

Vision-based navigation Simon Lacroix

► To cite this version:

Simon Lacroix. Vision-based navigation. Doctoral. Spring School on Location-Based Services, École Nationale d'Aviation Civile, Toulouse (France), France. 2015. cel-01276880

HAL Id: cel-01276880 https://hal.science/cel-01276880v1

Submitted on 20 Feb 2016

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Vision-based navigation

Simon Lacroix Robotics and InteractionS (RIS) LAAS/CNRS, Toulouse

http://homepages.laas.fr/simon/



Where do I come from?

Robotics at LAAS/CNRS, Toulouse, France

- Research topics
 - Perception, planning and decision-making, control
 - <u>Plus:</u> control architecture, interactions, ambient intelligence systems, learning
- Research domains
 - Cognitive and interactive Robotics
 - Aerial and Terrestrial Field Robotics
 - Human and anthropomorphic motion
 - Bio-informatics, Molecular motion

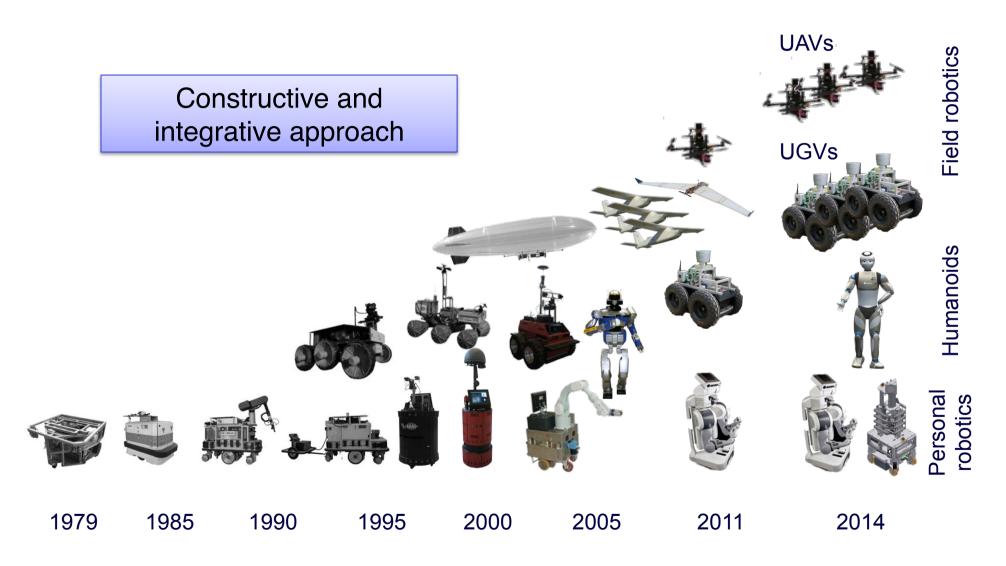
3 research groups : 12 full time researchers 10 university researchers 4 visitors 50 PhD students 10 post-docs

 Considered applications: Planetary exploration, Service and personal robotics, virtual worlds and animation, biochemistry, embedded systems, transport, driver assistance, defense, civil safety

Perception Action

A keyword: **autonomy**

Robots @ LAAS



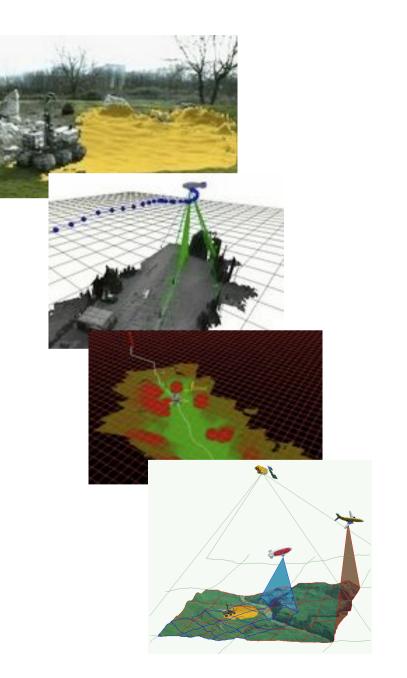
Open source software tools: www.openrobots.org

What am I working on? Field robotics

- Environment perception and modeling
- Localization and SLAM

Autonomous rover navigation

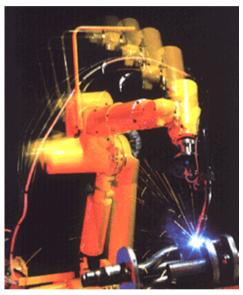
Multi-Robot cooperation



"From automatic control to autonomous control"

In laboratories

Industrial











"From automatic control to autonomous control"















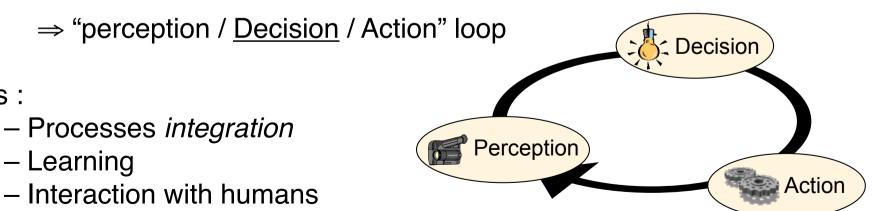




Robots everywhere

"From automatic control to autonomous control"

- Automatic control :
 - Well defined task ("regulate variable", "follow trajectory"...)
 - "Direct" link between (simple) perception and action
- Autonomous control :
 - More general task ("reach position", "monitor area "...)
 - Calls for decisional processes



- Interactions with other robots

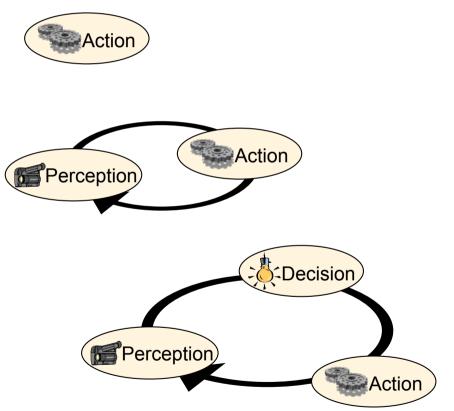
— ...

Plus :

"From automatic control to autonomous control"

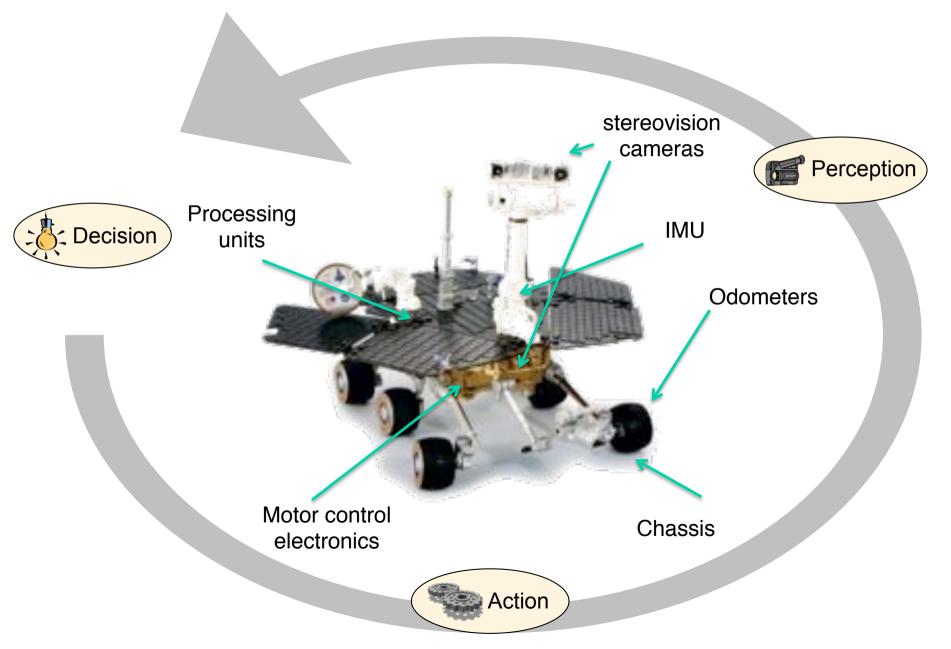
E.g. for a drone:

- Regulate heading / speed / altitude
- Follow a list ordered waypoints
- Follow a geometric trajectory
- Follow a road
- Follow a target
- Survey an area while avoiding threats and obstacles



"Decision": notion of deliberation, planning, prediction and evaluation of the outcomes of an action

Anatomy of a robot



Anatomy of a robot





Action

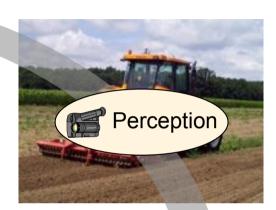












Illustration: autonomous navigation

```
nav•i•ga•tion |<sub>i</sub>navi'gā sH ən|
noun
1 the process or activity of accurately ascertaining one's
position and planning and following a route.
```



detect obstacles, traversable areas, localize the robot



avoid obstacles, find trajectories, itineraries

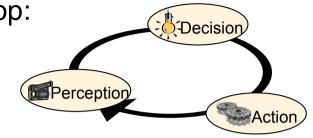


ensure the execution of the planned motions

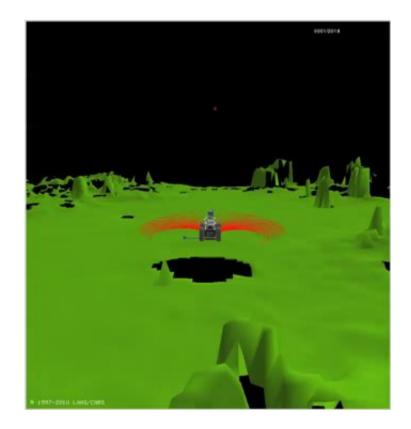
An elementary decision: AGV obstacle avoidance

Simple instance of a perception / decision / action loop:

- Gathering data on the environment
- Structuring the data into a model
- Planning the trajectory to find the "optimal" one
- Executing the trajectory







Perception in robotics

Perception :

« Acquisition and representation of information on the environnement and the robot itself »

Proprioceptive and exteroceptive sensors:

pro-pri-o-cep-tive |propreə'septiv| adjective Physiology relating to stimuli that are produced and perceived within an organism, esp. those connected with the position and movement of the body. Compare with EXTEROCEPTIVE and INTEROCEPTIVE .

ex•ter•o•cep•tive |_iekstərō'septiv| adjective Physiology relating to stimuli that are external to an organism. Compare with INTEROCEPTIVE .

Why is localization so important?



Why is localization so important *in robotics*?

Localization is required to:

- Ensure the spatial consistency of the built environment models
- Ensure the achievement of the missions, most often defined in localization tems ("goto [goal]", "explore / monitor [area]", ...)
- Ensure the proper execution of paths / trajectories
- Ensure the lowest level (locomotion) controls

But... what localization?

Essential questions to answer:

- 1. With which precision?
- 2. In which frame?
- 4. Integrity of the solution?
- 5. Disponibility of the solution?

From *cm* to *meters* Absolute vs. local 3. At which frequency? From *kHz* to "sometimes"

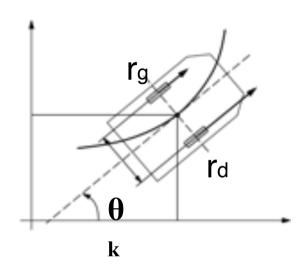
• Ensure the lowest level (locomotion) controls *cm* accuracy, > 100 Hz, - Ensure the proper execution of paths / trajectories local frame • Ensure the spatial consistency of the built models ~m accuracy, [• Ensure the achievement of the missions, most often defined

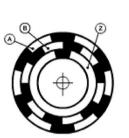
"sometimes", - in localization terms ("goto [goal]", "explore / global frame monitor [area]", ...)

