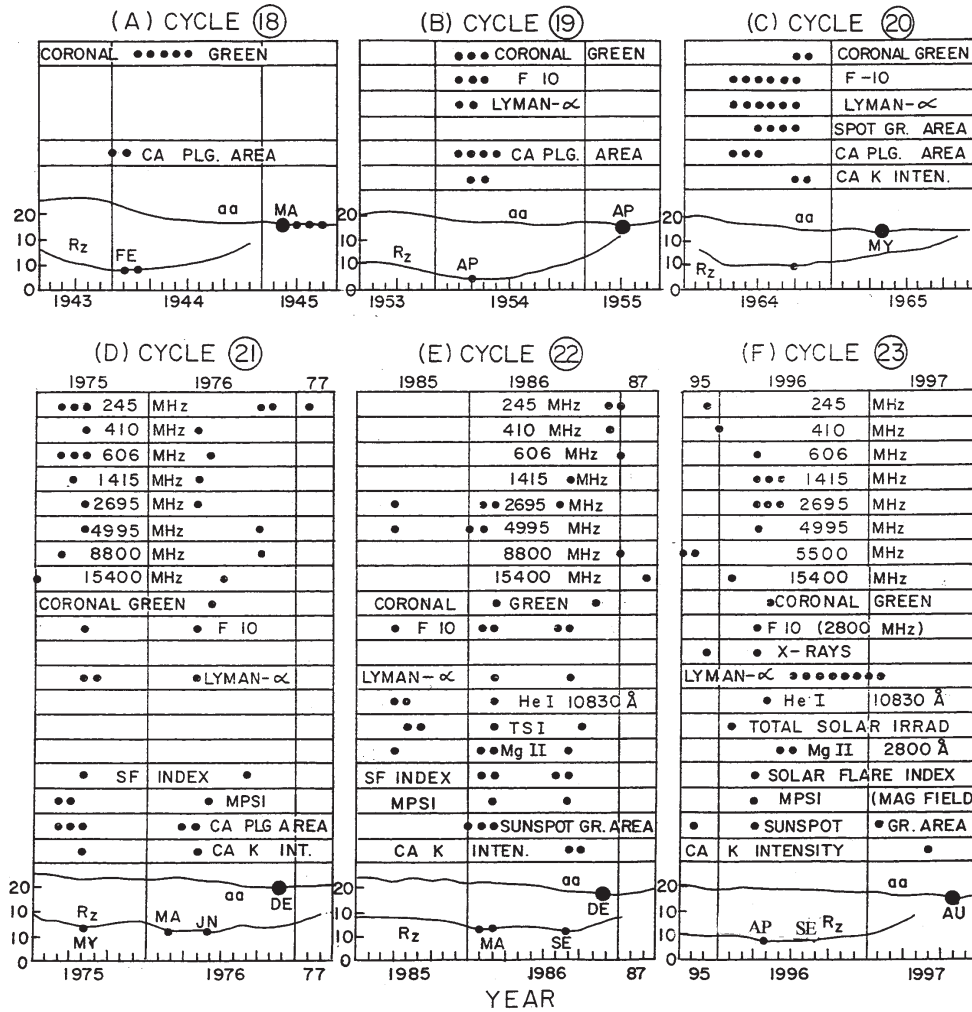
- Cycle 18: The months of minima of *Rz*, Calcium plage area and Coronal green line emission index were all in the first half of 1944, but the *aa*(min) was much later, in March 1945. Thus, *aa*(min) did not match with any of the other three solar indices (including *Rz*), and occurred much later.
- Cycle 19: Minima of six solar indices occurred in the first half of 1954, but *aa*(min) occurred almost a year later, in April 1955.