Outline

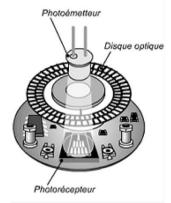
- Autonomous robots
- On the importance of localization
- Localization using dead-reckoning approaches

• Odometry: estimation of (x, y, θ) by integration of elementary motions

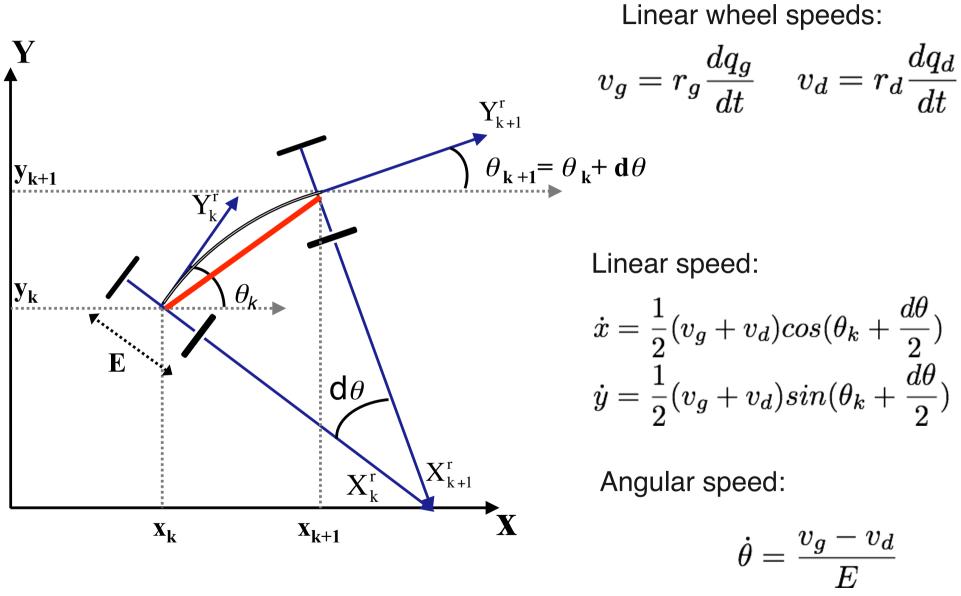




Représentation signaux incrémentaux A, B et Z sur disque optique



Wheel rotation encoders



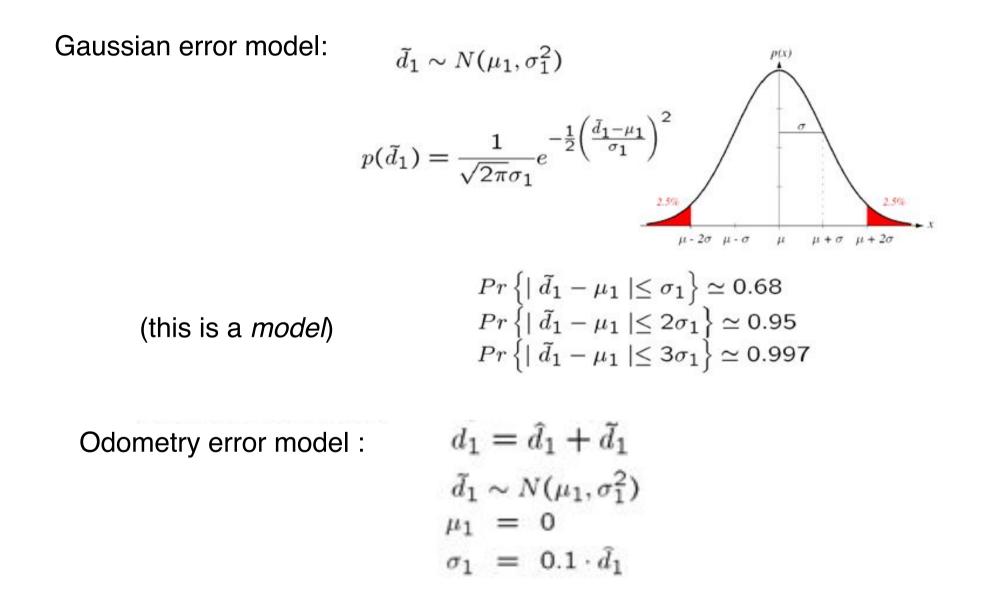


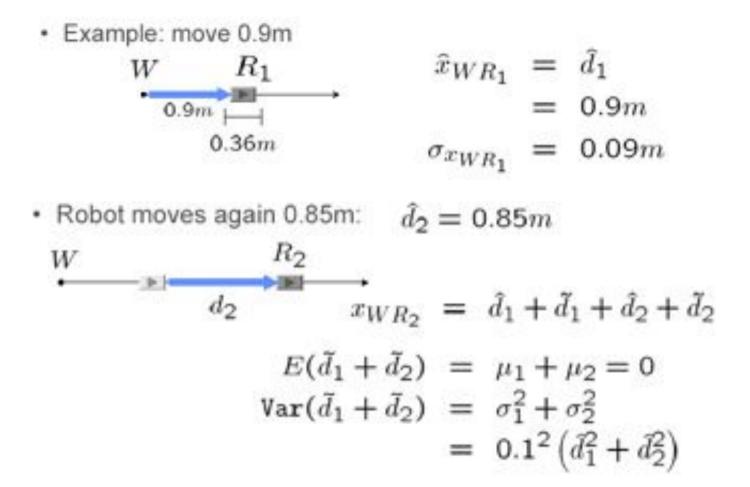
• Measured distance: $d_1 = \hat{d}_1 + \tilde{d}_1$

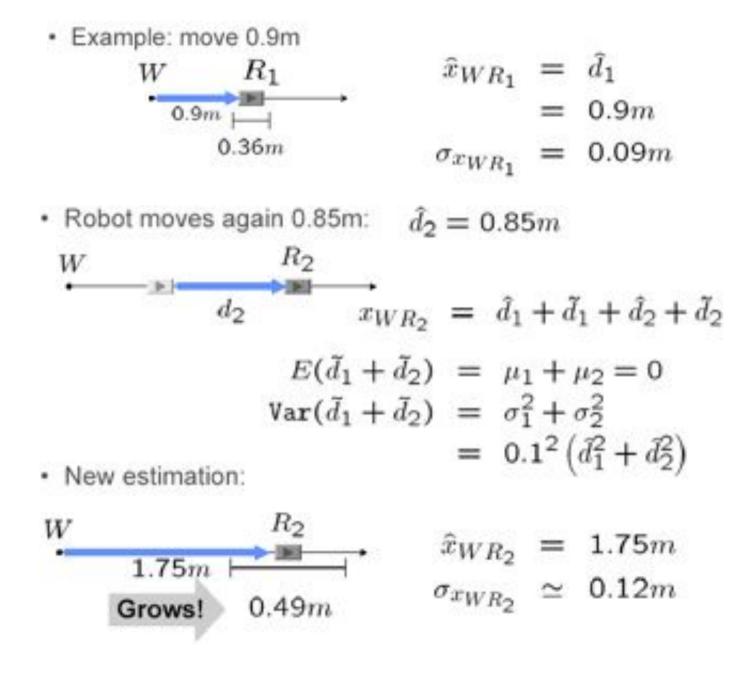
Error model:
$$\begin{array}{rcl} E(\tilde{d}_1) &=& \mu_1 \\ & \\ \operatorname{Var}(\tilde{d}_1) &=& \sigma_1^2 \end{array}$$

٠

For instance:
$$\begin{array}{rrrr} \mu_1 &=& 0 \\ \sigma_1 &=& 0.1 \cdot \hat{d}_1 \end{array}$$





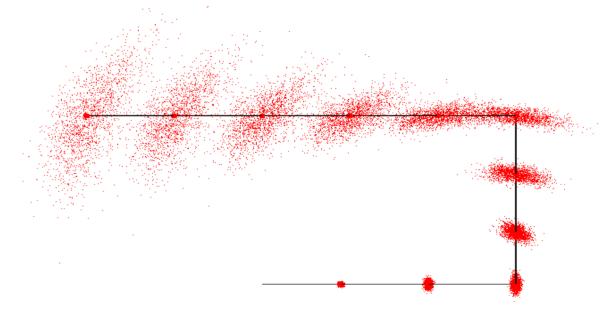


ı.

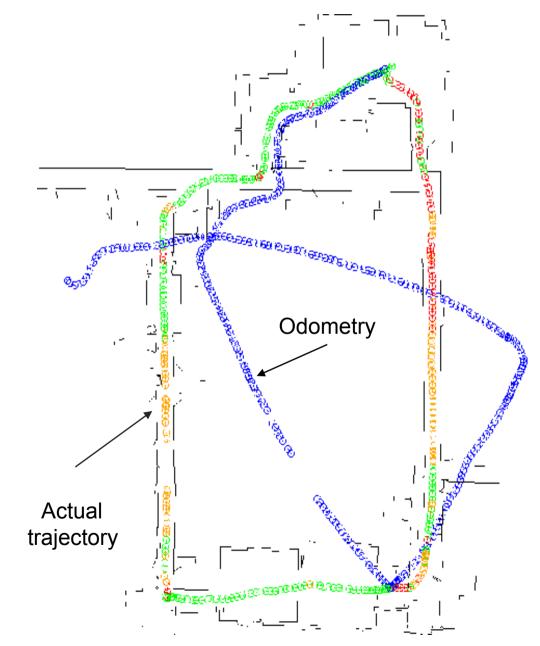
Now angular rotations come into play

Monte-Carlo simulation:

1



Odometry: illustration



• With an indoor robot

Localization solutions in robotics

- Odometry
- Similarly, motion / accelerations sensors (inertial navigation)

Inherently drifts over time and distances, subject to slippages and skids

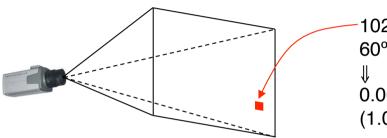
Develop solutions relying on the robot exteroceptive sensors

A few words on vision

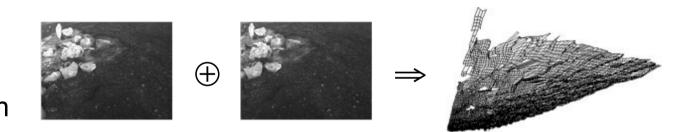
 Cameras : low cost, light and power-saving



- Perceive data
 - In a volume
 - Very far
 - Very precisely
- Stereovision
 - 2 cameras provide depth



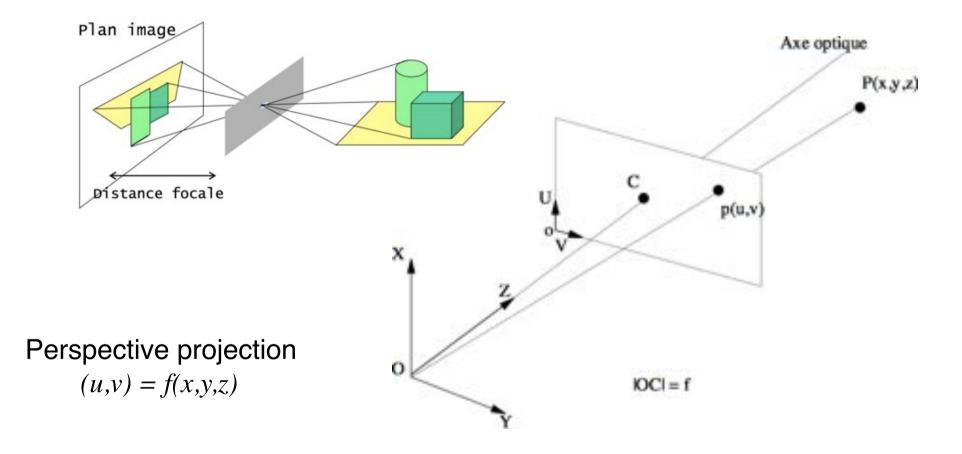
-1024 x 1024 pixels 60° x 60° FOV ↓ 0.06 ° pixel resolution (1.0 cm at 10.0 m)



- Images carry a vast amount of information
- A vast know-how exists in the computer vision community

Camera geometric model

• Pinhole model



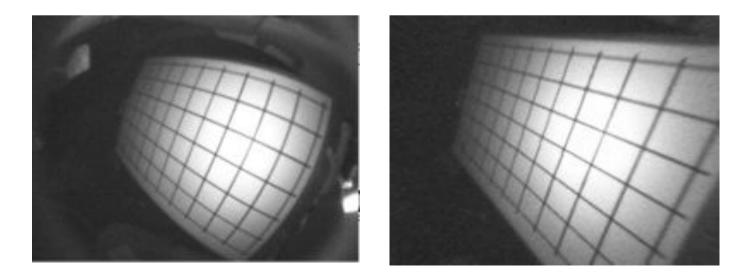
 $u = k_u f x/z + u_0$ $v = k_v f y/z + v_0$ $p = I_c P$ I_c : camera intrinsic matrix

Camera geometric model

(But the real world is more complex)