- Cycle 20: Minima of seven solar indices occurred in the latter half of 1964, but *aa*(min) occurred a few months later, in April 1965.
- Cycle 21: Here, *Rz* had a minor minimum in May 1975 and many solar indices (more than a dozen) had minima in nearby months. Major minima of *Rz* were in March–June 1976 and minima of many solar indices occurred in this interval as well. In contrast, *aa*(min) occurred much later, in December 1976. The solar indices with minima nearest to this month were the coronal 245, 4995 and 8800 MHz solar radio emissions, and the solar flare index. Thus, some relationship with solar corona was indicated. Incidentally, the *aa* index had another minimum several years later, in March 1980 (discussed further).
- Cycle 22: Here, *Rz* had minima in February–March and September 1986 and many solar indices had similar minima. The *aa*(min) occurred later in December 1986, when some coronal indices had minima, again indicating a coronal connection.
- Cycle 23: This cycle is not yet complete (only halfway through). The *Rz* had a minimum (7.6) in April 1996, but the values remained low until September 1996 (8.4). Many other solar indices had minima near April 1996. The *aa*(min) occurred much later, in August 1997, and no other solar index had a minimum anywhere near it, except Calcium K line intensity (June 1997). Thus, there was no coronal connection in this cycle.

Thus, the *aa*(min) was always later than *Rz*(min) in cycles 18–23, and a few solar radio emissions accompanied the *aa*(min).

## 4 Relationship with solar wind parameters

Geomagnetic indices are basically related to the Earth, though a possible relationship with solar phenomena was suspected long ago. Chapman and Bartels (1940) observed that geomagnetic activity often increased several hours after some solar events and speculated that solar corpuscular emissions from M regions were responsible for these increases. Chapman firmly believed that the solar atmosphere was basically static, like the Earth's atmosphere, only much more extensive, with the upper corona sometimes extending right up to the Earth. Parker (1958, 1963) noticed that the solar atmosphere was not only not static, but was highly dynamic and the Sun was emitting corpuscular radiation (solar wind) all the time, much more so during solar events. The solar wind occupied the interplanetary space and Interplanetary Magnetic Fields (IMF) were formed. A southward component (*Bz*) of IMF was particularly effective in causing a reconnection with the geomagnetic field through the magnetotail, resulting in increased geomagnetic activity. The present view is that around solar maximum, the dominant interplanetary phenomena causing intense magnetic storms are



**Fig. 2.** Plots of the 12-month moving averages of  $R_z$  and  $aa$  during years of sunspot minima of (A) cycle 18, 1943–1945, (B) cycle 19, 1953–1955, (C) cycle 20, 1964–1965, (D) cycle 21, 1975–1977, (E) cycle 22, 1985–1987, (F) cycle 23, 1995–1997. For other solar indices, only the months of minima are indicated by full dots. The  $aa(\min)$  is indicated by a bigger full dot.