Camera calibration

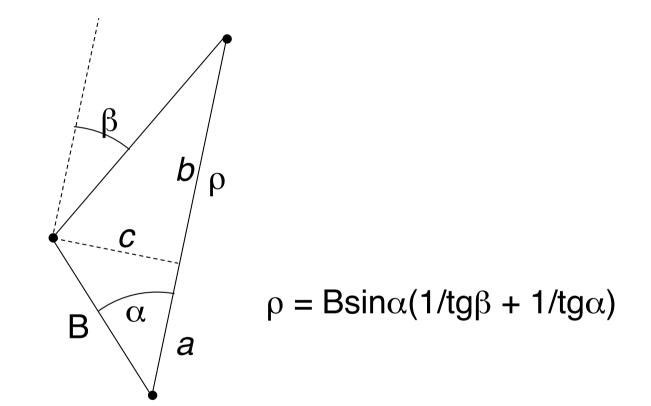
- Principle
 - 1. Acquisition of images of a known calibration pattern
 - 2. Extraction of the pattern features
 - 3. Association between extracted features and patten features
 - 4. Use of a minimization technique to estimate the projection parameters

Classic calibration patterns



Well known techniques, available softwares on line (*e.g.* Matlab calibration toolbox, openCV library)

Triangulation



Triangulation



Figure 3 : Triangulation laser

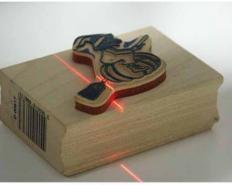
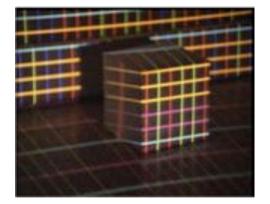
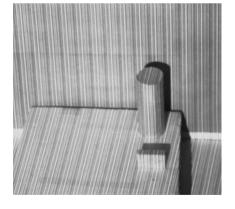


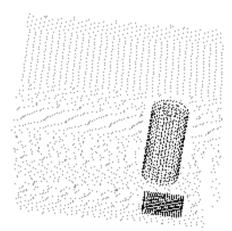
Figure 4 : Zoom sur l'objet



Figure 6 : Nuage de points







The precision depends on the baseline

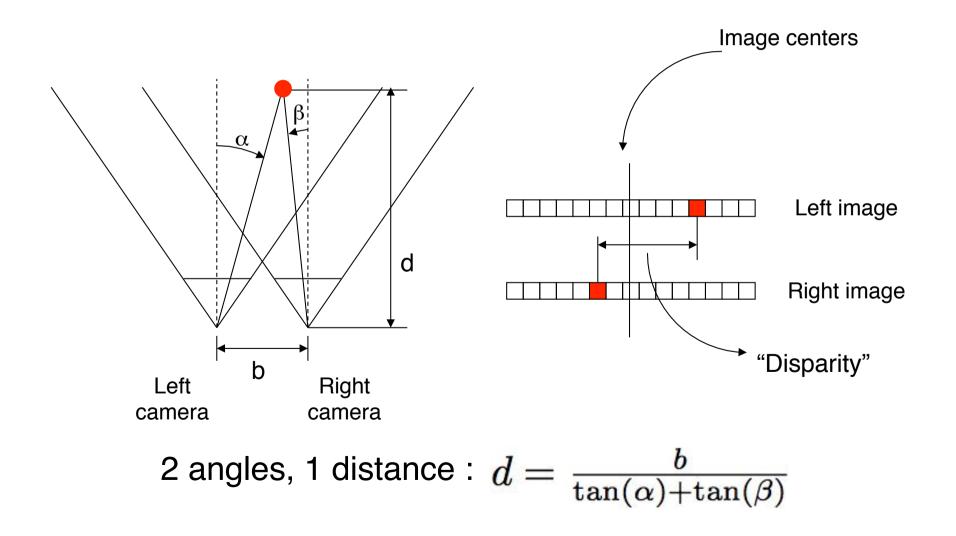
• Autumn 2010 : Kinect







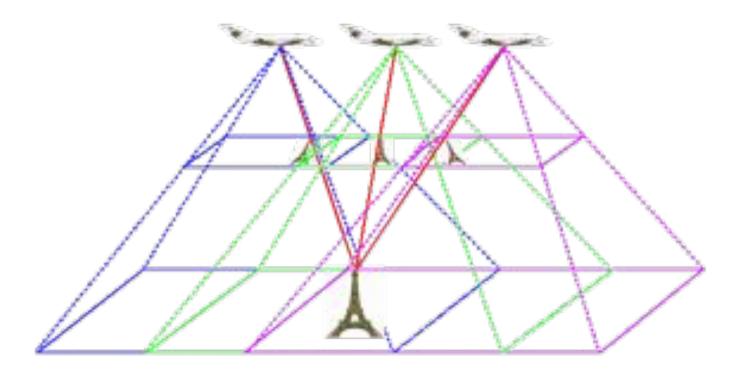
• Stereovision = triangulation



Dense stereovision 0. Image pair acquisition Calibration data 1. Image rectification Calibration data 2. Pixel matching 3.3D process reconstruction

Single camera stereovision (« Structure from Motion »)

One moving camera









Additional difficulty: estimation of the motion parameters

(« structure and motion from motion », « SLAM »)

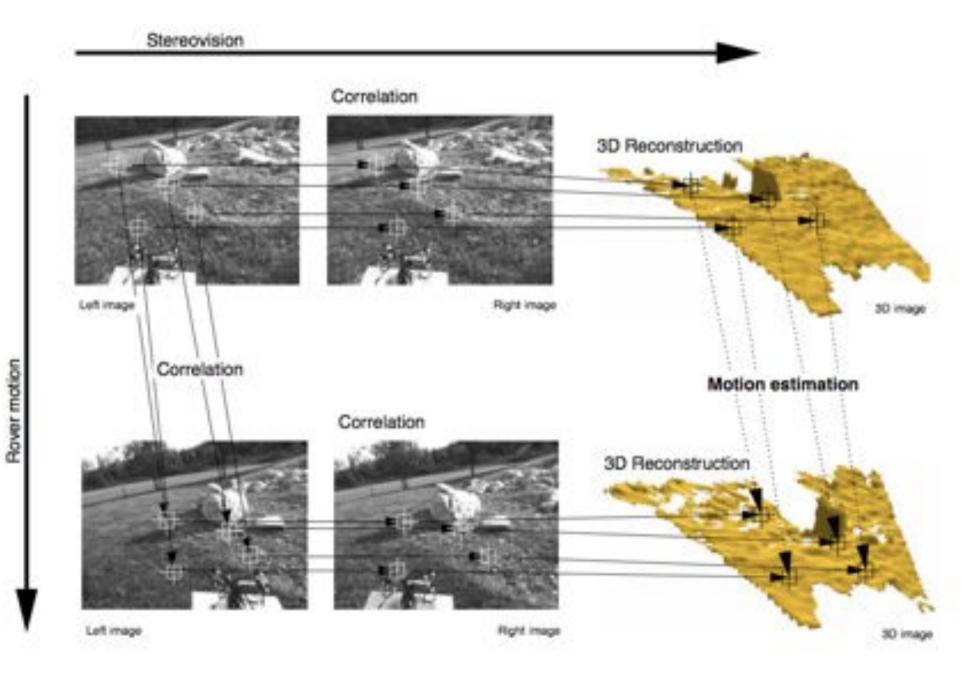
Localization solutions in robotics

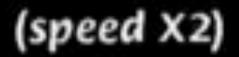
- Odometry
- Similarly, motion / accelerations sensors (inertial navigation)

Inherently drifts over time and distances, subject to slippages and skids

Develop solutions relying on the robot exteroceptive sensors

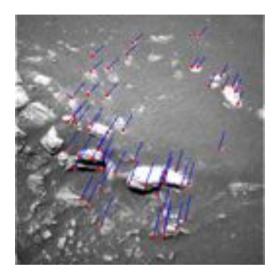
Visual odometry: principle

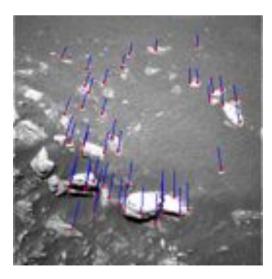


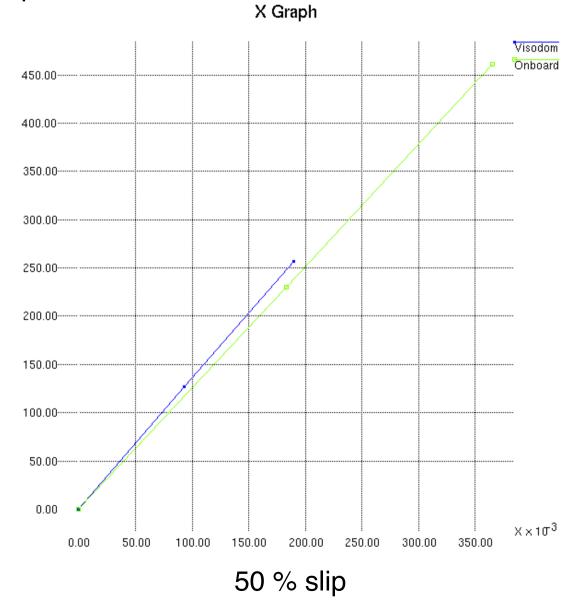


Visual odometry: results

• Applied on the Mars Exploration Rovers







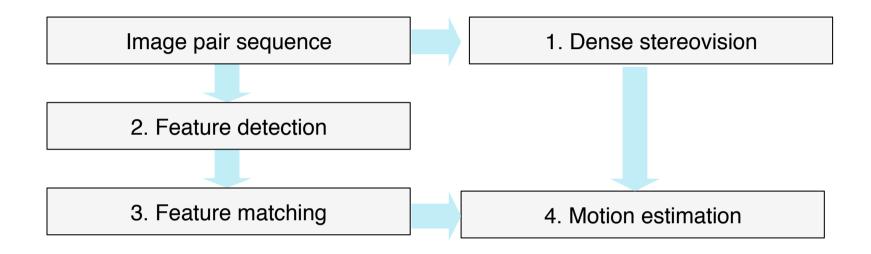
Visual odometry: benefits

- Contrary to wheel odometry, VO is not affected by wheel slip in uneven terrain or other adverse conditions.
- More accurate trajectory estimates compared to wheel odometry (relative position error 0.1% – 2%)

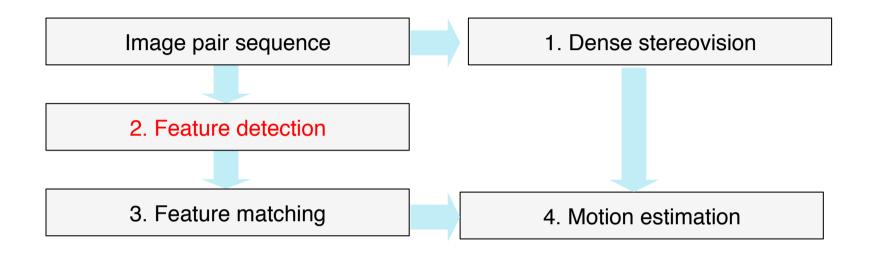


• In GPS-denied environments (*e.g.* underwater, planetary or indoor), VO has utmost importance

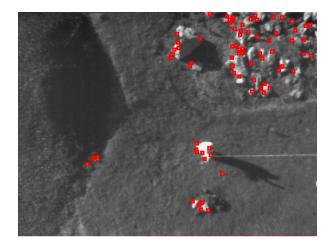
Visual odometry: implied functions



Visual odometry: implied functions



Interest points



Harris interest points: sharp peaks of the autocorrelation function

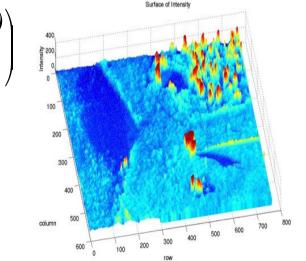
Auto-correlation matrix:

$$G(\mathbf{x},\overline{\sigma}) \otimes \begin{pmatrix} I_u(\mathbf{x},s\sigma)^2 & I_u(\mathbf{x},s\sigma)I_v(\mathbf{x},s\sigma) \\ I_u(\mathbf{x},s\sigma)I_v(\mathbf{x},s\sigma) & I_v(\mathbf{x},s\sigma)^2 \end{pmatrix}$$

$$I_u(\mathbf{x},s\sigma) = s G_u(\mathbf{x},s\sigma) * I(\mathbf{x}),$$

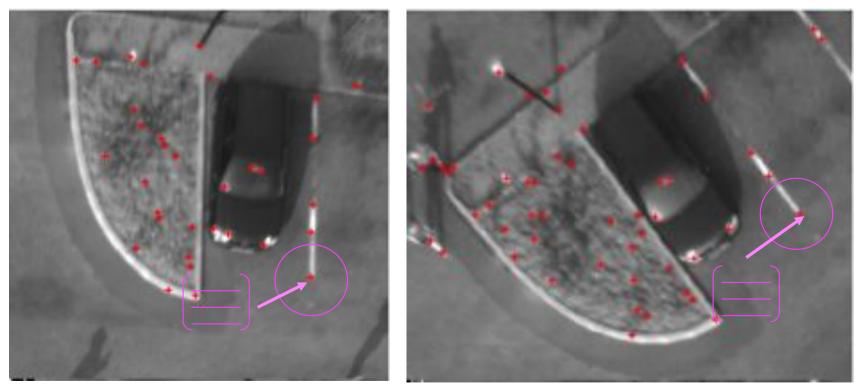
$$I_v(\mathbf{x},s\sigma) = s G_v(\mathbf{x},s\sigma) * I(\mathbf{x})$$

Principal curvatures defined by the two eigen values of the matrix λ_1, λ_2 (s: scale of the detection)



Interest points

 Local gray value invariants [Harris 88][Schmid 97] : local description vector invariant to rotation



Find matches with the similarity measure of *descriptors*

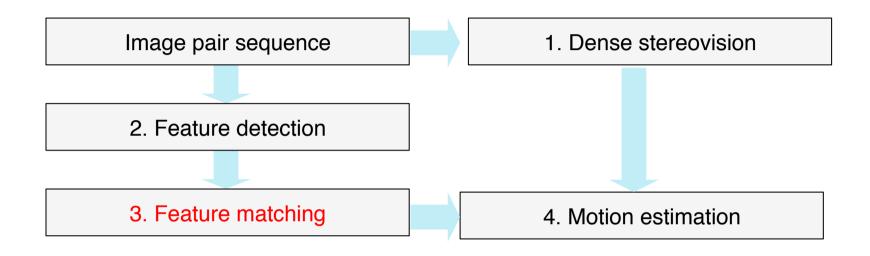
Harris interest points



Interest points

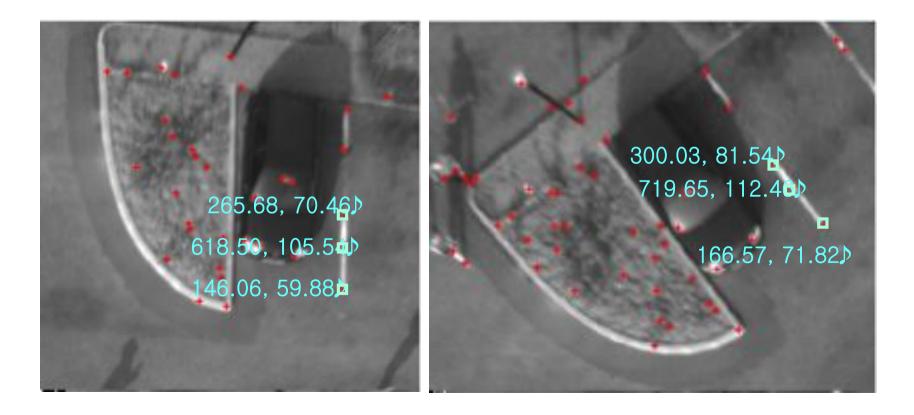
- Numerous interest points definition available
 - Scale invariant interest points ("SIFT", [Lowe99])
 - Speeded-up robust features ("SURF", [Bay 2006])
 - Binary Robust Independent Elementary Features ("BRIEF", [Calonder 2010])
 - ...
- The choice depends on the considered problem context

Visual odometry: implied functions



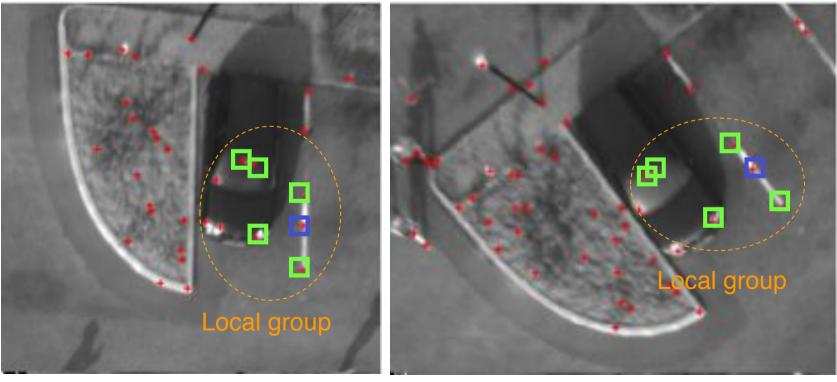
Interest points matching : principle

- If a generated match is correct,
 - Similar principal curvatures
 - Applied to matching candidate selection



Interest points matching : principle

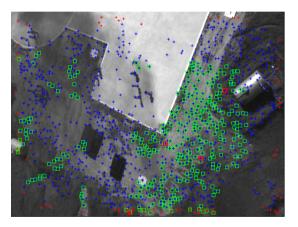
- If a generated match is correct,
 - In the vicinity of the match, neighbor matches must exist
 - Local group matching : consideration a local region of image

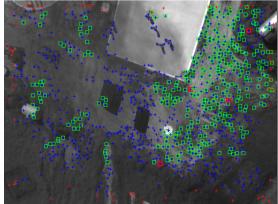


□: pivot □: members

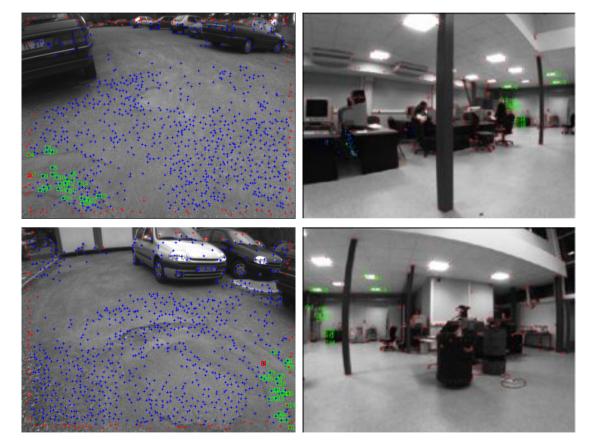
Some matching results

Consecutive frames

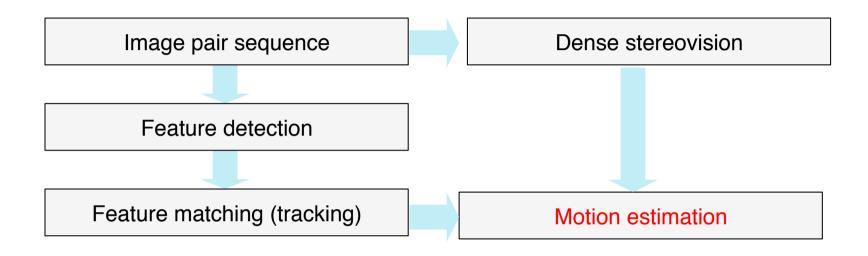




Small overlap

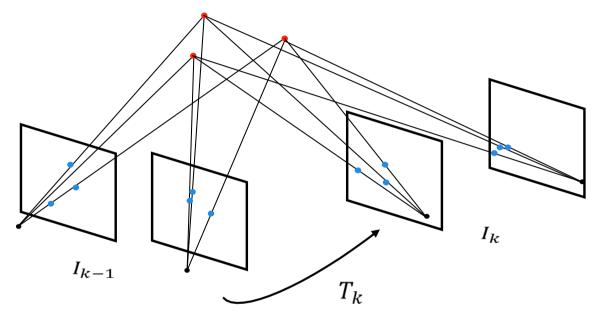


Visual odometry: implied functions



Motion estimation: problem statement

• Given two set of matched 3D points



• Find the 3D transformation T_k that minimizes the point distances

$$T_k = \begin{bmatrix} R_{k,k-1} & t_{k,k-1} \\ 0 & 1 \end{bmatrix} = \arg\min_{T_k} \sum_i ||\tilde{X}_k^i - T_k \tilde{X}_{k-1}^i||$$

Motion estimation: least square minimization

- Given two set of matched 3D points $\{p_i\}, \{p'_i\}$
- The coordinates of matching points are linked by:

$$p_i' = R.p_i + T + N_i$$

Where N_i denotes some noise

• Least square estimation: find the 3D transform (R,T) that minimizes:

$$\Sigma^2 = \sum_{i=1}^{N} \|p'_i - (R.p_i + T)\|^2$$

Motion estimation: least square minimization

 Assuming a zero-mean noise on the points coordinates, the barycenter of the transformed first set and the second set should be equal:

$$p' = p''$$

where
$$p = \frac{1}{N} \cdot \sum_{i=1}^{N} p_i$$
; $p' = \frac{1}{N} \cdot \sum_{i=1}^{N} p'_i$; $p'' = \frac{1}{N} \cdot \sum_{i=1}^{N} \hat{R} \cdot p_i + \hat{T}$
Changing the coordinates: $q_i = p_i - p$; $q'_i = p'_i - p'$

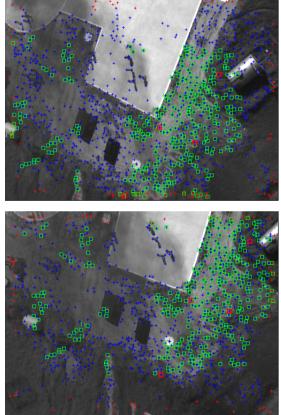
then we have $\Sigma^2 = \sum_{i=1}^N \left\| q_i' - R.q_i \right\|^2$

- 1. Find *R* that minimizes Σ^2 (least square minimization)
- 2. Estimate T as $\hat{T} = p' \hat{R}.p$

•

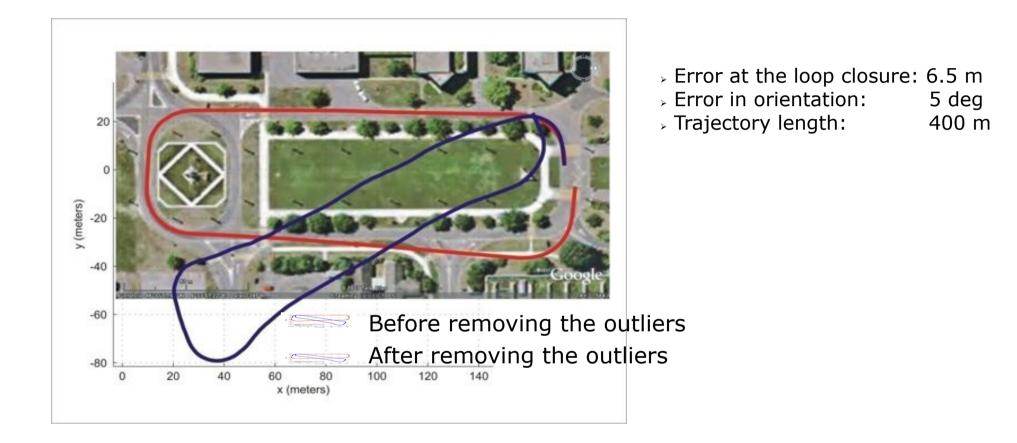
Robust estimation

- Matched points are usually contaminated by wrong data associations (= "outliers")
- Possible causes of outliers are
 - image noise
 - occlusions
 - 。 blur,
 - changes in view point and illumination for which the feature detector or descriptor does not account for
- For the camera motion to be estimated accurately, outliers *must* be removed
- This is the task of robust estimation



• "RANSAC" ("Random Sample Consensus") [Fishler & Bolles, 1981] has been established as the standard method for motion estimation in the presence of outliers

Results / Robust estimation



[D. Scaramuzza @ ETHZ]

Localization solutions in robotics

- Odometry
- Similarly, motion / accelerations sensors (inertial navigation)

Inherently drifts over time and distances, subject to slippages and skids

- Develop solutions relying on the robot exteroceptive sensors
- Visual odometry: akin to dead reckoning

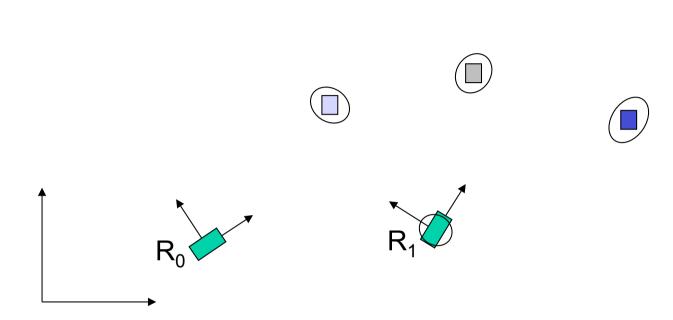
Inherently drifts over time and distances



Develop solutions relying on the robot exteroceptive sensors that memorizes stable environment features (SLAM)