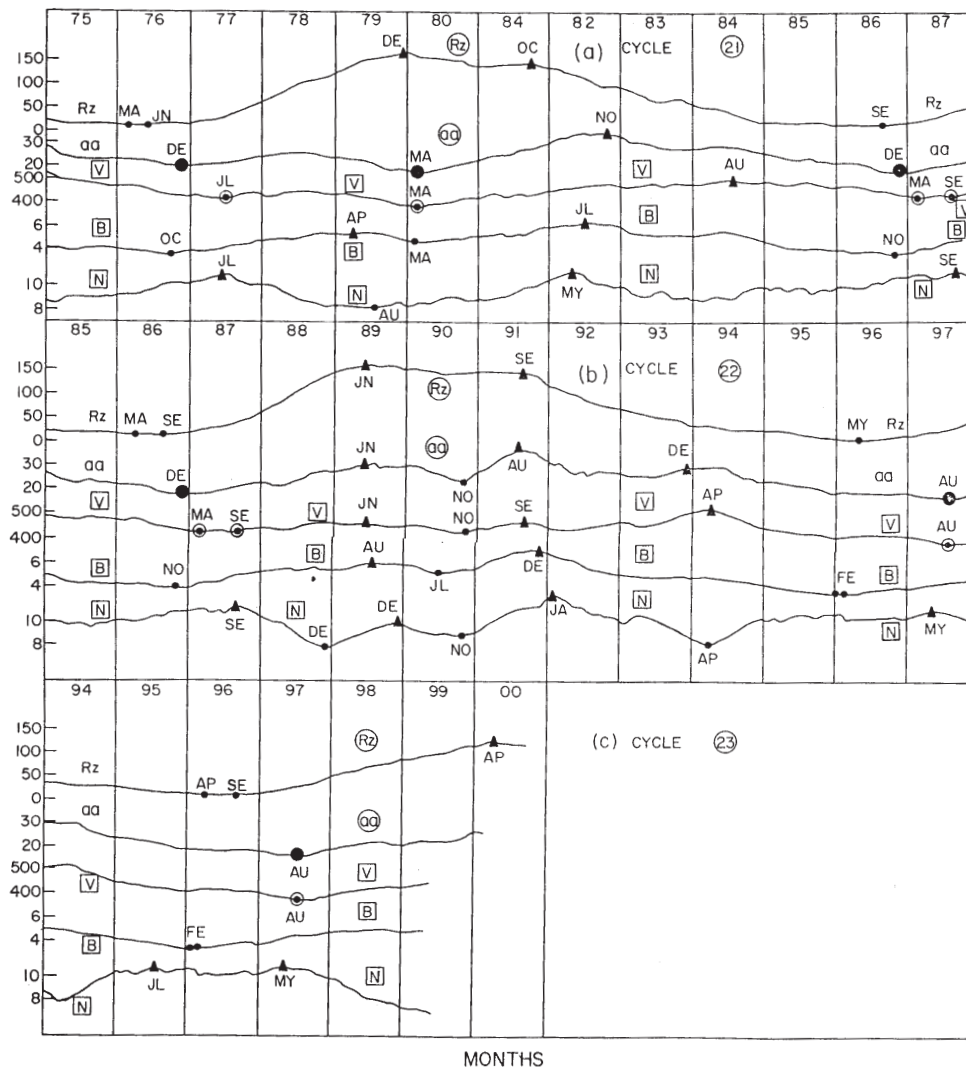
the interplanetary manifestations of fast coronal mass ejections (CMEs; Gonzalez et al., 1999). The parameters of solar wind for which data are available are (i) solar wind velocity  $V$ , (ii) ion density  $N$ , and (iii) magnetic field  $B$  (components  $B_x$ ,  $B_y$ ,  $B_z$ ). The data set is a composite of multispacecraft observations obtained over different time periods, beginning with 27 November 1963 (details in King, 1976), but the coverage is very uneven in the early years. Here, only data for cycles 21–23 (1975 onward) are used. Daily values are often intermittent, but monthly values may be reliable. Moving averages over 12 months should be fairly reliable, though the effects of individual events lasting for a few days are obliterated and only intermediate-time scale effects would be seen.

#### 4.1 Plots for cycles 21, 22, 23

Figure 3 shows a plot of smoothed monthly values of  $R_z$ ,  $aa$  index, and solar wind parameters  $V$ ,  $B$ ,  $N$ , for (a) cycle 21, (b) cycle 22, and (c) cycle 23. For each cycle, data for thir-

teen years are plotted so that two minima and one maximum of  $R_z$  are seen in the same plot. The phase relationship of  $R_z(\min)$ ,  $aa(\min)$ , etc. was as follows:

- Cycle 21: The  $R_z(\min)$  occurred in March–June of 1976, while  $aa(\min)$  occurred a few months later, in December 1976 (big dot), almost coinciding with the October 1976 minima of some solar radio emissions (Fig. 2D). The total magnetic field  $B$  of solar wind had a minimum in October 1976, almost coinciding with  $aa(\min)$ , but the solar wind velocity  $V$  had a minimum much later, in July 1977 (big open circle). Thus, even though solar wind velocity  $V$  and  $aa$  index are reported to be highly correlated, their first minima did not occur simultaneously in the beginning of cycle 21. There was another minimum much later in March 1980, coincident for  $V(\min)$ ,  $aa(\min)$  and  $B(\min)$ , though the  $R_z$  had attained a maximum at this time. A curious feature was that the ion density  $N$  did not have a minimum in



**Fig. 3.** Plots of the 12-month moving averages of  $Rz$ ,  $aa$ , and solar wind parameters  $V$ ,  $B$ ,  $N$ , for (a) cycle 21 (1975–1987), (b) cycle 22 (1985–1997), (c) cycle 23 (1994–2000). The minima are indicated by full dots (big full dot for  $aa$ (min), open circle for  $V$ (min)) and maxima by full triangles.

1976–1977 at all. Instead, there was a maximum (triangle) in July 1977, though later, there was a minimum in August 1979. The maxima of  $aa$ ,  $V$ ,  $B$  and  $N$  for this cycle 21 occurred much later than the maximum of  $Rz$  (rather a flat maximum during December 1979 to October 1981), confirming that solar wind and geomagnetic activity strengthen during the declining phase of the sunspot cycle. However, the maxima of  $aa$  and  $V$  did not coincide and were several months apart, with  $V$ (max) occurring later.

followed by a minimum in December 1988.  $Rz$  had a flat maximum during June 1989 and September 1991. Let us term these as two maxima, one in June 1989 and another in September 1991, though there is no valley in between. The maxima of  $aa$ ,  $V$ ,  $B$  and  $N$  all occurred almost simultaneously, but there were two maxima in each, one coinciding with the first maximum of  $Rz$  (June 1989) and another with the second maximum of  $Rz$  (September 1991). However,  $aa$  and  $V$  had a third maximum in the end of 1993, in the declining phase of  $Rz$ .

– Cycle 22: Here,  $Rz$ (min) was in March–September 1986,  $aa$ (min) a few months later, in December 1986, and  $V$ (min) still later, in March–September, 1987. The  $B$ (min) was in November 1986, almost coinciding with  $aa$ (min). The ion density  $N$  did not have a minimum and instead, showed a maximum in September 1987,

– Cycle 23:  $Rz$ (min) was during April–September, 1996, while  $aa$ (min) was much later, in August 1997, and  $V$ (min) coincided with  $aa$ (min). The  $B$ (min) was much earlier, in February 1996, earlier than even  $Rz$ (min). Again, ion density  $N$  did not have a minimum at all;

instead, two maxima were seen, one in July 1996 and another in May 1997. The  $R_z(\text{max})$  occurred in April 2000 and there are no data available as of yet for the other indices.

Data for only three sunspot cycles are certainly not enough for drawing any statistical conclusions, but the following is noteworthy:

1. In cycles 21 and 22,  $R_z$  had a flat plateau at the maximum. Let us term the beginning of this plateau as the first maximum and the end of the plateau as the second maximum, though there is virtually no valley in between. In cycle 23, the  $R_z(\text{max})$  occurred only recently and further evolution is unknown.
2. The  $aa(\text{min})$  occurred later than  $R_z(\text{min})$  in all the three cycles, by 3–15 months. The  $aa$  had more than one maxima, one occurring coincident with  $R_z(\text{max})$  and others later, in the declining phase of  $R_z$ .
3. The  $V(\text{min})$  occurred 0–9 months later than  $aa(\text{min})$ , indicating that the geomagnetic activity lowered first. The  $V(\text{max})$  occurred coincident with  $aa(\text{max})$ , or later.
4. The  $B(\text{min})$  occurred earlier than  $aa(\text{min})$  and in cycle 23, earlier than even  $R_z(\text{min})$ , indicating that the magnetic field in solar wind weakened earliest. The  $B(\text{max})$  occurred within a few months of  $aa(\text{max})$ .
5.  $N$  had a very strange behavior.  $N(\text{max})$  occurred soon after  $R_z(\text{min})$  as well as soon after  $R_z(\text{max})$ . Thus, a 5-year (rather than an 11-year) cycle is indicated.