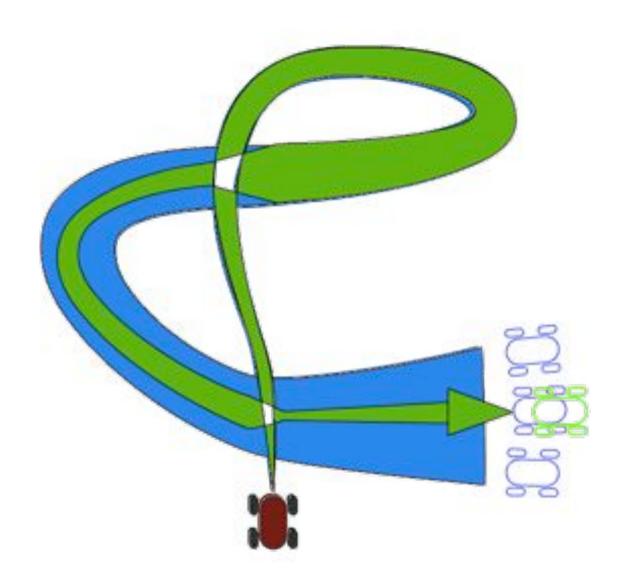
SLAM Simultaneous Localisation And Mapping

Principle of SLAM



- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- <u>Estimation</u>: refinement of the landmark <u>and</u> robot positions

Principle of SLAM



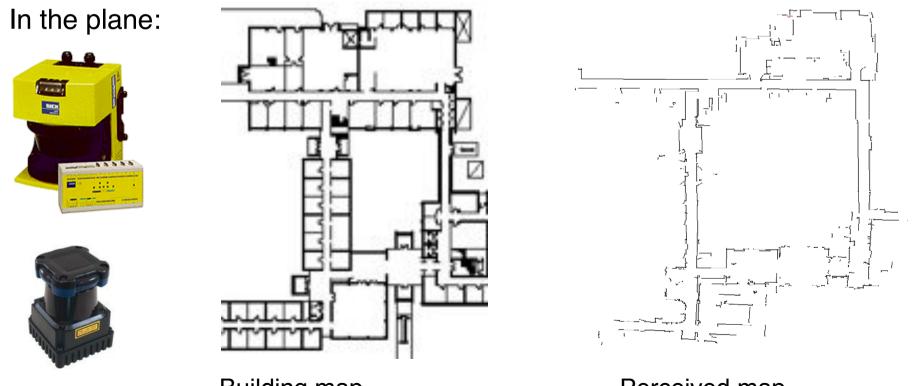
(parenthesis: 2D Lidars)

• Telemetry (« measuring distances »)



Laser («Light Amplification by Stimulated Emission of Radiation ») Time of flight of phase shift measures

→ LIDAR (« Light Detection And Ranging »)



Building map

Perceived map

Occupancy grid: on a flat plane, with odometry and "2D" LRF (S. Thrun)



Occupancy grid: on a flat plane, with odometry and "2D" LRF (S. Thrun)





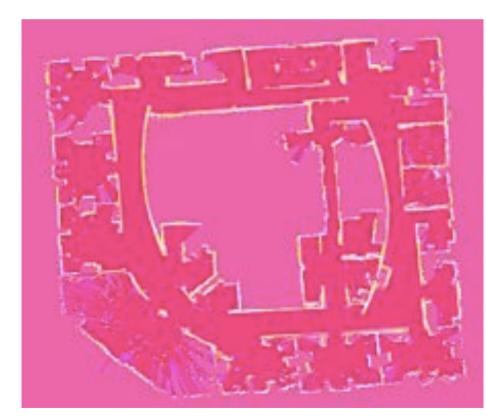


Occupancy grid: on a flat plane, with odometry, a "2D" LRF and SLAM (S. Thrun)



Occupancy grid: on a flat plane, with odometry, a "2D" LRF and SLAM (S. Thrun)







SLAM must reads

There are tons of papers on SLAM...

At least, read those:

Simultaneous Localisation and Mapping (SLAM): Part I The Essential Algorithms

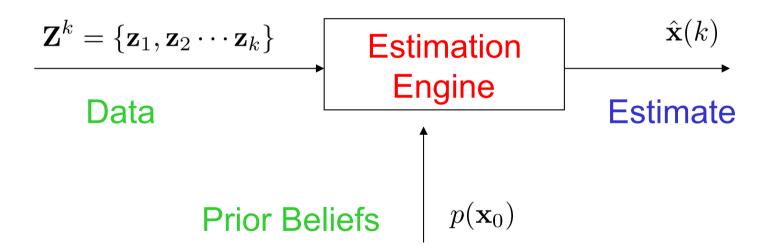
Hugh Durrant-Whyte, Fellow, IEEE, and Tim Bailey

Simultaneous Localisation and Mapping (SLAM): Part II State of the Art

Tim Bailey and Hugh Durrant-Whyte

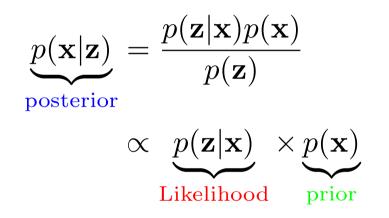
(in Robotics and Automation Magazine, Vol 13, Num 2/3, 2006)

"Estimation is the process by which we infer the value of a quantity of interest, \mathbf{x} , by processing data that is in some way dependent on \mathbf{x} ."



Maximum A Posteriori estimation:

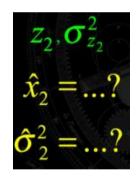
Sensor model p(z|x): "Given x, the probability of the sensor measurement being within 1m is...."

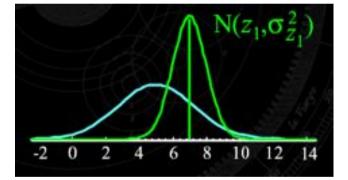


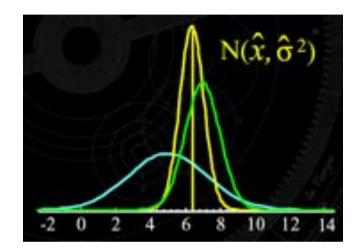
Given an observation \mathbf{z} , a likelihood function $p(\mathbf{z}|\mathbf{x})$ and a prior distribution on \mathbf{x} , $p(\mathbf{x})$, the **maximum a posteriori estimator - MAP** finds the value of \mathbf{x} which maximises the posterior distribution $p(\mathbf{x}|\mathbf{z})$

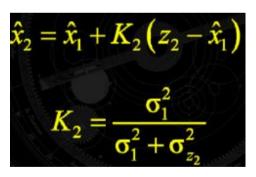
$$\hat{\mathbf{x}}_{map} = \arg\max_{\mathbf{x}} p(\mathbf{z}|\mathbf{x}) p(\mathbf{x}) \tag{1}$$

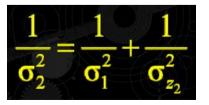
Example of MAP estimation With normal prior and likelihood











Recursive Bayesian estimation

 $\mathbf{Z}^k = \{\mathbf{z}_1, \mathbf{z}_2 \cdots \mathbf{z}_k\}$ Sequence of data (measurements)

We want conditional mean (mmse) of x given Z^k

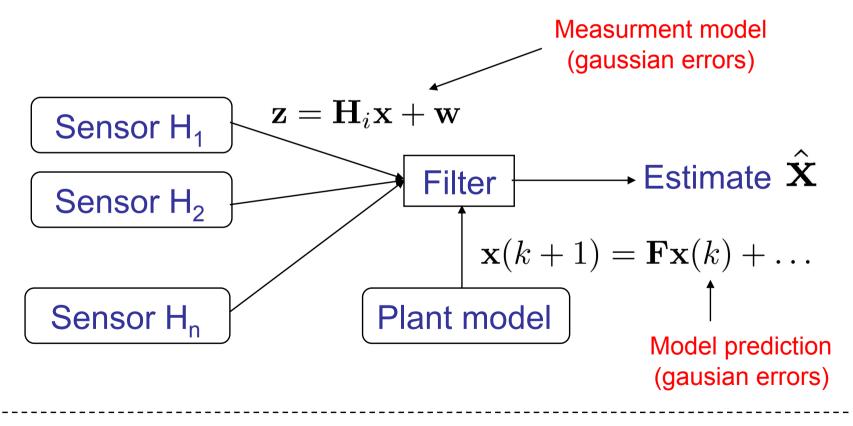
Can we iteratively calculate this – *i.e.* every time a new measurement comes in, update our estimate?

Key idea: "one mans posterior is another's prior"

Basics on estimation

Kalman filter

Recursive process: estimate the system state from uncertain observations (measures) and an uncertain system model



Actual underlying state: x

Basics on estimation

Kalman filter: things to know

- A recursive process
- Asynchronous
- Prediction / update structure
- Prediction increases covariances
- Update decreases covariances
- Essential importance of correlations

Mapping and Localisation

• With perfect localisation:

Given the robot position \mathbf{x}_v , and a sensor model $p(\mathbf{Z}^k | \mathbf{M}, \mathbf{x}_v)$ compute the map M: $p(\mathbf{M} | \mathbf{x}_v, \mathbf{Z}^k)$

→ Mapping problem « solved » (proper management of the sensors uncertainties)

With a perfect known map

Given a feature map M, and a sensor model $p(\mathbf{Z}^{\mathbf{k}}|\mathbf{M}, \mathbf{x}_v)$ compute the robot position \mathbf{x}_v : $p(\mathbf{x}_v|\mathbf{M}, \mathbf{Z}^{\mathbf{k}})$

Localisation problem « solved » (proper matching of sensor data and the map)

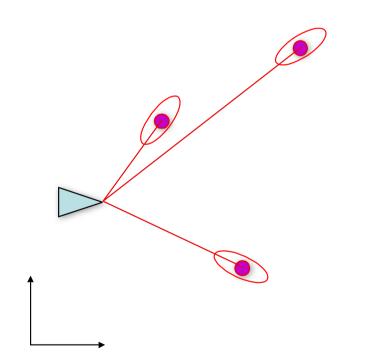
Mapping and Localisation

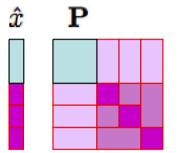
Without perfect localisation, nor perfect map ?
 ⇒ Simultaneous localisation and mapping (SLAM)

Given the robot controls u_k and the sensor readings z_k , compute the map M and the robot position x_v : $p(M, x_v|u_k, z_k)$

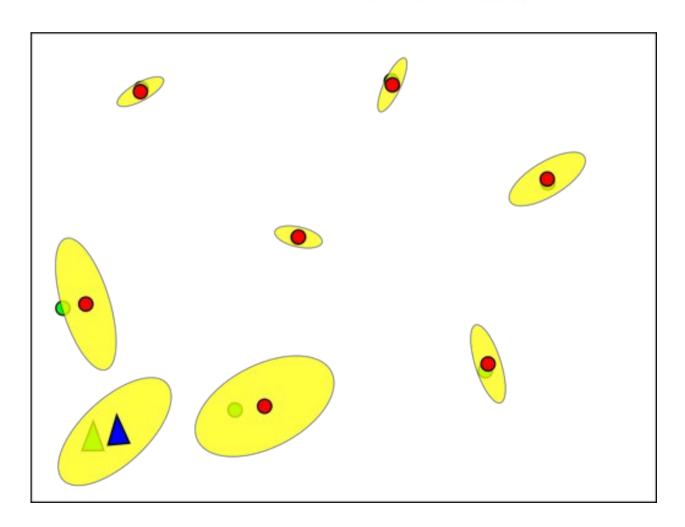
SLAM: outline

- Simultaneous localisation and mapping
 - Problem presentation
 - Basics on estimation
 - EKF SLAM



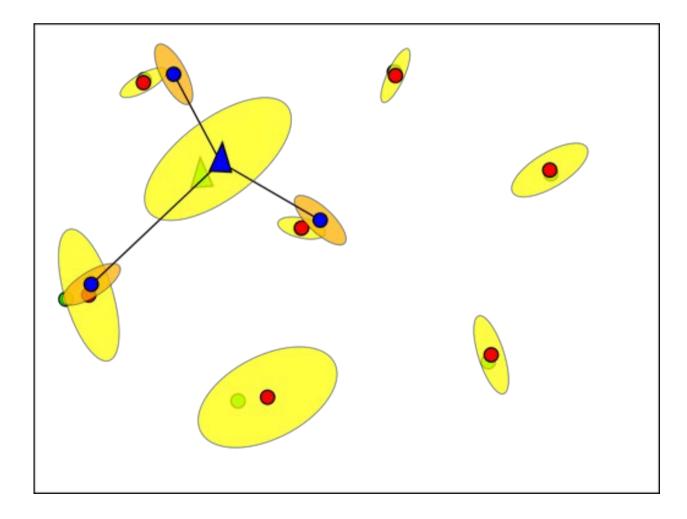


Importance of the correlations $\mathbf{P} = \begin{bmatrix} \mathbf{P}_{vv} & \mathbf{P}_{vm} \\ \mathbf{P}_{vm}^T & \mathbf{P}_{mm} \end{bmatrix}$