#### 4.2 Correlations

Soon after data for solar wind parameters were available, Snyder et al. (1963) reported a good correlation between solar wind velocity  $V$  and the geomagnetic index  $Ap$ . For individual magnetic storms lasting for a few to tens of hours, magnetic field reconnection between the southwardly directed IMF and the geomagnetic field is the most widely accepted mechanism for magnetospheric energization. Several coupling functions that correlate well between solar wind parameters and magnetospheric dissipation parameters are used and these can be derived as particular cases of general expressions for the momentum and energy transfer at the magnetopause due to large-scale reconnection (Gonzalez, 1990; Gonzalez et al., 1994). Possible interplanetary mechanisms for the creation of very intense magnetic storms are discussed in detail by Gonzalez et al. (1999). However, for long-term averages of solar wind, the effects of individual storms are obliterated and only steady-state characteristics prevail. Crooker et al. (1993) reported a high correlation between solar wind speed and geomagnetic activity, but earlier, Crooker and Gringauz (1977) had reported a low correlation for data after 1976. For cycles 20, 21, 22 (1964–1995), Kane (1997) reported that the correlation between solar wind velocity and  $aa$  index was  $+0.91 \pm 0.02$  for cycle 20,  $+0.77 \pm 0.04$  for cycle 21, and  $+0.73 \pm 0.04$  for cycle 22, indicating that factors

other than the wind velocity were involved. For the same period, Ahluwalia (2000) used annual mean values of  $Ap$  and IMF, and reported a long-term trend in the  $B$  data for 1963–1998. He found good correlations between the variations of  $Ap$  and  $BV$  or  $BV^2$ . In Fig. 3, the variations in the values of  $V$  and  $aa$  do not seem to match all the time. Hence, a correlation analysis was done for successive intervals of seven years (84 smoothed monthly values) at a time, with overlaps of a few years. The correlations were as given in Table 1.

In Table 1, the following may be noted:

1. The correlations of  $aa$  with solar wind velocity  $V$  in the seven successive intervals were (all positive): 0.64, 0.85, 0.50, 0.38, 0.34, 0.78, 0.98, indicating that this simple relationship was highly variable.
2. The correlations between  $aa$  and  $BV$ , and  $aa$  and  $(BV^2)$  for the seven intervals were (all positive): 0.70 (0.89), 0.95 (0.94), 0.97 (0.96), 0.96 (0.97), 0.87 (0.92), 0.96 (0.98), 0.82 (0.93). Thus, a very large variance is explained by the parameters  $BV$  as well as  $BV^2$ , as observed by Ahluwalia (2000). The parameter  $VB$  represents the induced electric field  $E = BV$  in the dawn to dusk direction, through which the solar wind-magnetosphere coupling occurs (Dungey, 1961). The dimensions of  $BV$  correspond to force per unit charge, while those of  $BV^2$  correspond to power per unit charge (transferred from the solar wind to the magnetosphere).
3. The correlations between  $aa$  and  $B$  were (all positive): 0.34, 0.84, 0.92, 0.91, 0.68, 0.85, 0.41. However, these were lower than the correlations with  $BV$  or  $BV^2$ , indicating that just  $V$  or just  $B$  was not enough. Both were needed for a better relationship with the  $aa$  index.
4. The correlations of  $aa$  with the southward IMF component  $B_z$  were:  $-0.37$ ,  $-0.07$ ,  $-0.69$ ,  $-0.35$ ,  $+0.12$ ,  $+0.67$ ,  $+0.10$ . Thus, the relationship is highly variable, even in sign. This is probably because even though  $B_z$  has a very high significance for individual storms (large negative  $B_z$  associated with high  $Kp$ ), the long-term average over monthly and yearly values is of dubious significance. If the sign is ignored, the scalar magnitude  $|B_z|$  was reported to be varying in concert with  $B$  for cycles 20 and 21 (Hapgood et al., 1991).
5. The correlations of  $aa$  with ion density  $N$  were:  $+0.01$ ,  $+0.74$ ,  $-0.23$ ,  $-0.19$ ,  $+0.28$ ,  $-0.03$ ,  $-0.54$ , indicating a poor, uncertain relationship. This is probably because  $N$  shows a 5-year cycle, not shown by  $aa$  or any other index. The correlation of  $aa$  with  $BV$  or  $BV^2$  is high (exceeding  $+0.90$ ), except in the first interval (1975–1981), when it was slightly lower ( $BV$ ,  $+0.70$ ). However, the correlation of  $aa$  with  $N$  was negligibly small ( $+0.01$ ) in this interval. Hence, inclusion of  $N$  as a parameter in a multiple regression does not increase the variance explained.

**Table 1.** Correlations between the aa index and various solar wind parameters

		1	2	3	4	5	6	7	8
1975–1981		<i>aa</i>	<i>V</i>	$V^2$	<i>B</i>	$B^*V^2$	$B^*V$	$B_z$	<i>N</i>
<i>aa</i>	1	1.00							
<i>V</i>	2	0.64	1.00						
$V^2$	3	0.62	1.00	1.00					
<i>B</i>	4	0.34	-0.39	-0.39	1.00				
$B^*V^2$	5	0.89	0.54	0.53	0.57	1.00			
$B^*V$	6	0.70	0.10	0.09	0.88	0.89	1.00		
$B_z$	7	-0.37	-0.31	-0.29	-0.06	-0.32	-0.23	1.00	
<i>N</i>	8	0.01	0.01	-0.01	-0.44	-0.37	-0.44	0.13	1.00
1978–1984		<i>aa</i>	<i>V</i>	$V^2$	<i>B</i>	$B^*V^2$	$B^*V$	$B_z$	<i>N</i>
<i>aa</i>	1	1.00							
<i>V</i>	2	0.85	1.00						
$V^2$	3	0.84	1.00	1.00					
<i>B</i>	4	0.84	0.60	0.59	1.00				
$B^*V^2$	5	0.94	0.94	0.94	0.83	1.00			
$B^*V$	6	0.95	0.87	0.87	0.91	0.98	1.00		
$B_z$	7	-0.07	0.26	0.28	-0.32	0.07	-0.05	1.00	
<i>N</i>	8	0.74	0.46	0.45	0.63	0.58	0.62	0.00	1.00
1981–1987		<i>aa</i>	<i>V</i>	$V^2$	<i>B</i>	$B^*V^2$	$B^*V$	$B_z$	<i>N</i>
<i>aa</i>	1	1.00							
<i>V</i>	2	0.50	1.00						
$V^2$	3	0.50	1.00	1.00					
<i>B</i>	4	0.92	0.21	0.21	1.00				
$B^*V^2$	5	0.96	0.64	0.64	0.88	1.00			
$B^*V$	6	0.97	0.47	0.47	0.96	0.98	1.00		
$B_z$	7	-0.69	0.10	0.10	-0.81	-0.57	-0.69	1.00	
<i>N</i>	8	-0.23	-0.50	-0.50	-0.17	-0.36	-0.28	0.04	1.00
1985–1991		<i>aa</i>	<i>V</i>	$V^2$	<i>B</i>	$B^*V^2$	$B^*V$	$B_z$	<i>N</i>
<i>aa</i>	1	1.00							
<i>V</i>	2	0.38	1.00						
$V^2$	3	0.37	1.00	1.00					
<i>B</i>	4	0.91	0.07	0.06	1.00				
$B^*V^2$	5	0.97	0.45	0.44	0.92	1.00			
$B^*V$	6	0.96	0.28	0.27	0.98	0.98	1.00		
$B_z$	7	-0.35	-0.03	-0.02	-0.44	-0.40	-0.43	1.00	
<i>N</i>	8	-0.19	-0.16	-0.16	-0.13	-0.16	-0.15	0.33	1.00
1988–1994		<i>aa</i>	<i>V</i>	$V^2$	<i>B</i>	$B^*V^2$	$B^*V$	$B_z$	<i>N</i>
<i>aa</i>	1	1.00							
<i>V</i>	2	0.34	1.00						
$V^2$	3	0.33	1.00	1.00					
<i>B</i>	4	0.68	-0.35	-0.36	1.00				
$B^*V^2$	5	0.92	0.42	0.41	0.70	1.00			
$B^*V$	6	0.87	0.03	0.03	0.92	0.92	1.00		
$B_z$	7	0.12	-0.58	-0.58	0.51	0.05	0.30	1.00	
<i>N</i>	8	0.28	-0.34	-0.35	0.53	0.24	0.41	0.26	1.00