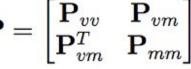


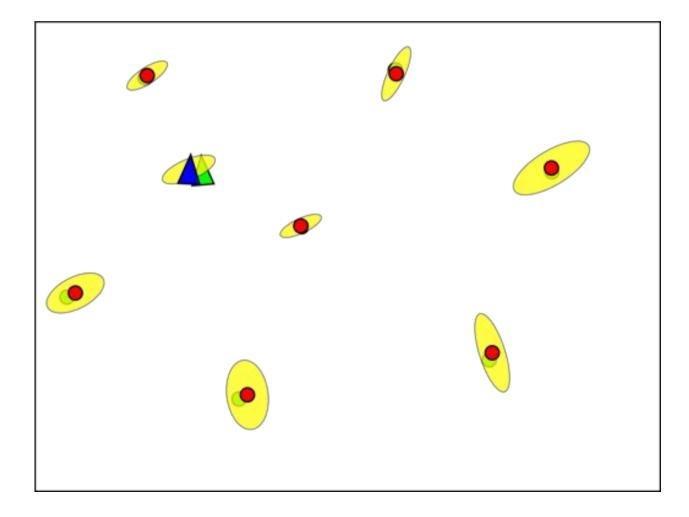
Importance of the correlations P

$$\mathbf{P} = \begin{bmatrix} \mathbf{P}_{vv} & \mathbf{P}_{vm} \ \mathbf{P}_{vm}^T & \mathbf{P}_{mm} \end{bmatrix}$$



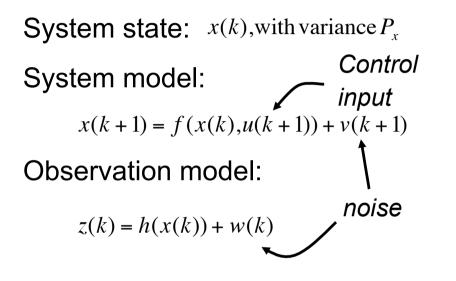
Importance of the correlations $\mathbf{P} = \begin{bmatrix} \mathbf{P}_{vv} & \mathbf{P}_{vm} \\ \mathbf{P}_{vm}^T & \mathbf{P}_{mm} \end{bmatrix}$

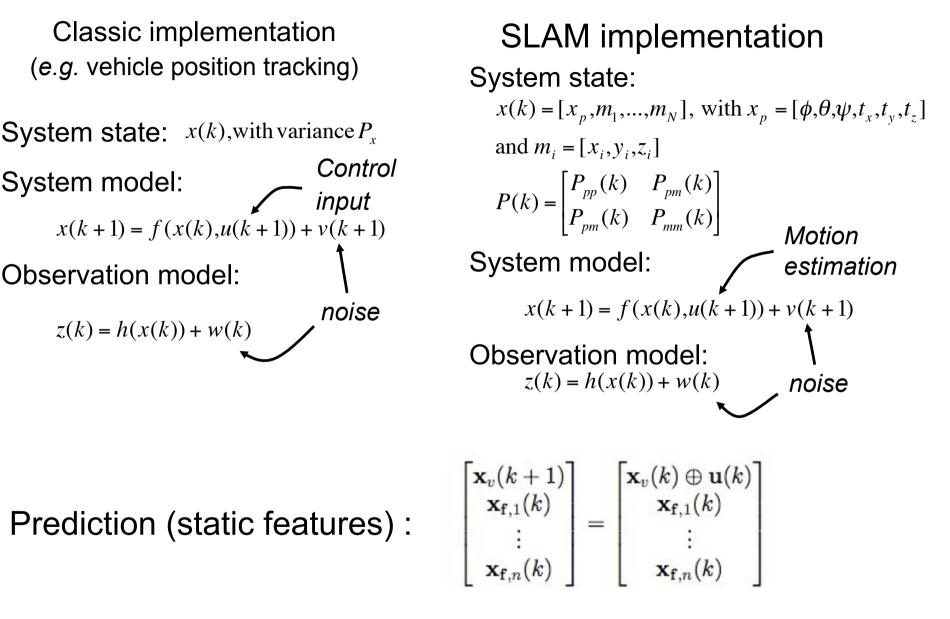




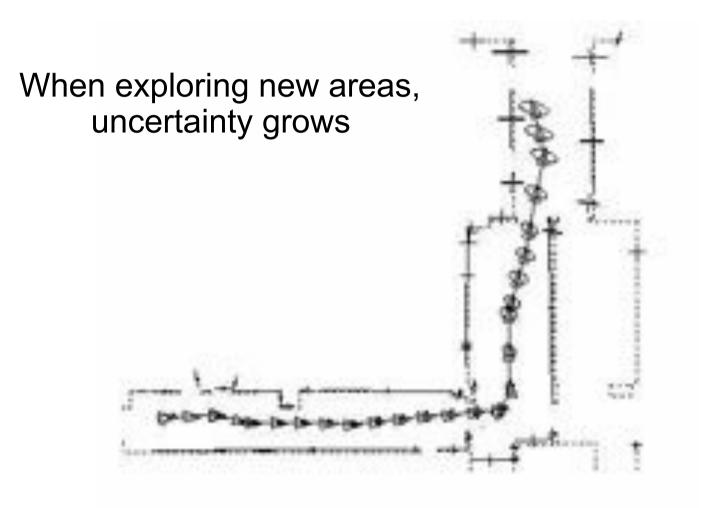
Kalman filter for SLAM

Classic implementation (e.g. vehicle position tracking)

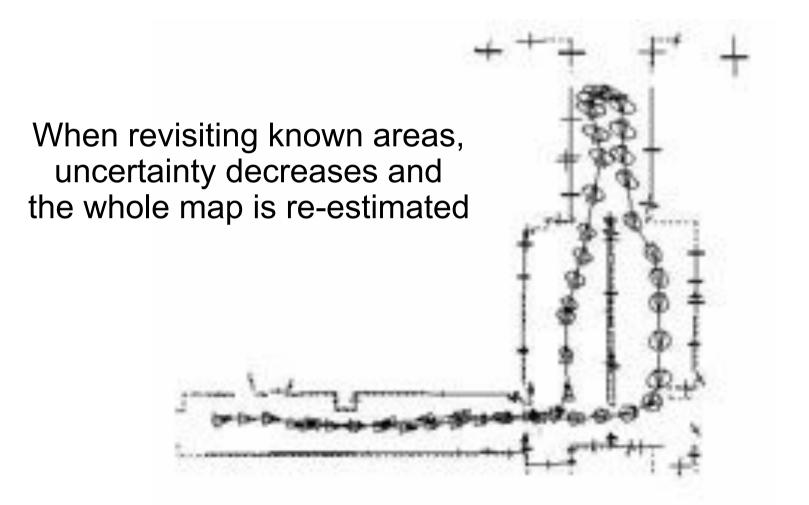




Kalman filter for SLAM



Kalman filter for SLAM



SLAM: outline

• Simultaneous localisation and mapping

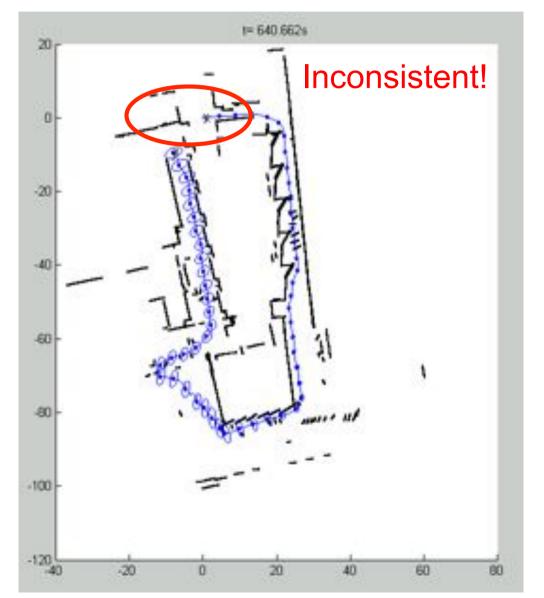
- Problem presentation
- Basics on estimation
- EKF SLAM
- Main issues

EKF-SLAM Issues

1. Algorithmic complexity: $O(n^2)$

EKF-SLAM Issues

2. Non-linearities yield inconsticency



Standard data association cannot close a 250m loop

Computational complexity was not a problem here!

EKF-SLAM Issues

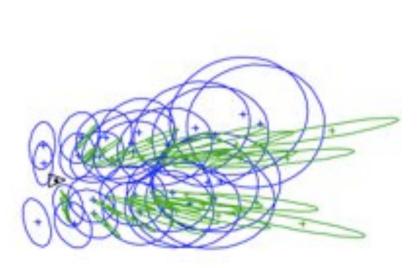
3. Data associations

Within the estimation framework:

Measurements Predicted features

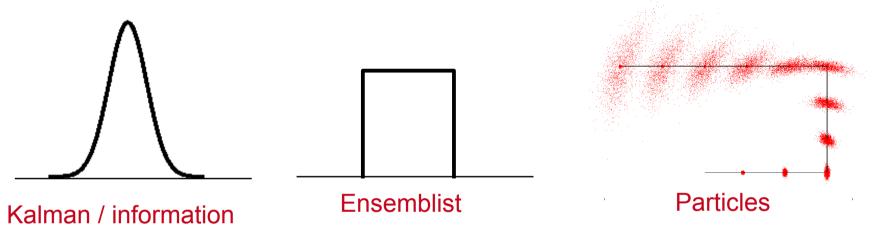
Within the estimation framework ?

Measurements Predicted features



SLAM : other estimation approaches

Stochastic approaches :



Global minimization approaches (*e.g.* bundle adjustment, scan matching)

SLAM: outline

• Simultaneous localisation and mapping

- Problem presentation
- Basics on estimation
- EKF SLAM
- Main issues
- Vision-based SLAM

Beyond estimation

Functions required by any SLAM implementation :

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Refinement of the landmark and robot positions

- A perception process
- A perception process
- Control, signal processing...
- A perception process
- An estimation process

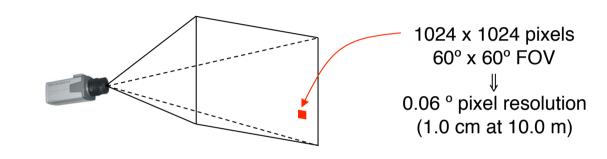
Use vision !

Micro UAVs

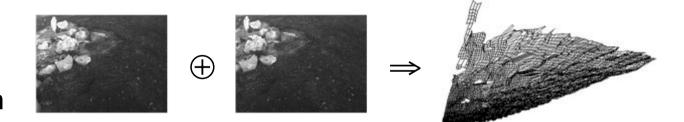
• Cameras : low cost, light and power-saving



- Perceive data
 - In a volume
 - Very far
 - Very precisely



- Loss of depth is (almost) not anymore a difficulty
- Stereovision
 - 2 cameras provide depth



- Images carry a vast amount of information
- A vast know-how exists in the computer vision community

SLAM : what kind of landmarks ?

A good landmark:

- Should be *discriminant* (easy to associate)
- Should be invariant wrt. the viewpoint
- Its position (or part of it) should be observable with an associated *error model*

Some point features have these properties:

- Harris features
- SIFT features

Stereovision SLAM

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Refinement of the landmark and \rightarrow Extended Kalman filter robot positions

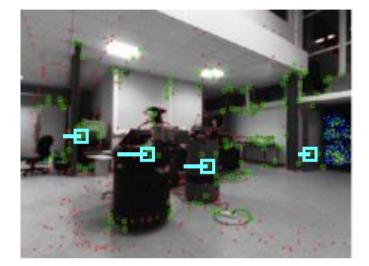
- \rightarrow Vision : interest points
 - \rightarrow Stereovision
 - \rightarrow Visual motion estimation
- \rightarrow Interest points matching

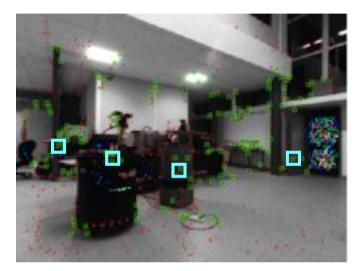
Landmark observation : stereovision

Dense stereovision

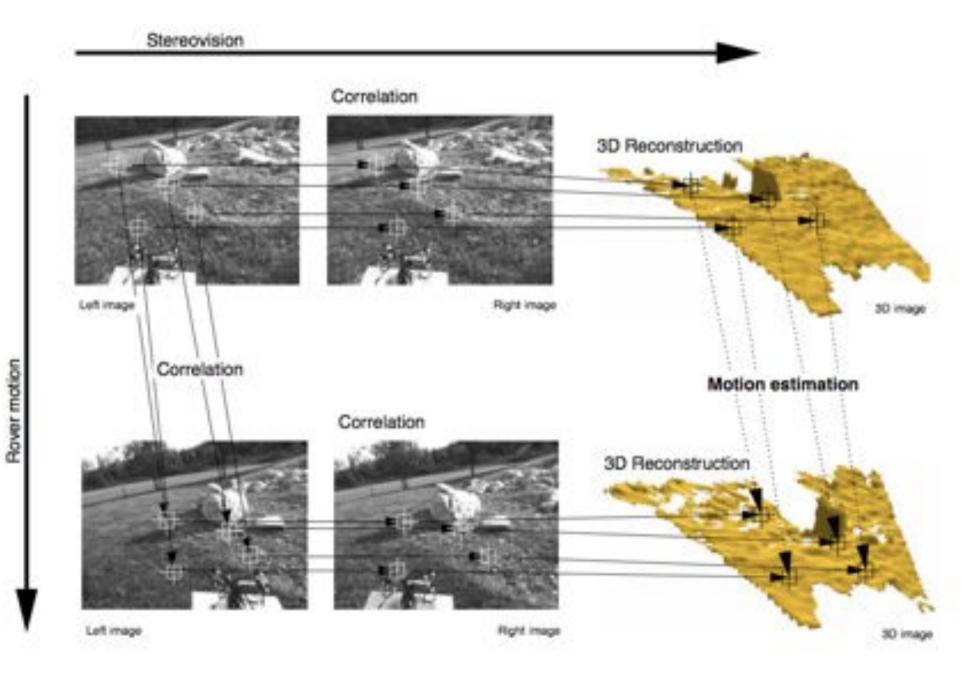
or

IP matching applied on stereo frames (even easier)





Visual odometry: principle



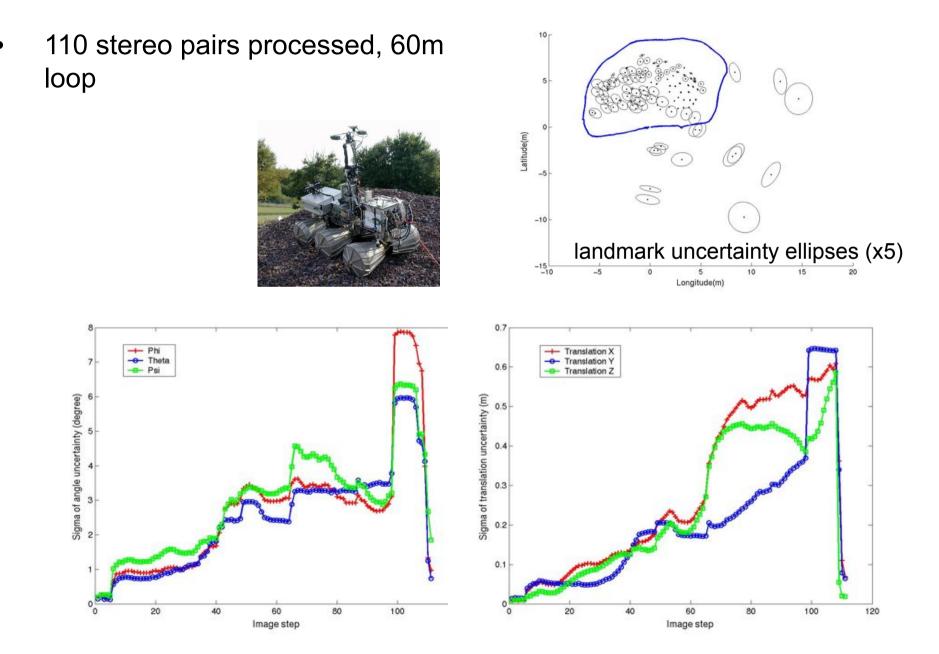
Stereovision SLAM

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Refinement of the landmark and \rightarrow Extended Kalman filter \leftarrow OK robot positions

 \rightarrow Vision : interest points \leftarrow OK

- \rightarrow Stereovision \leftarrow OK
- \rightarrow Visual motion estimation \leftarrow OK
- \rightarrow Interest points matching \leftarrow OK

On a ground rover



On a ground rover

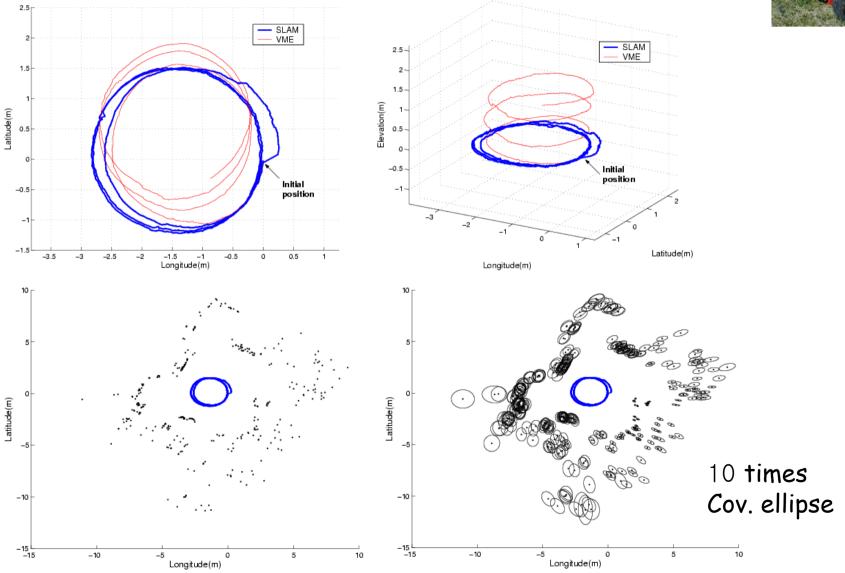
• 110 stereo pairs processed, 60m loop



	Frame 1/100 Reference	Reference Std. Dev.	VME result	VME Abs.error	SLAM result	SLAM Std. Dev.	SLAM Abs. error
Θ	0.52°	0.31°	2.75°	2.23°	0.88°	0.98°	0.36°
Φ	0.36°	0.25°	-0.11°	0.47°	0.72°	0.74°	0.36 °
ψ	-0.14°	0.16°	1.89°	2.03°	1.24°	1.84°	1.38°
tx	-0.012 m	0.010 m	0.057m	0.069 m	-0.077 m	0.069 m	0.065 m
ty	-0.243 m	0.019 m	-1.018 m	0.775 m	-0.284 m	0.064 m	0.041 m
tz	0.019m	0.015 m	0.144m	0.125 m	0.018m	0.019 m	0.001 m

In indoor environments

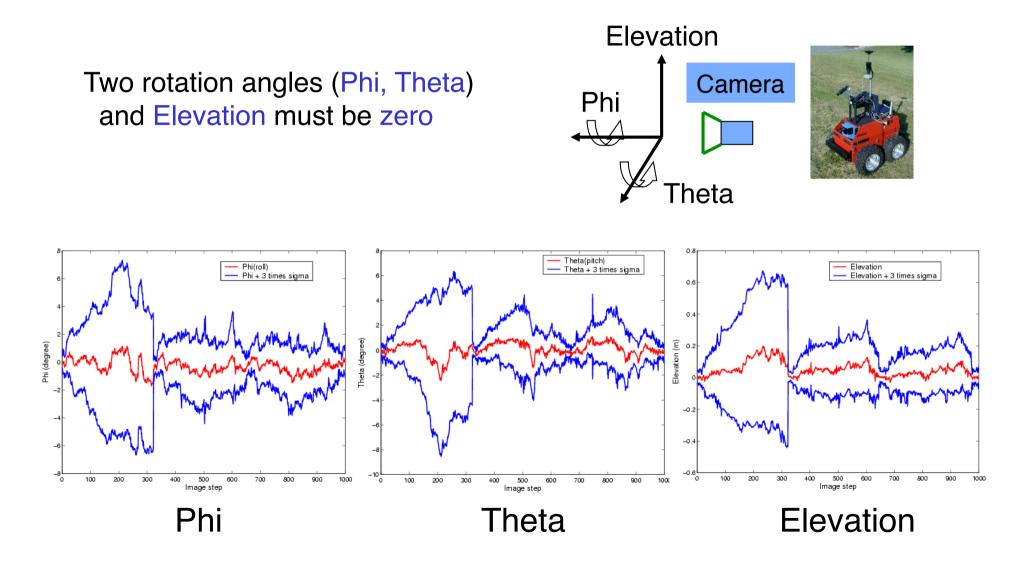
About 30 m long trajectory, 1300 stereo image pairs





In indoor environments

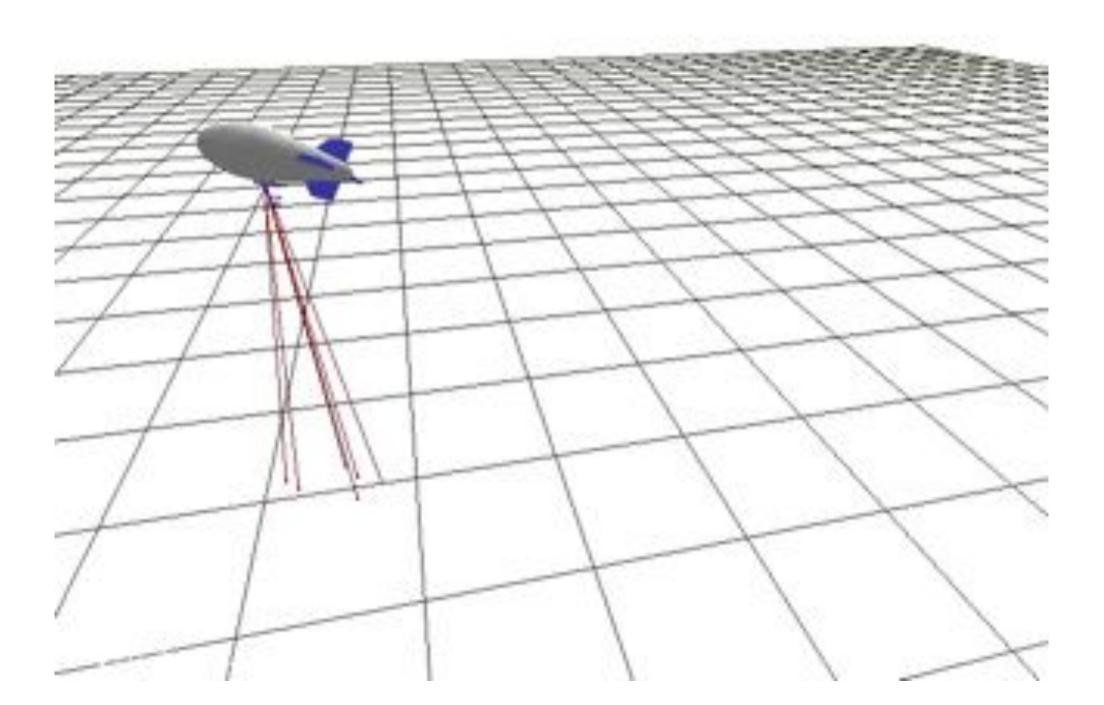
About 30 m long trajectory, 1300 stereo image pairs



With a blimp







SLAM: outline

• Simultaneous localisation and mapping

- Problem presentation
- Basics on estimation
- EKF SLAM
- Main issues
- Vision-based SLAM
 - SLAM with stereovision
 - SLAM with monocular imagery

SLAM with monocular vision

Micro UAVs







Smartphones, wearable devices





SLAM with monocular vision

Prediction: any information on the robot motion

Landmarks:

• interest points = 3D(x, y, z) points

Application of the « usual » SLAM steps:

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Estimation: refinement of the landmark and robot positions

But why is it particularily difficult?