**Table 1.** (continued)

1991–1997		<i>aa</i>	<i>V</i>	<i>V</i> <sup>2</sup>	<i>B</i>	<i>B</i> * <i>V</i> <sup>2</sup>	<i>B</i> * <i>V</i>	<i>Bz</i>	<i>N</i>
	<i>aa</i>	1	1.00						
	<i>V</i>	2	0.78	1.00					
	<i>V</i> <sup>2</sup>	3	0.77	1.00	1.00				
	<i>B</i>	4	0.85	0.41	0.40	1.00			
	<i>B</i> * <i>V</i> <sup>2</sup>	5	0.98	0.79	0.78	0.88	1.00		
	<i>B</i> * <i>V</i>	6	0.96	0.65	0.64	0.96	0.98	1.00	
	<i>Bz</i>	7	0.67	0.34	0.32	0.81	0.71	0.77	1.00
	<i>N</i>	8	−0.03	−0.54	−0.57	0.31	−0.08	0.09	0.18
1994–1999		<i>aa</i>	<i>V</i>	<i>V</i> <sup>2</sup>	<i>B</i>	<i>B</i> * <i>V</i> <sup>2</sup>	<i>B</i> * <i>V</i>	<i>Bz</i>	<i>N</i>
	<i>aa</i>	1	1.00						
	<i>V</i>	2	0.98	1.00					
	<i>V</i> <sup>2</sup>	3	0.97	1.00	1.00				
	<i>B</i>	4	0.41	0.31	0.32	1.00			
	<i>B</i> * <i>V</i> <sup>2</sup>	5	0.93	0.91	0.91	0.68	1.00		
	<i>B</i> * <i>V</i>	6	0.82	0.77	0.78	0.85	0.97	1.00	
	<i>Bz</i>	7	0.10	0.10	0.11	0.59	0.34	0.45	1.00
	<i>N</i>	8	−0.54	−0.50	−0.50	−0.76	−0.72	−0.80	−0.55

6. Some large correlations in Table 1 are due to obvious interdependences (*V* with *BV*, etc.) and are of little consequence.

## 5 Conclusions

The results of the present analysis may be summarized as follows:

1. The smoothed values of the minima of sunspot number *Rz* and the geomagnetic index *aa* were compared for sunspot cycles 12–23. In one cycle (cycle 14), *aa*(min) occurred earlier than *Rz*(min), but the broad, flat *aa*(min) continued until after *Rz*(min). In two cycles (12, 15), *Rz*(min) and *aa*(min) coincided within a month or two. In nine cycles, *aa*(min) occurred more than three months later than *Rz*(min).
2. A comparison with the plots of other solar indices showed that the *aa*(min) coincided with the minima of some solar radio emission indices originating in the solar corona.
3. Since *aa* is reported to be correlated with solar wind, a comparison was made for sunspot cycles 21, 22, 23. Solar wind velocity *V*(min) occurred 0–9 months later than the *aa*(min). Solar wind total magnetic field *B*(min) occurred near the *Rz*(min). The solar wind ion density *N* had maxima (instead of minima) near *Rz*(min), and again near *Rz*(max), indicating a 5-year periodicity, instead of an 11-year periodicity.
4. The maxima of *aa*, *V* and *B* occurred near *Rz*(max) and/or later in the declining phase of *Rz*.

5. The *aa* index was very well correlated with the functions *BV* and *BV*<sup>2</sup>.

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