Partial observations! (« bearings-only »)



Bearing-only SLAM

Generic SLAM

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Refinement of the landmark and robot positions

Stereovision SLAM

- \rightarrow Vision : interest points
 - \rightarrow Stereovision
 - \rightarrow Visual motion estimation
- \rightarrow Interest points matching
- \rightarrow Extended Kalman filter

Bearing-only SLAM

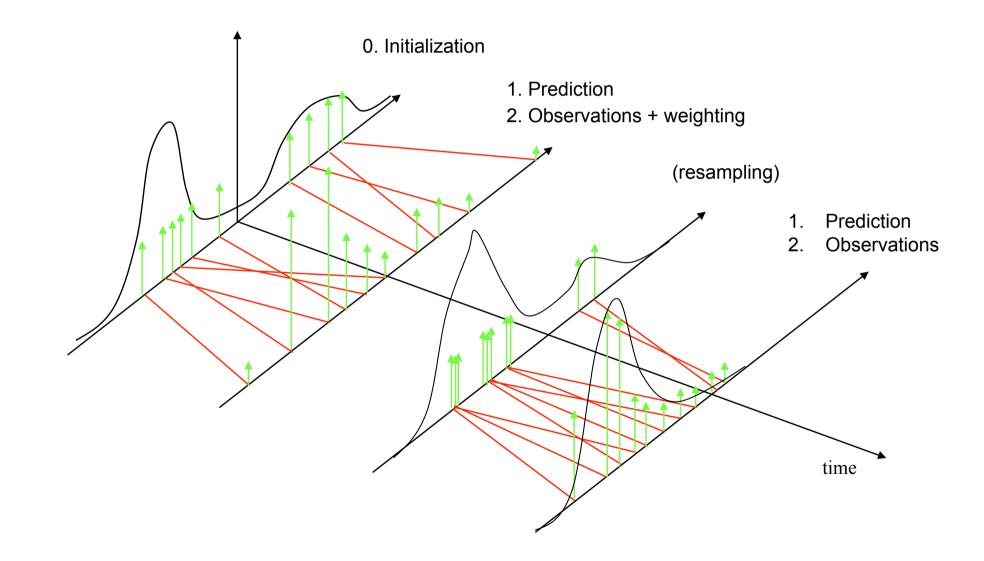
Generic SLAM

- Landmark detection
- Relative observations (measures)
 - Of the landmark positions
 - Of the robot motions
- Observation associations
- Refinement of the landmark and robot positions

Monocular SLAM

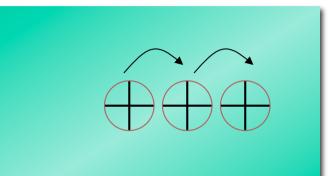
- \rightarrow Vision : interest points
 - \rightarrow « Multi-view stereovision »
 - \rightarrow INS, Motion model...
- \rightarrow Interest points matching
- \rightarrow Extended Kalman filter

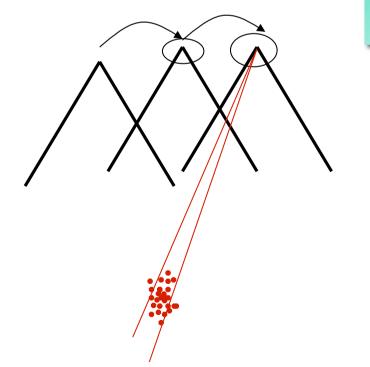
(Particle filtering)



Bearing-only SLAM: landmark initialisation

« Initialisation filter » \approx particle filter

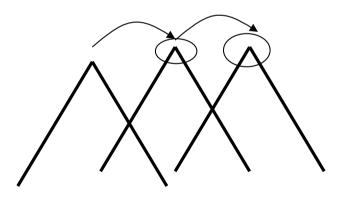


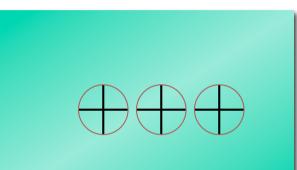


One interest point matched in the image

Bearing-only SLAM: landmark initialisation

« Initialisation filter » \approx particle filter





One interest point matched in the image

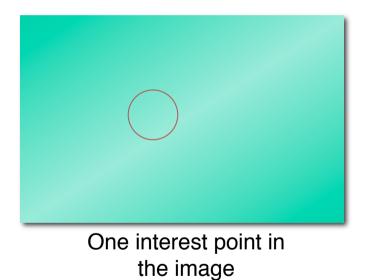
Issues with this approach:

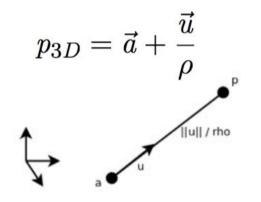
- Complexity
- Some landmarks remain non-observable
- Numerous observations are lost

Landmark initialisation

« Initialisation », 2nd approach: inverse depth parametrization Solution established in 2006 [J. Montiel / A. Davison]:

- *Direct* initialization of a point the first time it is perceived
- Allows to consider points located at the infinite





One landmark in the MAP

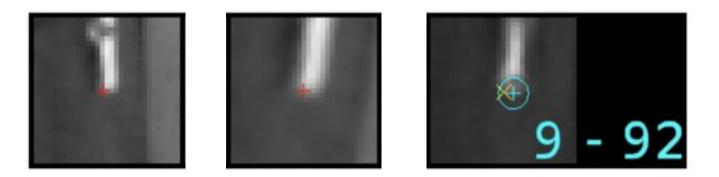
Every detected landmark is directly and <u>immediatly</u> observable

Constant velocity model

Robot state: $\mathcal{R} = (\mathbf{p} \mathbf{q} \mathbf{v} \mathbf{w})^T$

Prediction: $\mathbf{p}^+ = \mathbf{p} + \mathbf{v}.dt$ $\mathbf{q}^+ = \mathbf{q} * \mathbf{w}.dt$ $\mathbf{v}^+ = \mathbf{v}$ $\mathbf{w}^+ = \mathbf{w}$

Allows to focus the data association step:



- 1. Start with a descriptor of the landmark (e.g. appearance at first observation)
- 2. Apply affine transformation to predict the current appearance
- 3. Search the landmark inside the observation uncertainty ellipse

Constant velocity model

Robot state: $\mathcal{R} = (\mathbf{p} \mathbf{q} \mathbf{v} \mathbf{w})^T$

Prediction: $\mathbf{p}^+ = \mathbf{p} + \mathbf{v}.dt$ $\mathbf{q}^+ = \mathbf{q} * \mathbf{w}.dt$ $\mathbf{v}^+ = \mathbf{v}$ $\mathbf{w}^+ = \mathbf{w}$

• simple (no additional sensor required)

• not precise

 \rightarrow bad linearization points

 \rightarrow large search areas

 \rightarrow difficulty to track very high motion

dynamics

• no scale factor estimate possible

Constant acceleration model

Robot state: $\mathcal{R} = (\mathbf{p} \mathbf{q} \mathbf{v} \mathbf{w} \mathbf{v}_{\mathbf{a}} \mathbf{w}_{\mathbf{a}})^T$

Prediction: $\mathbf{v}^+ = \mathbf{v} + \mathbf{v_a} \cdot dt$ $\mathbf{w}^+ = \mathbf{w} + \mathbf{w_a} \cdot dt$ $\mathbf{v_a}^+ = \mathbf{v_a}$ $\mathbf{w_a}^+ = \mathbf{w_a}$

- simple (no additional sensor required)
- not very precise
 - \rightarrow bad linearization points
 - \rightarrow large search areas
- no scale factor estimate possible

Using an inertial measurement unit

Prediction:
$$\mathbf{p}^+ = \mathbf{p} + \mathbf{v} \cdot dt$$

 $\mathbf{q}^+ = \mathbf{q} \otimes v2\mathbf{q} \left((\mathbf{w}_m - \mathbf{w}_b) \cdot dt \right)$
 $\mathbf{v}^+ = \mathbf{v} + (\mathbf{q}2\mathbf{R}(\mathbf{q}) \cdot (\mathbf{a}_m - \mathbf{a}_b) + \mathbf{g}) \cdot dt$
 $\mathbf{a}_b^+ = \mathbf{a}_b$
 $\mathbf{w}_b^+ = \mathbf{w}_b$
 $\mathbf{g}^+ = \mathbf{g}$

additional sensor required

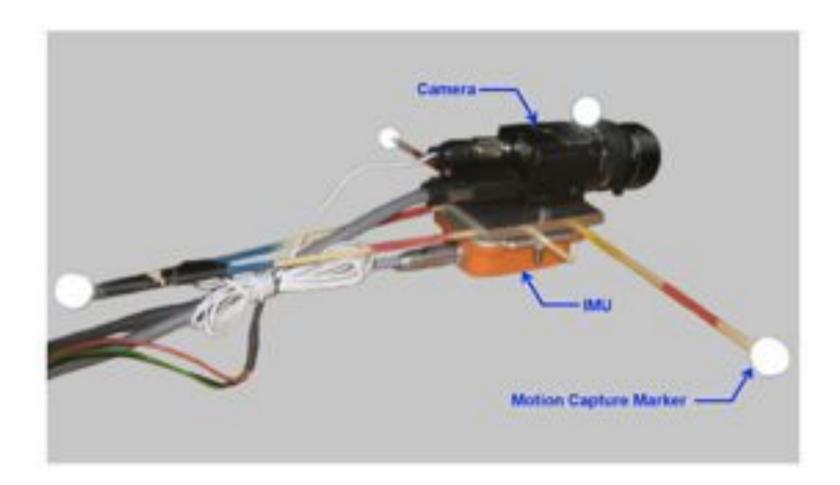
• precise

- \rightarrow good linearization points
- \rightarrow small search areas
- \rightarrow possibility to track very high motion

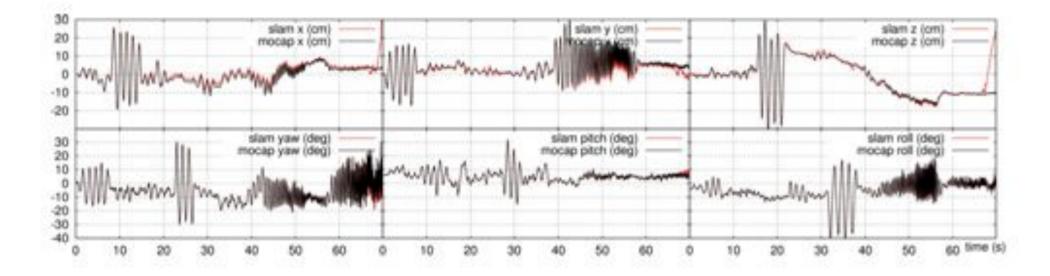
dynamics

• scale factor estimate possible

Using an inertial measurement unit: results



Using an inertial measurement unit: results



Estimated trajectory of the 6 position parameters

Using an inertial measurement unit: results



Using an inertial measurement unit: results



Using an inertial measurement unit: summary

- An additional proprioceptive sensor can help if :
 - high frequency
 - not too noisy
- Can also be directly used in the prediction step if :
 - complete
 - never faulty

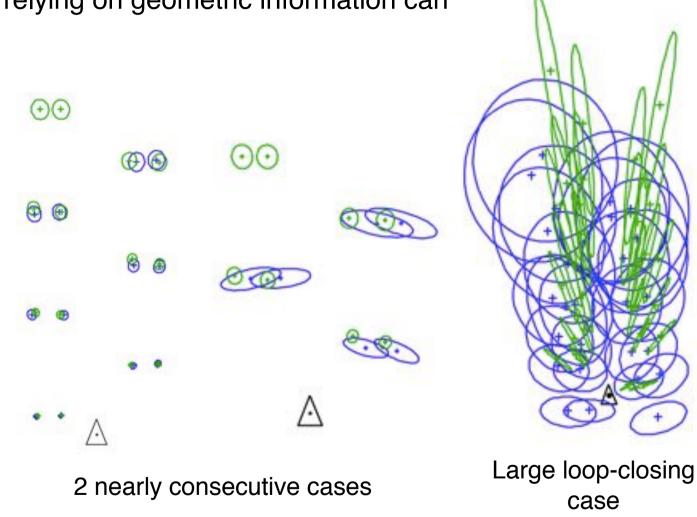
SLAM: outline

- Basics of simultaneous localisation and mapping
- SLAM with monocular vision
 - Solutions to the landmark initialisation problem
 - Importance of the motion prediction, introduction of an IMU
 - What about loop-closing?

A closer look at data association

Data association relying on geometric information can become tricky...

Blue: predicted (mapped) features Green: observed features



→ Better use landmark matching techniques

Overall summary

- Autonomous robots, on the importance of localization
- Localization using dead-reckoning approaches
- SLAM
 - Problem presentation
 - Basics on estimation
 - EKF SLAM
 - Main issues
- Vision-based SLAM
 - SLAM with stereovision
 - SLAM with monocular imagery
 - Solutions to the landmark initialisation problem
 - Illustrations
 - Importance of the motion prediction, introduction of an IMU
 - (Visual loop-closing detection)